

# Effective Approaches to Abstraction Refinement for Automatic Software Verification

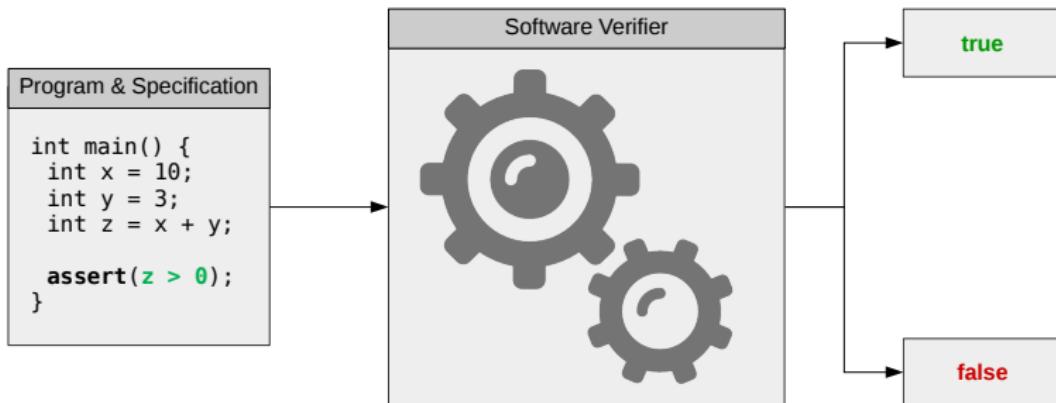
Stefan Löwe

Faculty of Computer Science and Mathematics

—  
University of Passau

March 24, 2017

# Automatic Software Verification



# Automatic Software Verification

**Program & Specification**

```
int main() {
    int x = 10;
    int y = 3;
    int z = x + y;

    assert(z > 0);
}
```

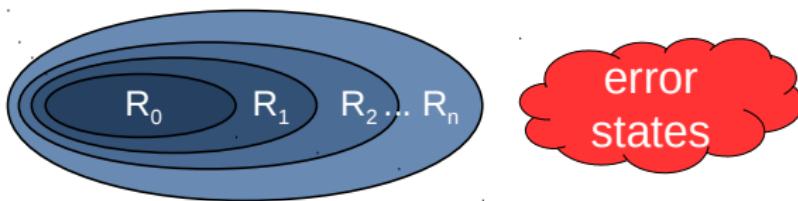
**Software Verifier**

```
reached := {e0}
frontier := {e0}

while frontier ≠ ∅ do
    choose (e) from frontier
    frontier := frontier \ {e}
    foreach e' ∈ post(e) do
        if ¬stop(e', reached) then
            reached := reached ∪ {e'}
            frontier := frontier ∪ {e'}
return reached
```

true

false



# Motivation

## Statement

We want software verification

## Statement

We want software verification that is automatic

## Statement

We want software verification that is automatic, as well as effective

# Software is Full of Devastating, Critical Bugs

-  “Heartbleed” allows sensitive data theft
-  “Shellshock” allows arbitrary code execution
-  “goto-fail” eases man-in-the-middle attack
-  “Ghost” allows arbitrary code execution
-  “Stagefright” allows arbitrary code execution
  
-  New vulnerabilities of your personal computers on a daily basis

# Some even may have Catastrophic Consequences



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?

# Motivation

We want software verification

Agreed

Statement

We want software verification that is automatic

Statement

We want software verification that is automatic, as well as effective

# Doing it Manually is Impossible



# Motivation

We want software verification

Agreed

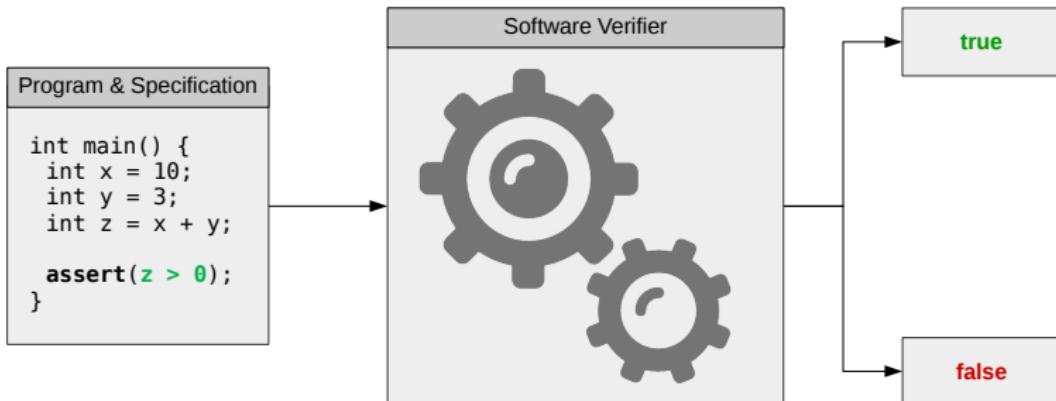
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## Statement

We want software verification that is automatic, as well as effective

# Automatic Software Verification



# Automatic Software Verification for Real-World Programs

**Program & Specification**

```

int ldv_mutex_is_locked_usb_bus_lock(struct mutex *lock)
{
    int nondetermined;
    {
        #line 1495
        if (ldv_mutex_usb_bus_list_lock == 1) {
            #line 1496
            nondetermined = __VERIFIER_nondet_int();
            #line 1501
            if (nondetermined) {
                #line 1502
                return (0);
            }
            #line 1503
            return (1);
        }
    }

    void ldv_mutex_unlock_usb_bus_list_lock(struct mutex *lock)
    {
        {
            #line 1522
            if (ldv_mutex_usb_bus_list_lock == 2) {
                #line 1523
                if (ldv_mutex_usb_bus_list_lock == 1) {
                    #line 1524
                    ldv_error();
                }
                #line 1525
                ldv_mutex_usb_bus_list_lock = 1;
                #line 1526
                return;
            }
        }

        static int ldv_mutex_usbfs_mutex;
        int ldv_mutex_lock_usbfs_mutex(struct mutex *lock)
        {
            int nondetermined;
            {
                #line 1536
                if (ldv_mutex_usbfs_mutex == 1) {
                    #line 1537
                    if (ldv_mutex_usbfs_mutex == 1) {
                        #line 1538
                        nondetermined = __VERIFIER_nondet_int();
                        #line 1542
                        if (nondetermined) {
                            #line 1543
                            ldv_mutex_usbfs_mutex = 2;
                            #line 1544
                            return (0);
                        }
                        #line 1545
                        return (1);
                    }
                }
            }
        }
    }
}

```

**Software Verifier**

```

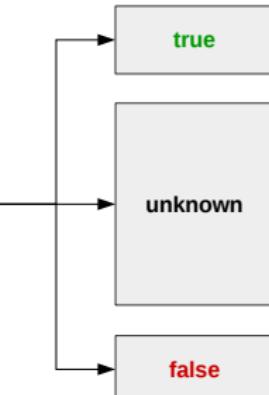
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while frontier ≠ ∅ do
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    frontier := frontier \ {e}

    foreach e' ∈ post(e) do
        if ¬stop(e', reached) then
            reached := reached ∪ {e'}
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return reached

```



# Automatic Software Verification for Real-World Programs

**Program & Specification**

```

int ldv_mutex_is_locked_usb_bus_lock(struct mutex *lock)
{
    int nondetermined;
    #line 1495
    if (ldv_mutex_usb_bus_list_lock == 1) {
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        nondetermined = __VERIFIER_nondet_int();
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        if (nondetermined) {
            #line 1502
            return (0);
        } else {
            #line 1506
            return (1);
        }
    }
}

void ldv_mutex_unlock_usb_bus_list_lock(struct mutex *lock)
{
    #line 1522
    if (ldv_mutex_usb_bus_list_lock == 2) {
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            #line 1524
            ldv_error();
        }
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        #line 1526
        return;
    }
}

static int ldv_mutex_usbfs_mutex;
int ldv_mutex_lock_usbfs_mutex(struct mutex *lock)
{
    int nondetermined;
    #line 1536
    if (ldv_mutex_usbfs_mutex == 1) {
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        if (ldv_mutex_usbfs_mutex == 1) {
            #line 1538
            nondetermined = __VERIFIER_nondet_int();
            #line 1542
            if (nondetermined) {
                #line 1545
                ldv_mutex_usbfs_mutex = 2;
                #line 1546
                return (0);
            } else {
                #line 1550
            }
        }
    }
}

```

**Software Verifier**

```

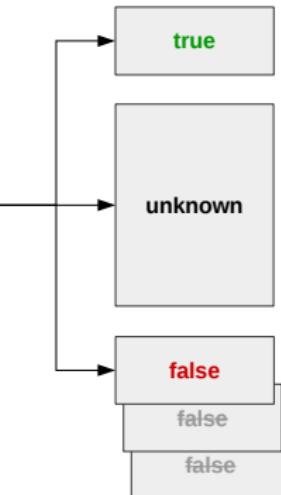
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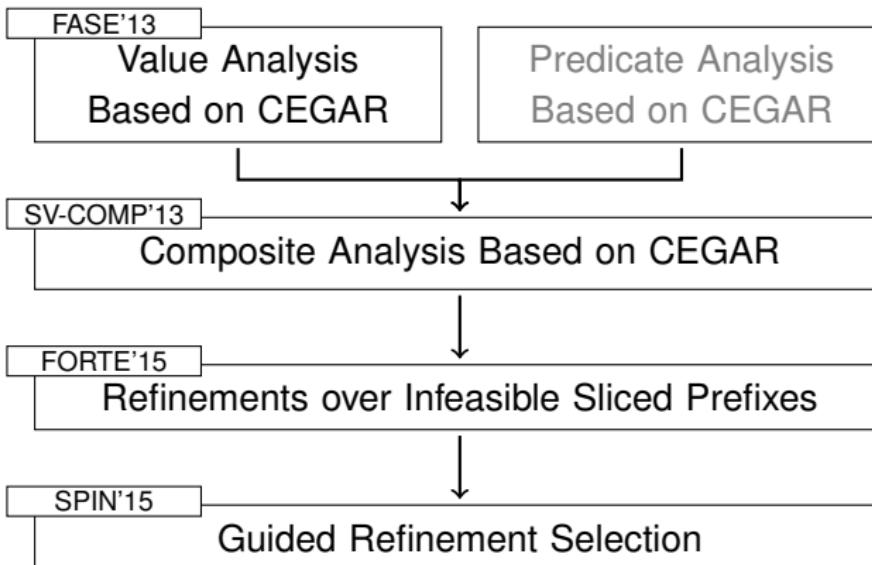
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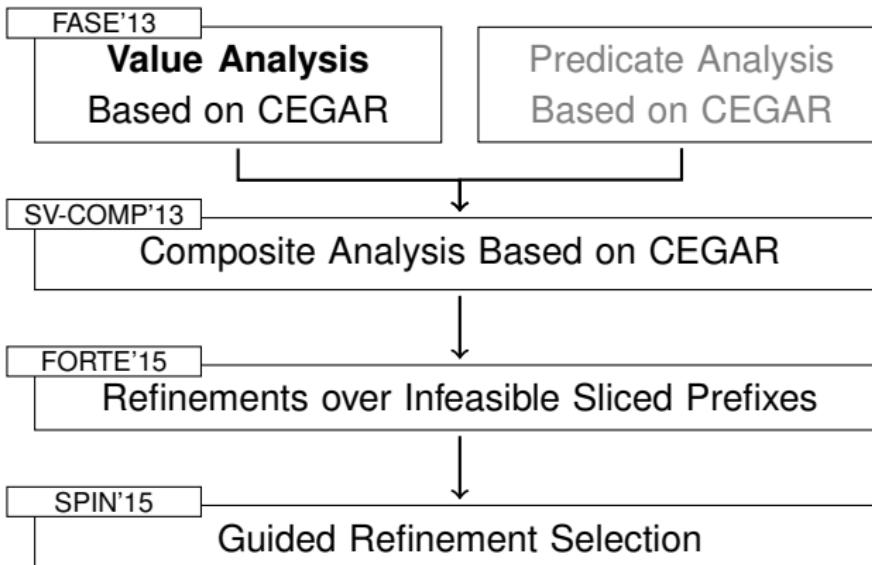
```



# Contributions



# Outline



# Design Decisions and Characteristics

- Contrasts the predominant symbolic analyses
- Does not rely on SAT or SMT solvers
- Tracks concrete assignments of program variables
- Successor computations are simple arithmetic evaluations

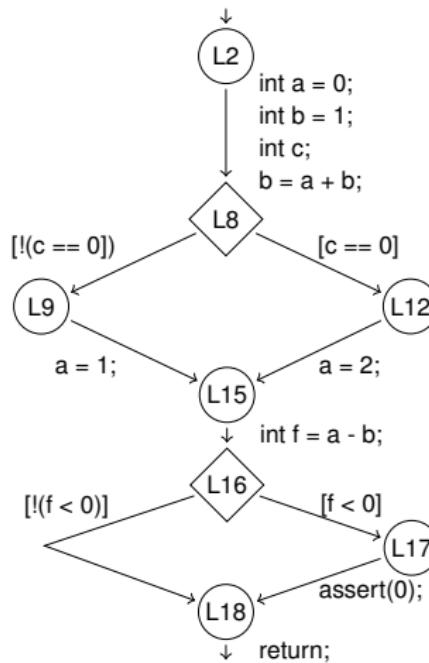
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# Example Program and its Control-Flow Automaton

```

1 #include <assert.h>
2 int main() {
3     int a = 0;
4     int b = 1;
5     int c;
6     b = a + b;
7
8     if (c) {
9         a = 1;
10    }
11    else {
12        a = 2;
13    }
14
15    int f = a - b;
16    if (f < 0) {
17        assert(0);
18    }
19 }
```

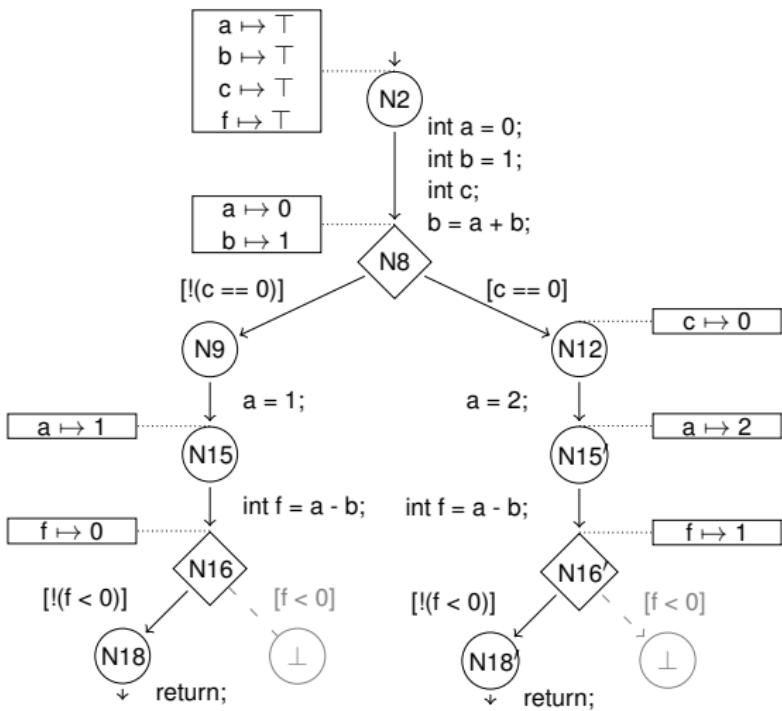


# Example Program and its Abstract Reachability Graph

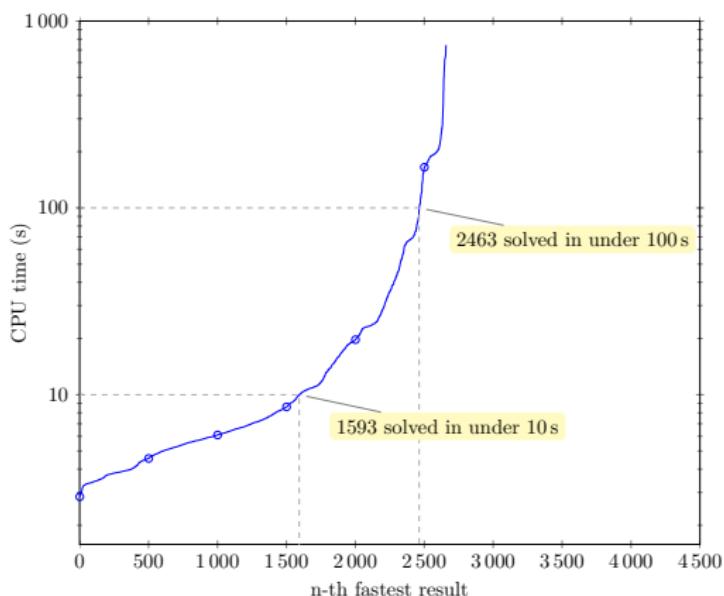
```

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2 int main() {
3     int a = 0;
4     int b = 1;
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8     if (c) {
9         a = 1;
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11    else {
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13    }
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15    int f = a - b;
16    if (f < 0) {
17        assert(0);
18    }
19 }

```

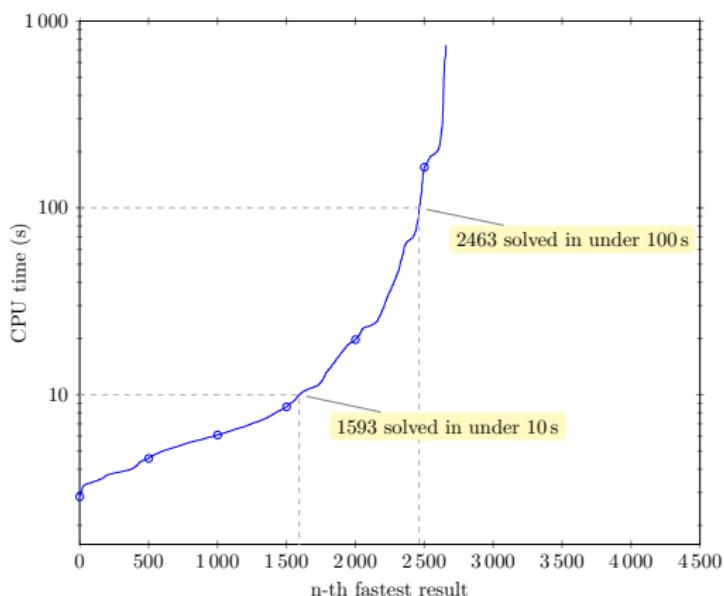


# Value Analysis in Action



- Evaluated on over 4200 verification tasks from SV-COMP'16
- Value Analysis solves almost two thirds
- Under SV-COMP'16 rules, complete evaluation takes 440 hours, i.e., over 18 days
- More than 90 % of the CPU time is wasted for unsolved verification tasks

# Value Analysis in Action

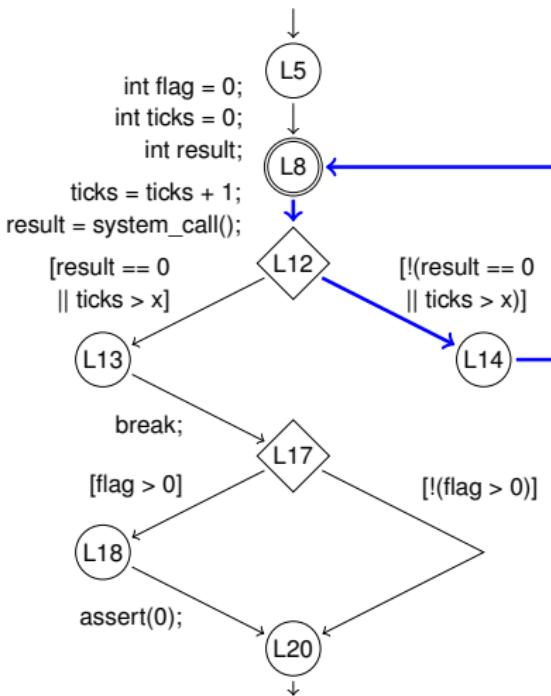


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- Value Analysis solves almost two thirds
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- More than 90 % of the CPU time is wasted for unsolved verification tasks

# State-Space Explosion

```

1 #include <assert.h>
2 extern int system_call();
3
4 int main(int x) {
5     int flag = 0, ticks = 0;
6     int result;
7
8     while(1) {
9         ticks = ticks + 1;
10        result = system_call();
11
12        if(result == 0 || ticks > x) {
13            break;
14        }
15    }
16
17    if(flag > 0) {
18        assert(0);
19    }
20 }
```



# State-Space Explosion

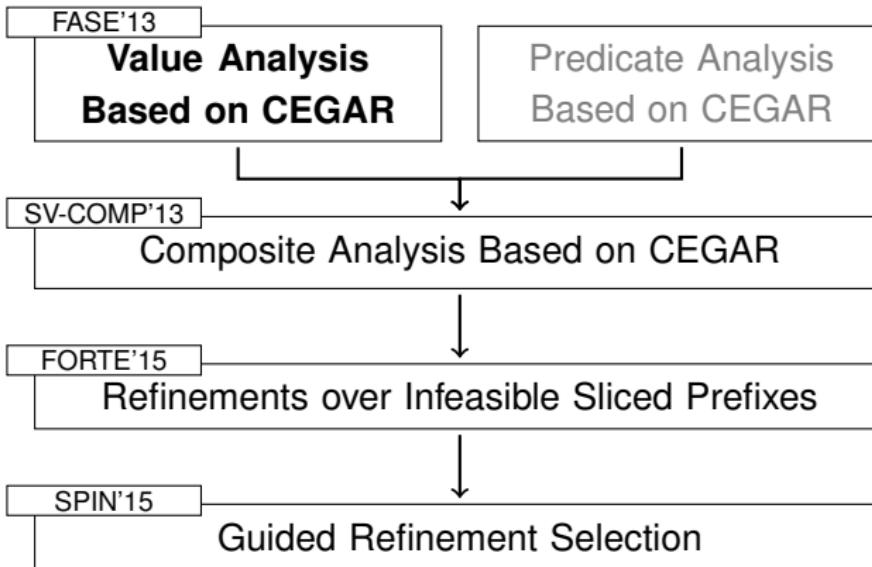
## Problem

The plain Value Analysis suffers from state-space explosion

## Proposition

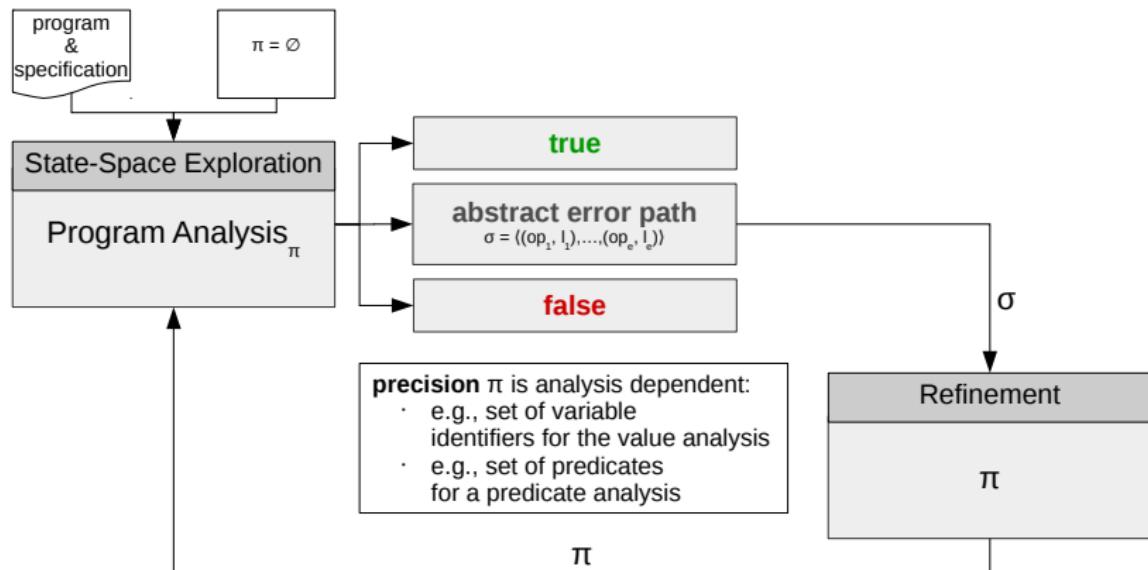
Abstraction techniques could reduce the size of the state space

# Outline



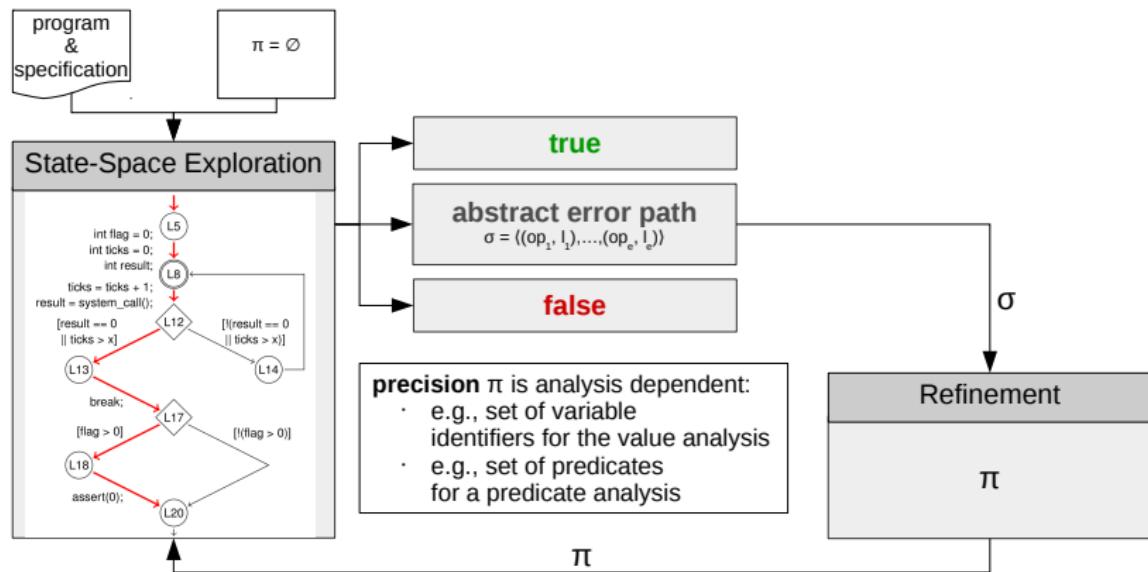
# Counterexample-Guided Abstraction Refinement — CEGAR

CAV'00, Clarke, Grumberg, Jha, Lu, Veith



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# Value Interpolation — Concept

## Definition

A constraint sequence  $\gamma$  is a sequence of program operations, formally,  
 $\gamma = \langle op_1, \dots, op_n \rangle$ , where  $op_1, \dots, op_n$  are program operations

## Examples

The sequence  $\gamma_1 = \langle [flag = 0], [ticks = 0] \rangle$  is a constraint sequence,  
the constraint sequence  $\gamma_2 = \langle [flag = 0], [flag > 0] \rangle$  is contradicting

# Value Interpolation — Concept

FASE'13, Beyer, Löwe

inspired by Interpolation (JSL'57, Craig) and Abstractions from Proofs (POPL'04, Henzinger et al)

## Theorem

*For a pair of constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting, an interpolant  $\Gamma$  is a constraint sequence that fulfills the following three requirements:*

- ① *the implication  $\gamma^- \implies \Gamma$  holds,*
- ② *the conjunction  $\Gamma \wedge \gamma^+$  is contradicting, and*
- ③  *$\Gamma$  contains in its constraints only program variables that occur in the constraints of both  $\gamma^-$  and  $\gamma^+$*

# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

**Output** : an interpolant  $\Gamma$  for  $\gamma^-$  and  $\gamma^+$

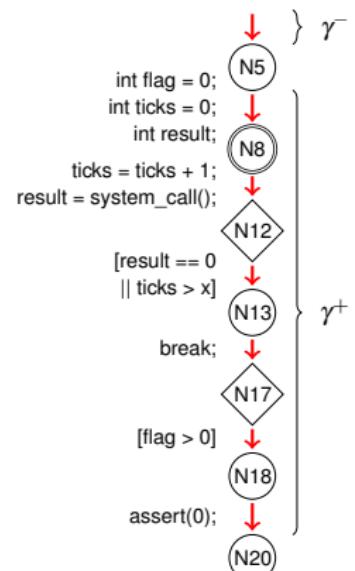
**Variables:** an abstract variable assignment  $v$

```

 $v := \widehat{\text{SP}}_{\gamma^-}(\top);$ 
foreach  $x \in \text{def}(v)$  do
    if  $\widehat{\text{SP}}_{\gamma^+}(v_{|\text{def}(v) \setminus \{x\}}) = \perp$  then
        //  $x$  is irrelevant and must not be in the interpolant
         $v := v_{|\text{def}(v) \setminus \{x\}};$ 
    // start assembling the interpolating constraint sequence
 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do
    // append an assume constraint for  $x$ 
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 
return  $\Gamma$ 

```

---



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


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**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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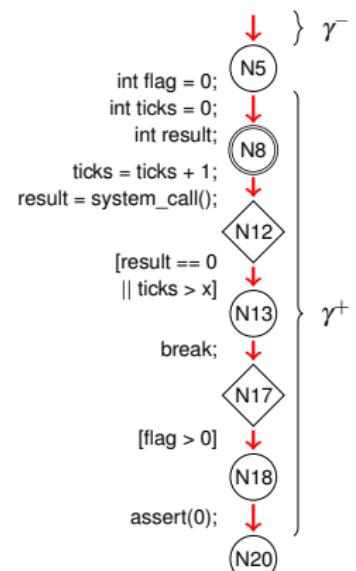
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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 
// start assembling the interpolating constraint sequence
 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do
    // append an assume constraint for x
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 
return  $\Gamma$ 

```

---



## Value Interpolation — Algorithm

---

**Algorithm 1:** Interpolate( $\gamma^-$ ,  $\gamma^+$ )

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

**Output** : an interpolant  $\Gamma$  for  $\gamma^-$  and  $\gamma^+$

**Variables:** an abstract variable assignment  $v$

$v := \widehat{\text{SP}}_v(\top); // \rightarrow v = \top$

```

reach  $x \in \text{def}(v)$  do
  if  $\widehat{\text{SP}}_{\gamma^+}(V_{|\text{def}(v) \setminus \{x\}}) = \perp$  then
    //  $x$  is irrelevant and must not be in the interpolant
     $V := V_{|\text{def}(v) \setminus \{x\}|}$ ;

```

*// start assembling the interpolating constraint sequence*

[ i = \langle \rangle ]

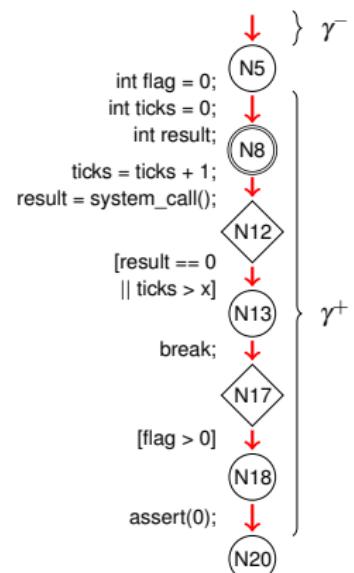
**foreach**  $x \in \text{def}(v)$  **do**

// append an assume constraint for x

$$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$$

```
return Γ //→ Γ = {}
```

$$\Gamma_{N5} = \langle \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


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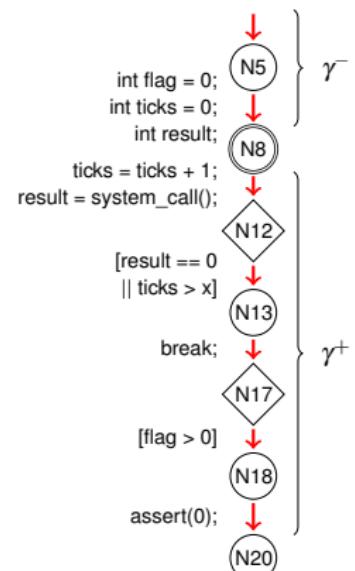
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return  $\Gamma$ 

```

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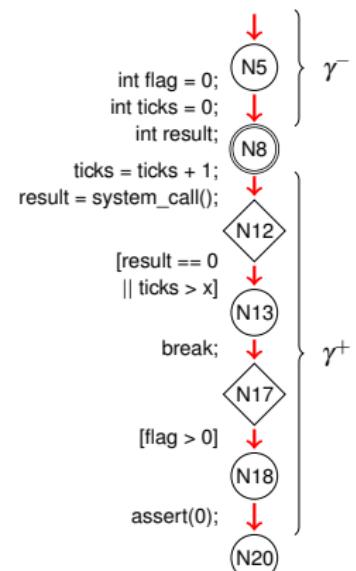
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**foreach**  $x \in \text{def}(v)$  **do**

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*// ticks is irrelevant and must not be in the interpolant*

$v := v_{|\text{def}(v) \setminus \{x\}};$

*// start assembling the interpolating constraint sequence*

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

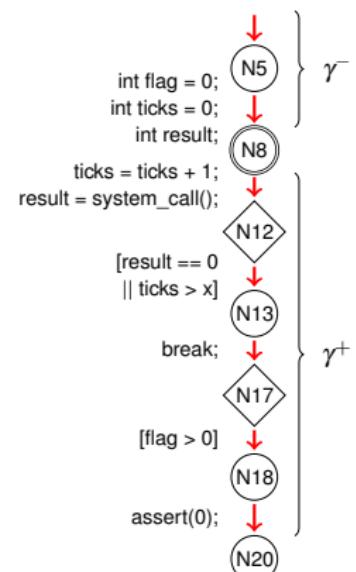
*// append an assume constraint for x*

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**return**  $\Gamma$

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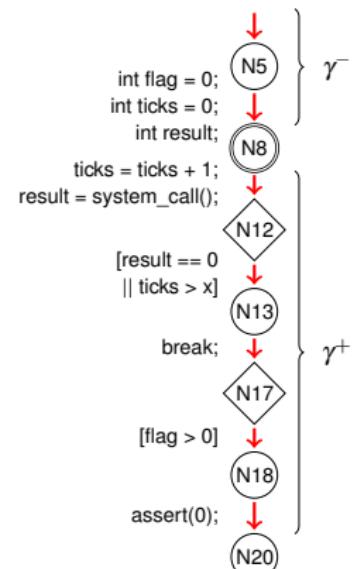
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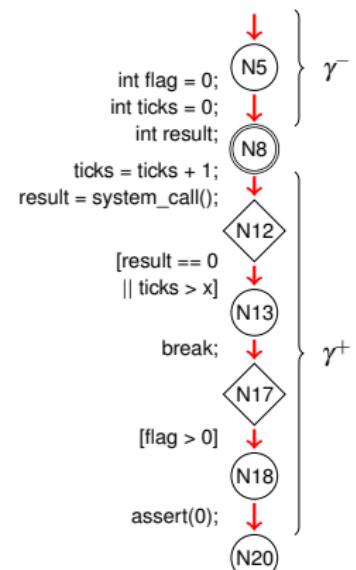
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```

*// start assembling the interpolating constraint sequence*

```

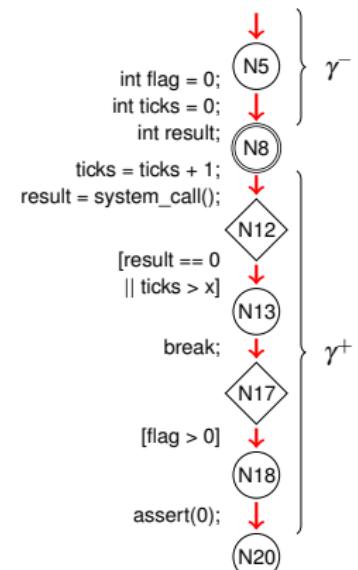
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foreach  $x \in \text{def}(v)$  do
    // append an assume constraint for x
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 

```

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

**Output** : an interpolant  $\Gamma$  for  $\gamma^-$  and  $\gamma^+$

**Variables:** an abstract variable assignment  $v$

```

 $v := \widehat{\text{SP}}_{\gamma^-}(\top); // \rightarrow v = \{\text{flag} \mapsto 0; \text{ticks} \mapsto 0\}$ 
foreach  $x \in \text{def}(v)$  do
    if  $\widehat{\text{SP}}_{\gamma^+}(v_{|\text{def}(v) \setminus \{x\}}) = \perp$  then
        // x is irrelevant and must not be in the interpolant
         $v := v_{|\text{def}(v) \setminus \{x\}};$ 

```

*// start assembling the interpolating constraint sequence*

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

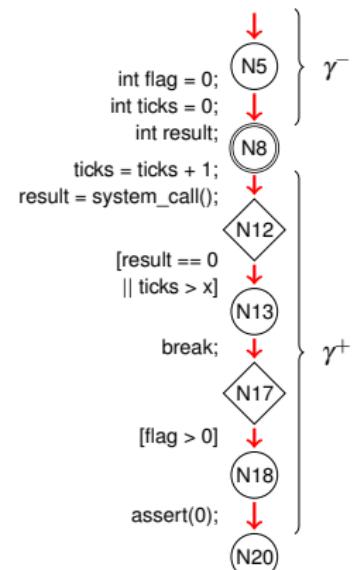
*// append an assume constraint for flag*

$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle$$



## Value Interpolation — Algorithm

---

**Algorithm 1:** Interpolate( $\gamma^-$ ,  $\gamma^+$ )

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

**Output** : an interpolant  $\Gamma$  for  $\gamma^-$  and  $\gamma^+$

**Variables:** an abstract variable assignment  $v$

```

 $v := \widehat{\text{SP}}_{\gamma^+}(\top); // \rightarrow v = \{\text{flag} \mapsto 0; \text{ticks} \mapsto 0\}$ 
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  if  $\widehat{\text{SP}}_{\gamma^+}(v|_{\text{def}(v) \setminus \{x\}}) = \perp$  then
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```

// start assembling the interpolating constraint sequence

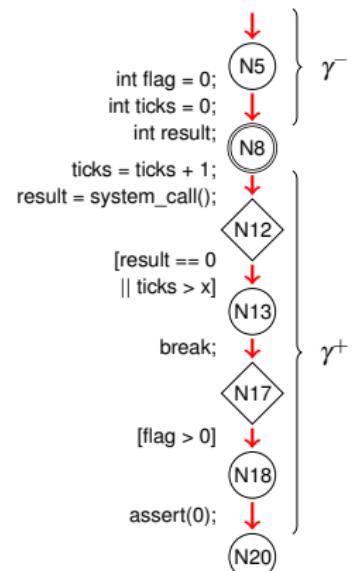
$\Gamma := \langle \rangle$

**foreach**  $x \in \text{def}(v)$  **do**

// append an assume constraint for x

$$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$$

```
return Γ //→ Γ = ⟨[flag = 0]⟩
```



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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**Variables:** an abstract variable assignment  $v$

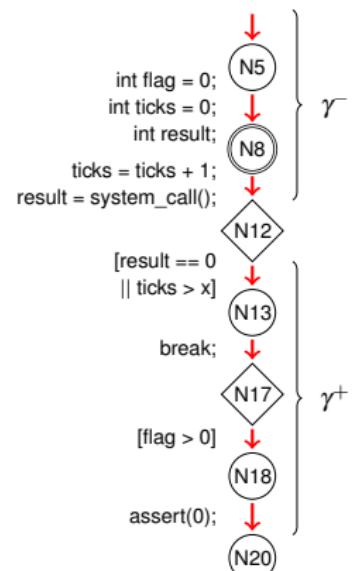
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 $\Gamma := \langle \rangle;$ 
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    // append an assume constraint for x
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 
return  $\Gamma$ 

```

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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```

*// start assembling the interpolating constraint sequence*

$\Gamma := \langle \rangle;$

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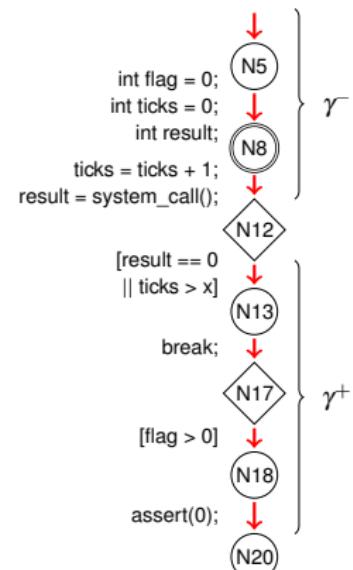
*// append an assume constraint for x*

$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:** Interpolate( $\gamma^-$ ,  $\gamma^+$ )
 

---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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// start assembling the interpolating constraint sequence

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

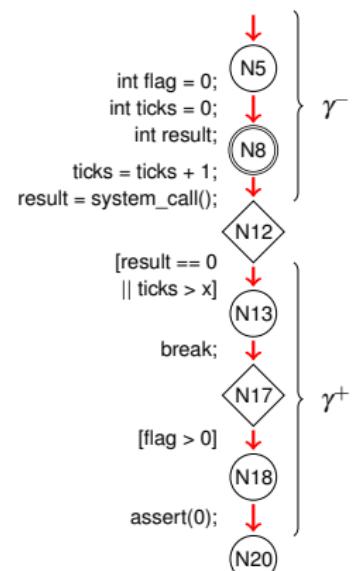
// append an assume constraint for  $x$

$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


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**Variables:** an abstract variable assignment  $v$

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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 

```

// start assembling the interpolating constraint sequence

```

 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do

```

// append an assume constraint for  $x$   
 $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

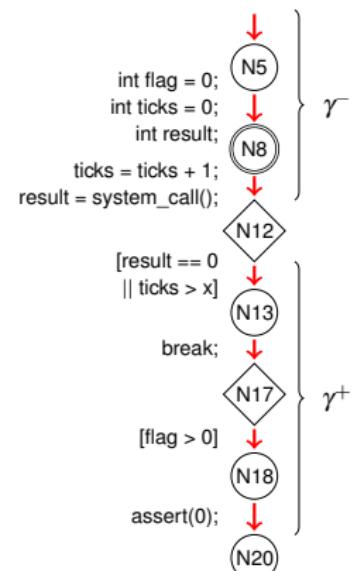
```

return  $\Gamma$ 

```

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

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**Variables:** an abstract variable assignment  $v$

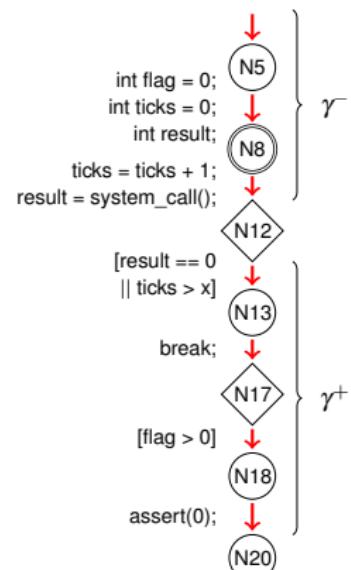
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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 
    // start assembling the interpolating constraint sequence
     $\Gamma := \langle \rangle;$ 
    foreach  $x \in \text{def}(v)$  do
        // append an assume constraint for  $x$ 
         $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 
return  $\Gamma$ 

```

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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**Variables:** an abstract variable assignment  $v$

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        // x is irrelevant and must not be in the interpolant
         $v := v_{|\text{def}(v) \setminus \{x\}};$ 

```

*// start assembling the interpolating constraint sequence*

```

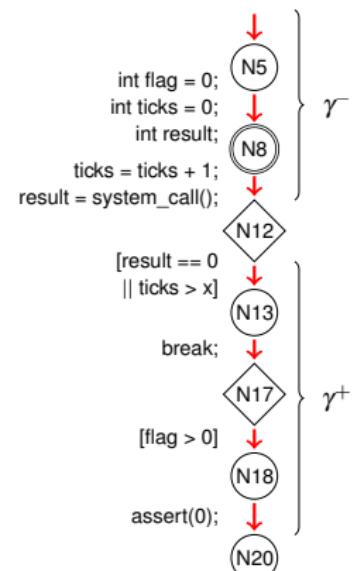
 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do
    // append an assume constraint for x
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 

```

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 

```

*// start assembling the interpolating constraint sequence*

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

*// append an assume constraint for flag*

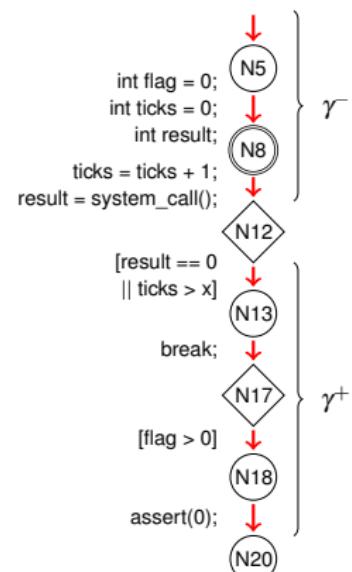
$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

---

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

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**Output** : an interpolant  $\Gamma$  for  $\gamma^-$  and  $\gamma^+$

**Variables:** an abstract variable assignment  $v$

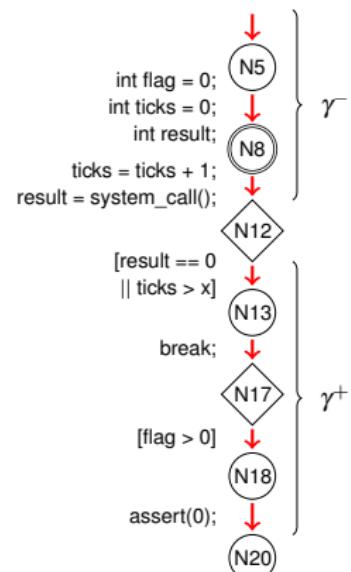
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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 
// start assembling the interpolating constraint sequence
 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do
    // append an assume constraint for x
     $\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$ 
return  $\Gamma // \rightarrow \Gamma = \langle [\text{flag} = 0] \rangle$ 

```

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle, \Gamma_{N12} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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```

// start assembling the interpolating constraint sequence

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

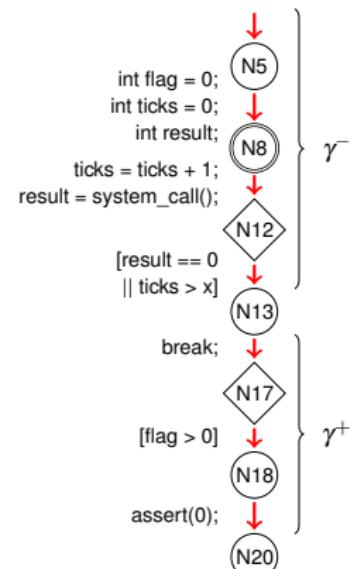
// append an assume constraint for  $x$

$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

**return**  $\Gamma$

---

$$\Gamma_{N5} = \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle, \Gamma_{N12} = \langle [\text{flag} = 0] \rangle, \Gamma_{N13} = \langle [\text{flag} = 0] \rangle$$



# Value Interpolation — Algorithm

---

**Algorithm 1:** Interpolate( $\gamma^-$ ,  $\gamma^+$ )
 

---

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     $v := v_{|\text{def}(v) \setminus \{x\}};$ 
  
```

// start assembling the interpolating constraint sequence

$\Gamma := \langle \rangle;$

**foreach**  $x \in \text{def}(v)$  **do**

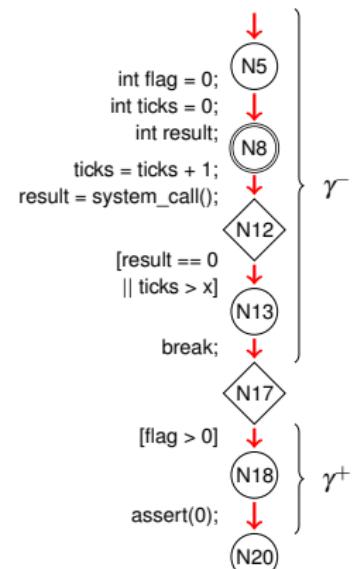
// append an assume constraint for  $x$

$\Gamma := \Gamma \wedge \langle [x = v(x)] \rangle;$

**return**  $\Gamma$

---

$$\begin{aligned}\Gamma_{N5} &= \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle, \Gamma_{N12} = \langle [\text{flag} = 0] \rangle, \Gamma_{N13} = \langle [\text{flag} = 0] \rangle, \\ \Gamma_{N17} &= \langle [\text{flag} = 0] \rangle\end{aligned}$$



# Value Interpolation — Algorithm

---

**Algorithm 1:**  $\text{Interpolate}(\gamma^-, \gamma^+)$ 


---

**Input** : two constraint sequences  $\gamma^-$  and  $\gamma^+$ , such that  $\gamma^- \wedge \gamma^+$  is contradicting

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         $v := v_{|\text{def}(v) \setminus \{x\}};$ 

```

// start assembling the interpolating constraint sequence

```

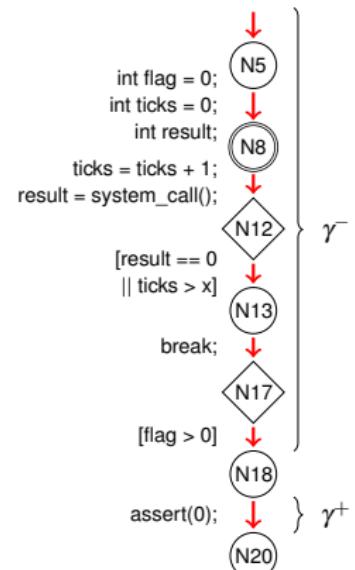
 $\Gamma := \langle \rangle;$ 
foreach  $x \in \text{def}(v)$  do
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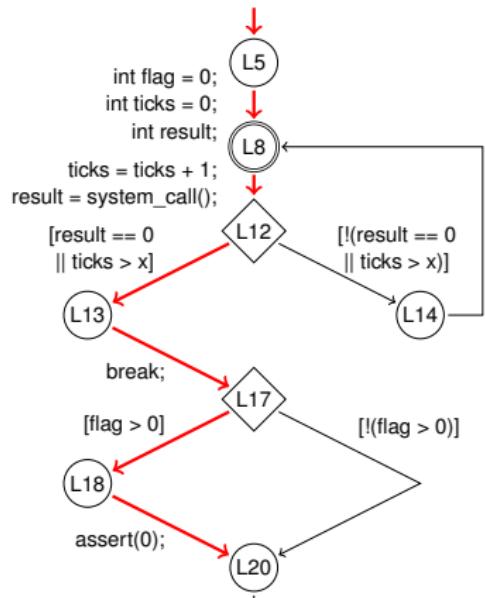
**return**  $\Gamma$

---

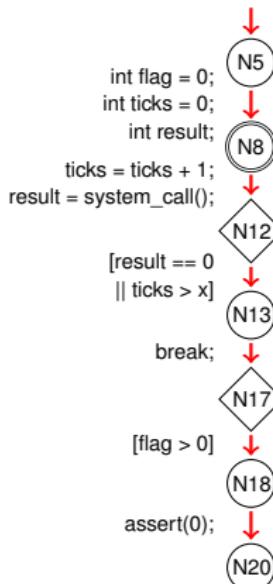
$$\begin{aligned} \Gamma_{N5} &= \langle \rangle, \Gamma_{N8} = \langle [\text{flag} = 0] \rangle, \Gamma_{N12} = \langle [\text{flag} = 0] \rangle, \Gamma_{N13} = \langle [\text{flag} = 0] \rangle, \\ \Gamma_{N17} &= \langle [\text{flag} = 0] \rangle, \Gamma_{N18} = \langle \rangle, \Gamma_{N20} = \langle \rangle \end{aligned}$$



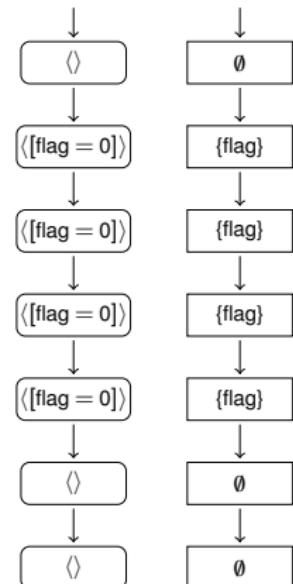
# Value Refinement Completed



verification task



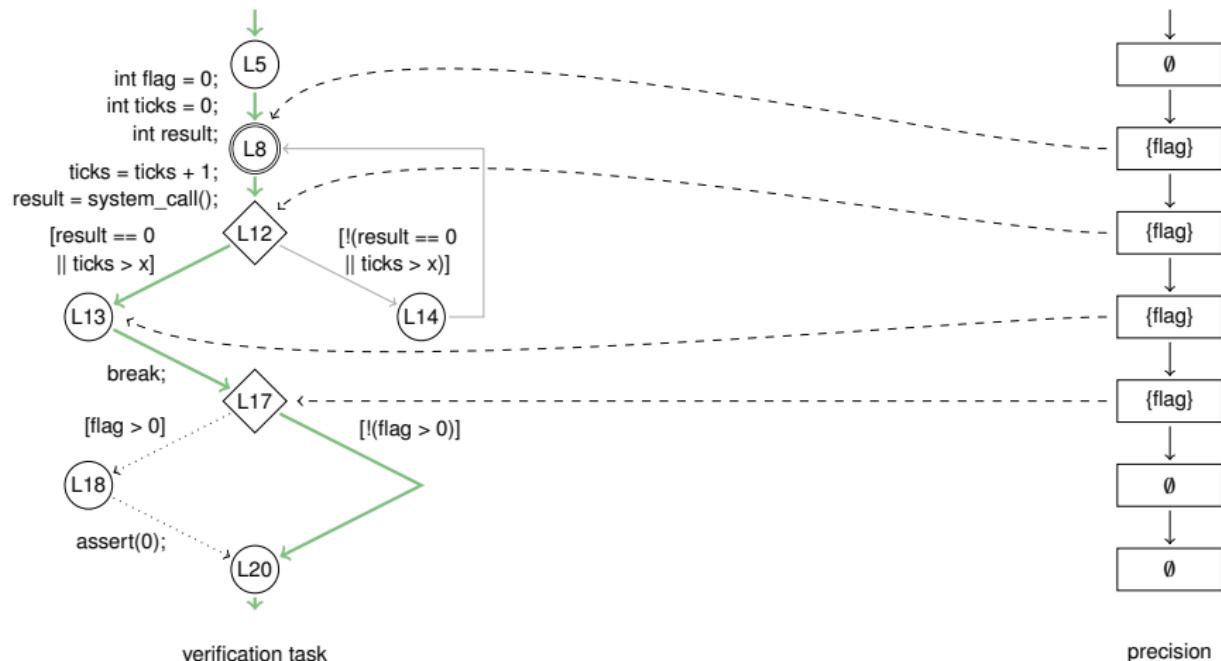
error path



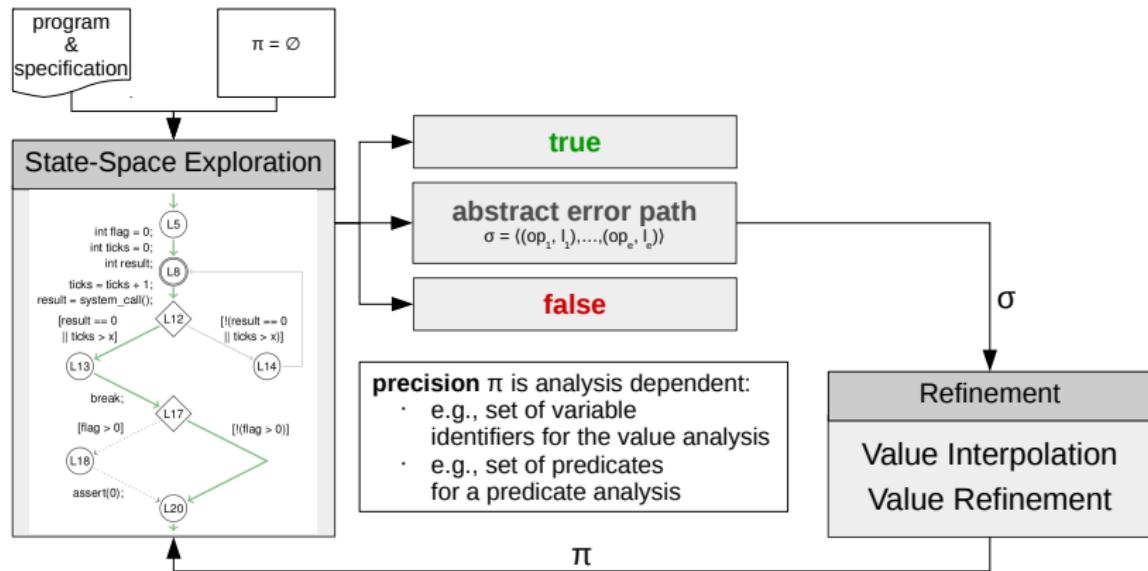
interpolants

precision

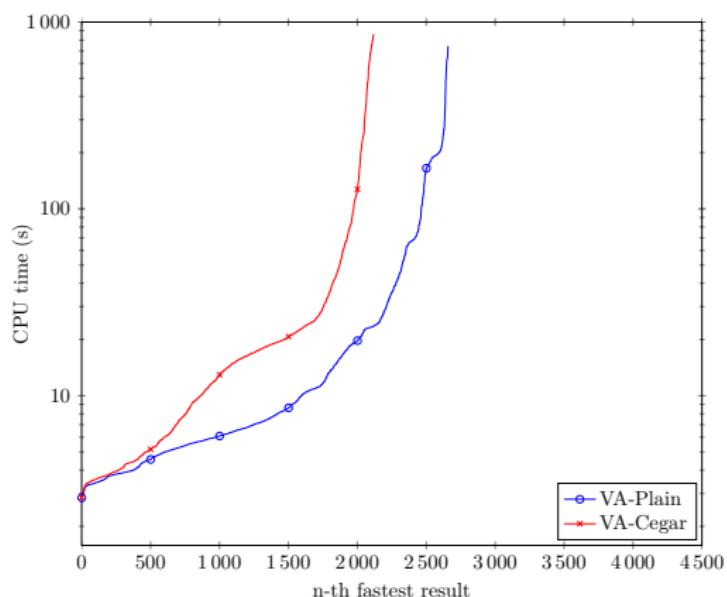
# Value Refinement Avoids Counterexample and Loop



# One Iteration of the CEGAR Loop Completed



# Value Analysis Based on CEGAR in Action



- Significant improvements for some verification tasks
- Significant regressions for other verification tasks
- Value Analysis based on CEGAR solves about 500 verification task *less*

# Value Analysis Based on CEGAR in Action

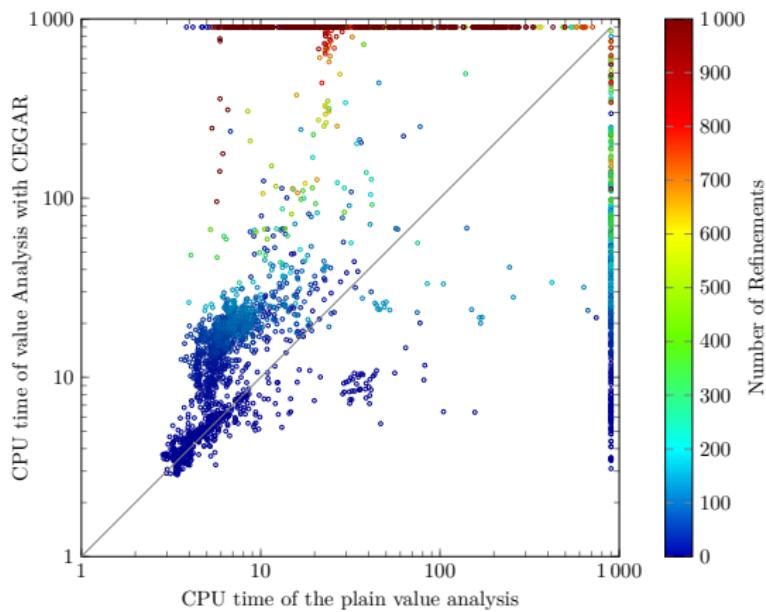
## New Problem

The Value Analysis based on CEGAR is, in total, less effective

## Proposition

Inspect the overhead introduced by CEGAR

# Value Analysis Based on CEGAR — Number of Refinements

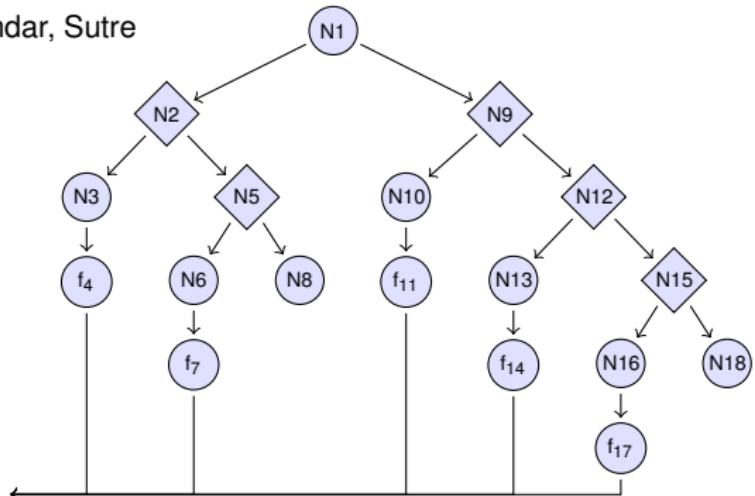
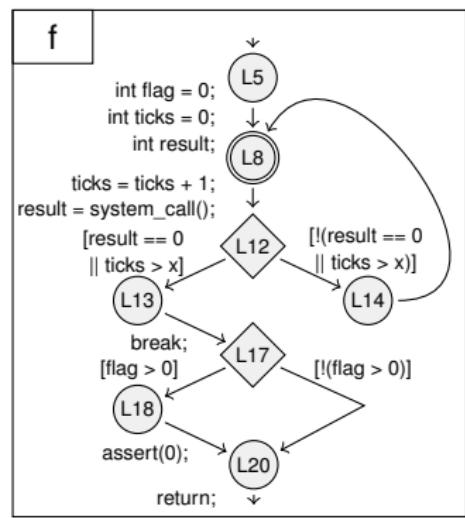


## Insights:

- Solved by both:  
usually < 200 refinements
- Solved only by VA-Cegar:  
usually < 500 refinements
- Solved only by VA-Plain:  
usually > 1 000 refinements

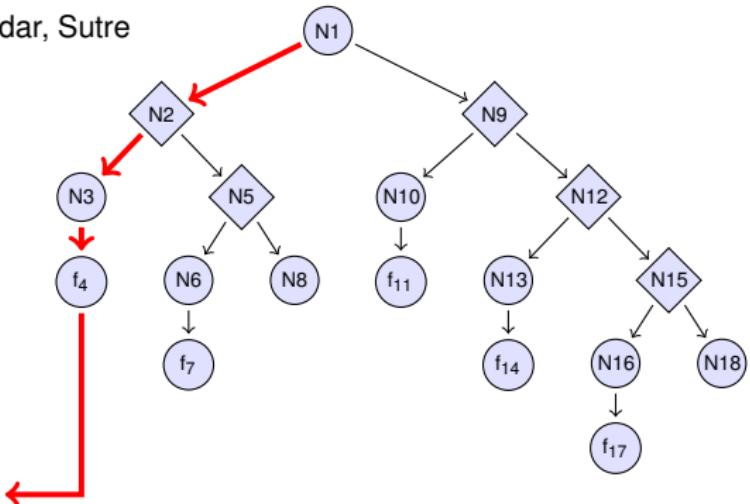
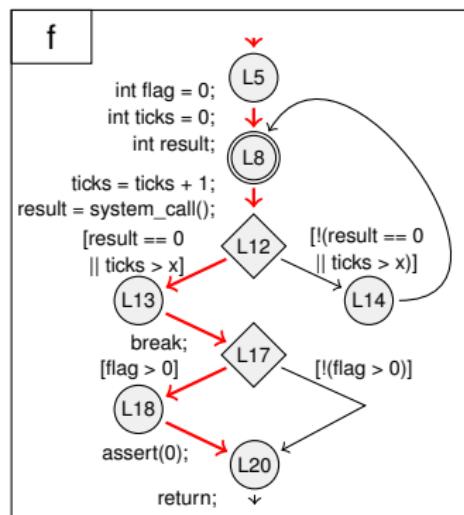
# Lazy Abstraction — Principle

POPL'02, Henzinger, Jhala, Majumdar, Sutre



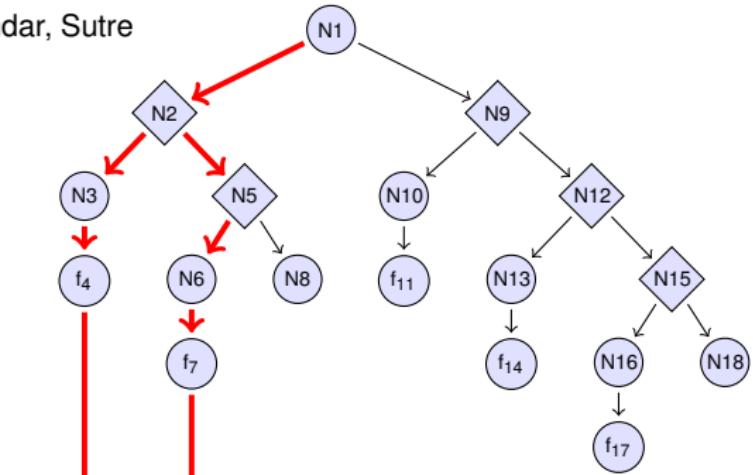
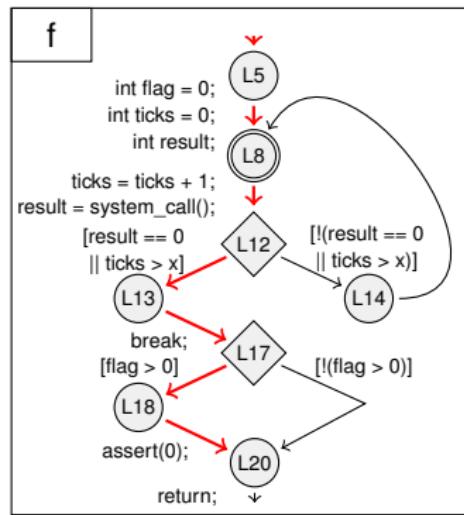
# Lazy Abstraction Often Leads to Repeated Refinements

POPL'02, Henzinger, Jhala, Majumdar, Sutre



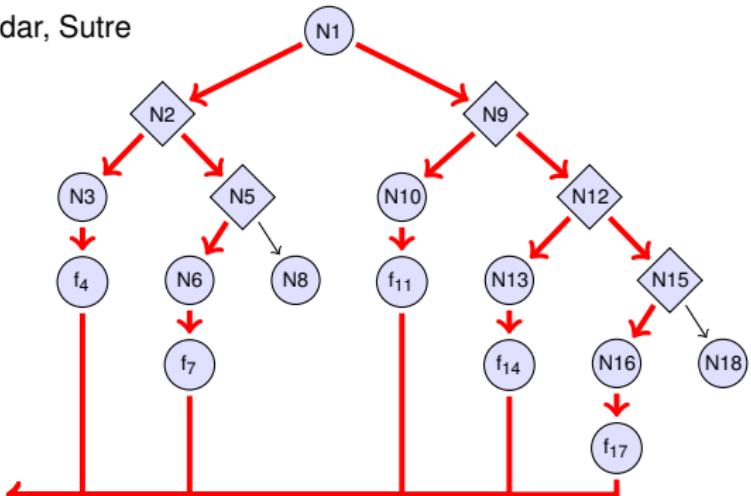
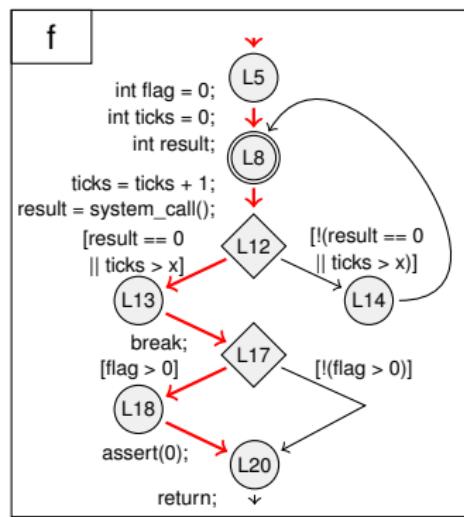
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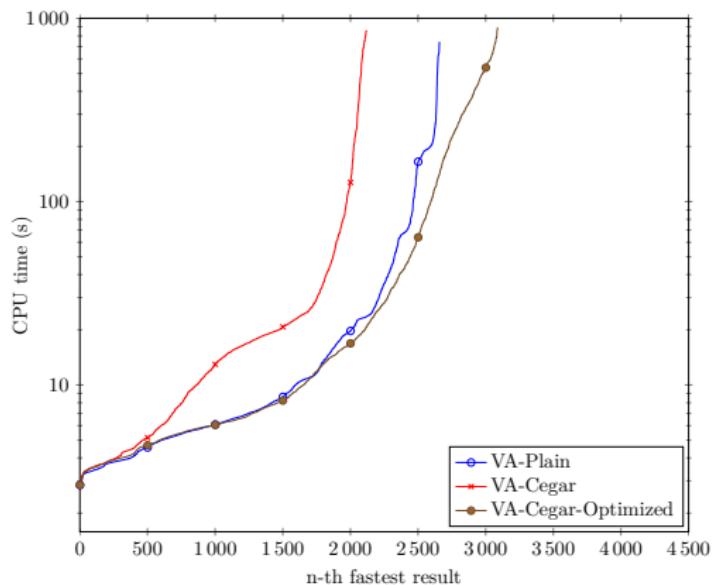


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POPL'02, Henzinger, Jhala, Majumdar, Sutre

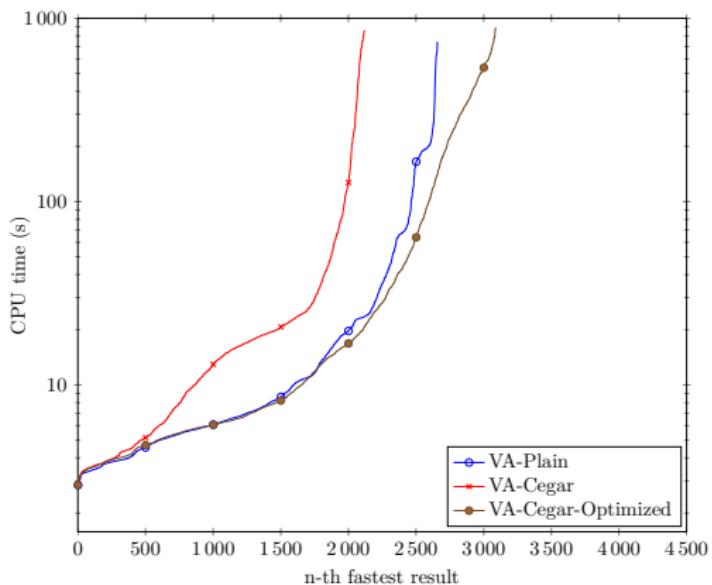


# Value Analysis Based on Optimized CEGAR in Action



- Lazy abstraction unsuitable
- Prefer scoped precision** over localized precision
- Prefer restart at root** over restart deep within state space

# Value Analysis Based on Optimized CEGAR in Action



- Lazy abstraction unsuitable
- Prefer scoped precision** over localized precision
- Prefer restart at root** over restart deep within state space
- Value Refinement applicable to other analyses
  - Octagon Analysis
  - Symbolic Execution

# Value Analysis Based on CEGAR — Summary

## Solution

The integration of CEGAR results in a more effective analysis

## Problem

The Value Analysis still cannot handle non-determinism well

```
1 #include <assert.h>
2 int main() {
3     int a;
4     if (a != 1) {
5         if (a == 1)
6             assert(0);
7     }
8 }
```

The Value Analysis wrongly reports **FALSE** for this verification task

# Value Analysis Based on CEGAR — Summary

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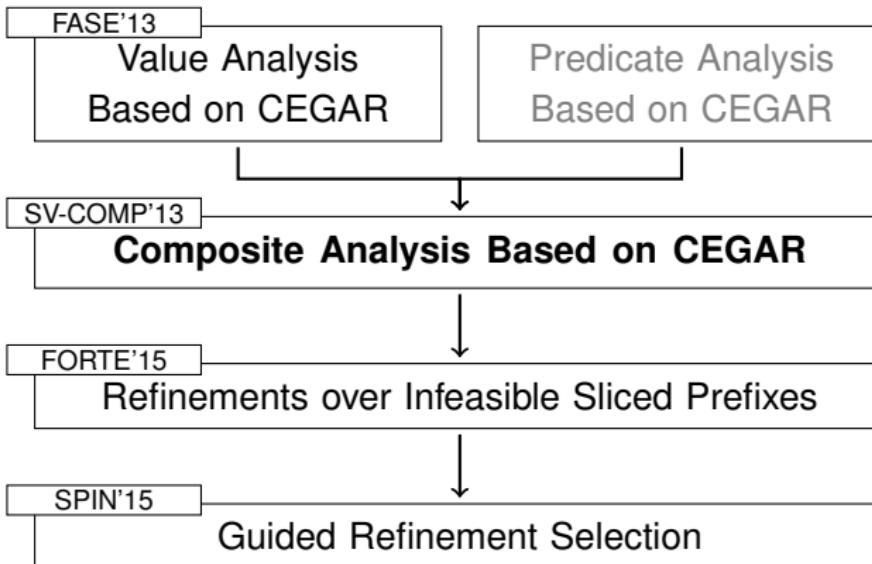
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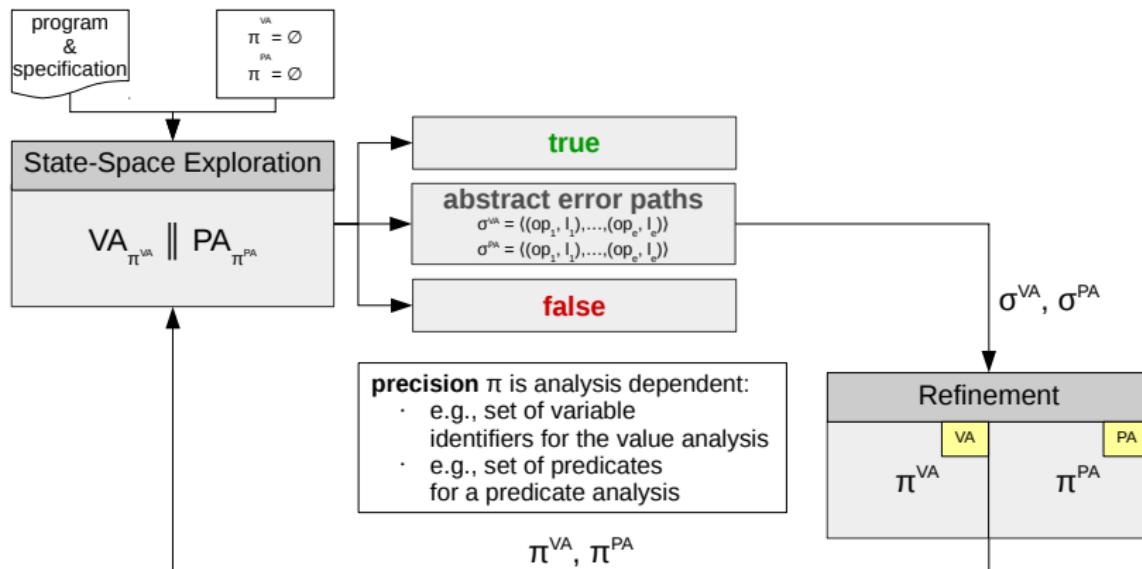
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# Outline



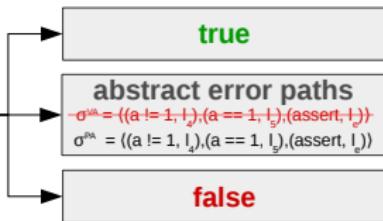
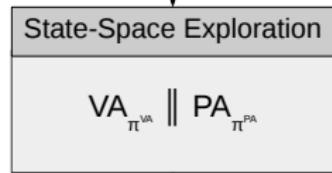
# Composite Analysis Based on CEGAR

SV-COMP'13, Löwe



# Composite Analysis Based on CEGAR

SV-COMP'13, Löwe



**precision  $\pi$  is analysis dependent:**

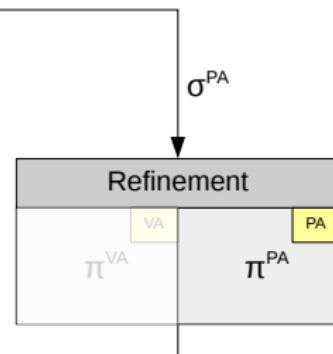
- e.g., set of variable identifiers for the value analysis
- e.g., set of predicates for a predicate analysis

$\pi^{PA}$

```

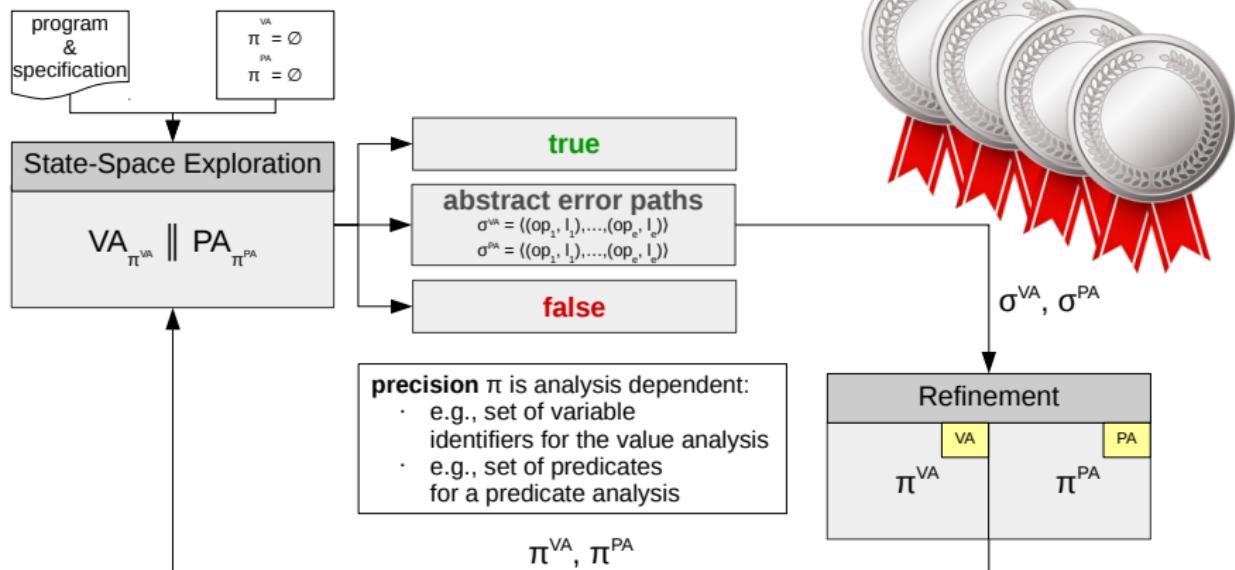
4   if (a != 1) {
5     if (a == 1)
6       assert(0);

```



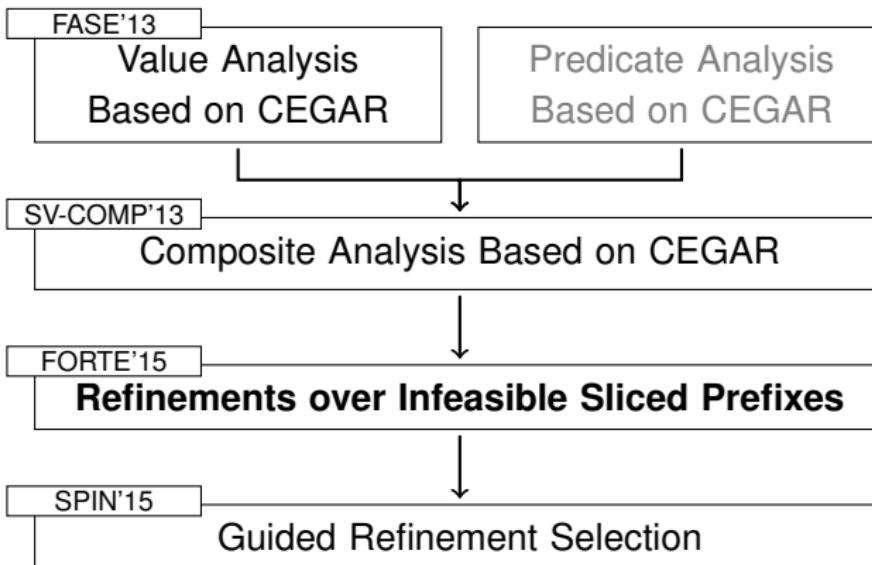
# Composite Analysis Based on CEGAR

SV-COMP'13, Löwe



Wins four silver medals in SV-COMP'13, including “Overall”

# Outline



# Interpolation-Based Refinement

## Statement

Interpolation is ideally suited for refinement of precision

# Interpolation-Based Refinement

## Statement

Interpolation is ideally suited for refinement of precision

**Unfortunately, this is only true in theory**

## Problem

In practice, we distinguish between “good” or “bad” refinements  
which are the result of “good” or “bad” interpolants

# “Good” and “Bad” Interpolants

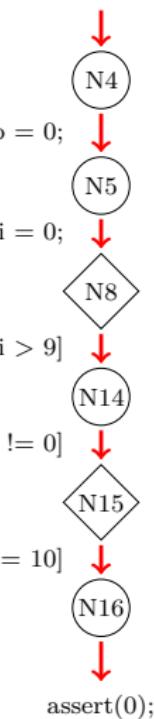
```
1 #include <assert.h>
2 extern int f(int x);
3 int main() {
4     int b = 0;
5     int i = 0;
6
7     while(1) {
8         if(i > 9) {
9             break;
10        }
11        f(i++);
12    }
13
14    if(b != 0) {
15        if(i != 10) {
16            assert(0);
17        }
18    }
19 }
```

verification task

# “Good” and “Bad” Interpolants

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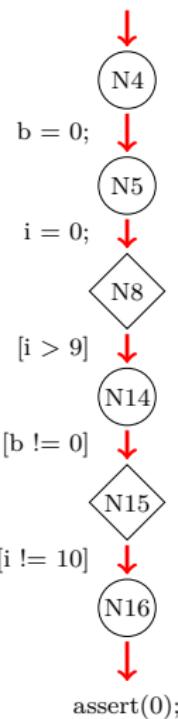
verification task

error path

# “Good” and “Bad” Interpolants

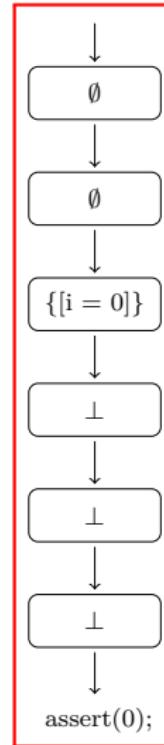
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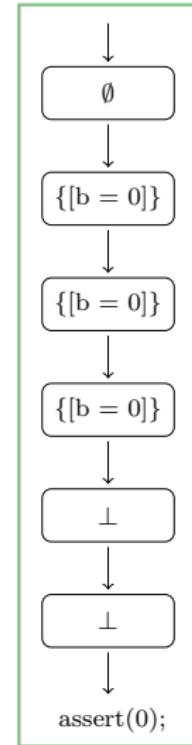


verification task

error path



bad sequence



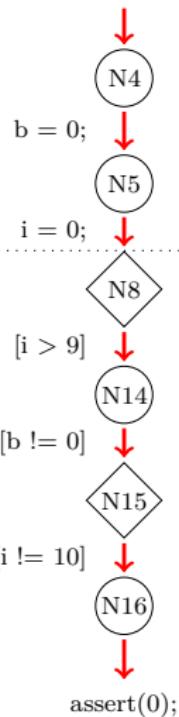
good sequence

# “Good” and “Bad” Interpolants

```

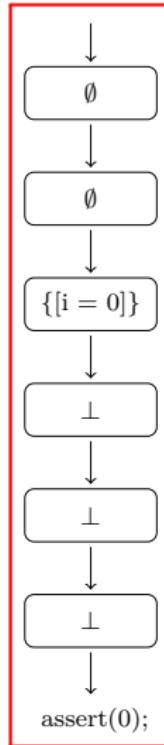
1 #include <assert.h>
2 extern int f(int x);
3 int main() {
4     int b = 0;
5     int i = 0;
6     would unroll loop! i = 0;
7     while(1) {
8         if(i > 9) {
9             break;
10        }
11        f(i++);
12    }
13
14    if(b != 0) {
15        if(i != 10) {
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```

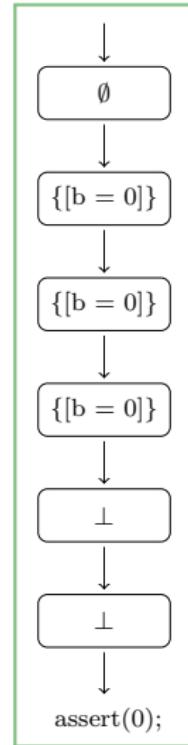


verification task

error path



bad sequence



good sequence

# Standard Interpolation Engines are Black Boxes

- Typically, interpolation engines use internal heuristics
- Resolution process cannot be controlled from outside

## Problem

We are stuck to the result of the interpolation engine,  
be it good or bad

## Proposition

Remodel interpolation problem  
such that different interpolant sequences can be extracted

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# Extraction of Infeasible Sliced Prefixes — Algorithm

FORTE'15, Beyer, Löwe, Wendler

---

**Algorithm 2:** ExtractInfeasibleSlicedPrefixes( $\sigma$ )
 

---

**Input** : an infeasible path  $\sigma = \langle (op_1, l_1), \dots, (op_m, l_m) \rangle$

**Output** : a non-empty set  $\Sigma = \{\sigma_1, \dots, \sigma_n\}$  of infeasible sliced prefixes of  $\sigma$

**Variables:** a path  $\sigma_f$  that is always feasible

$\Sigma := \emptyset$

$\sigma_f := \langle \rangle$

**foreach**  $(op, l) \in \sigma$  **do**

**if**  $\widehat{SP}_{\sigma_f \wedge (op, l)}(\top) = \perp$  **then**

*// add  $\sigma_f \wedge (op, l)$  to set  $\Sigma$  of infeasible sliced prefixes*

$\Sigma := \Sigma \cup \{\sigma_f \wedge (op, l)\}$

*// append no-op*

$\sigma_f := \sigma_f \wedge ([\text{true}], l)$

**else**

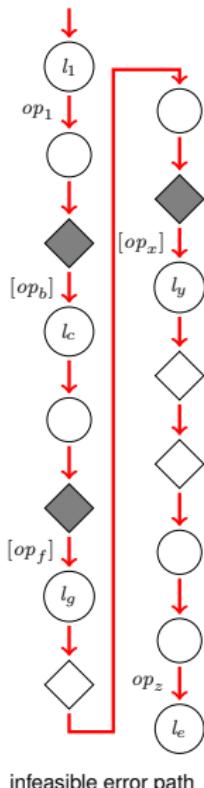
*// append original pair*

$\sigma_f := \sigma_f \wedge (op, l)$

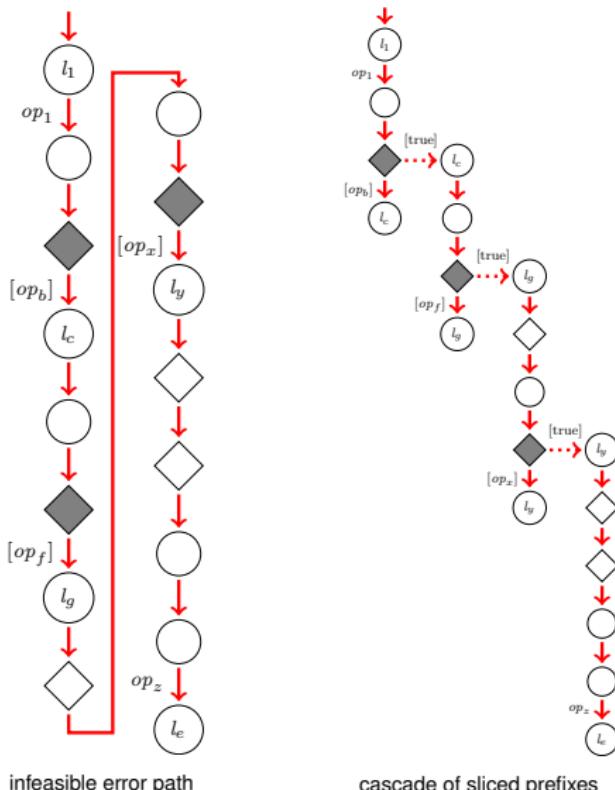
**return**  $\Sigma$

---

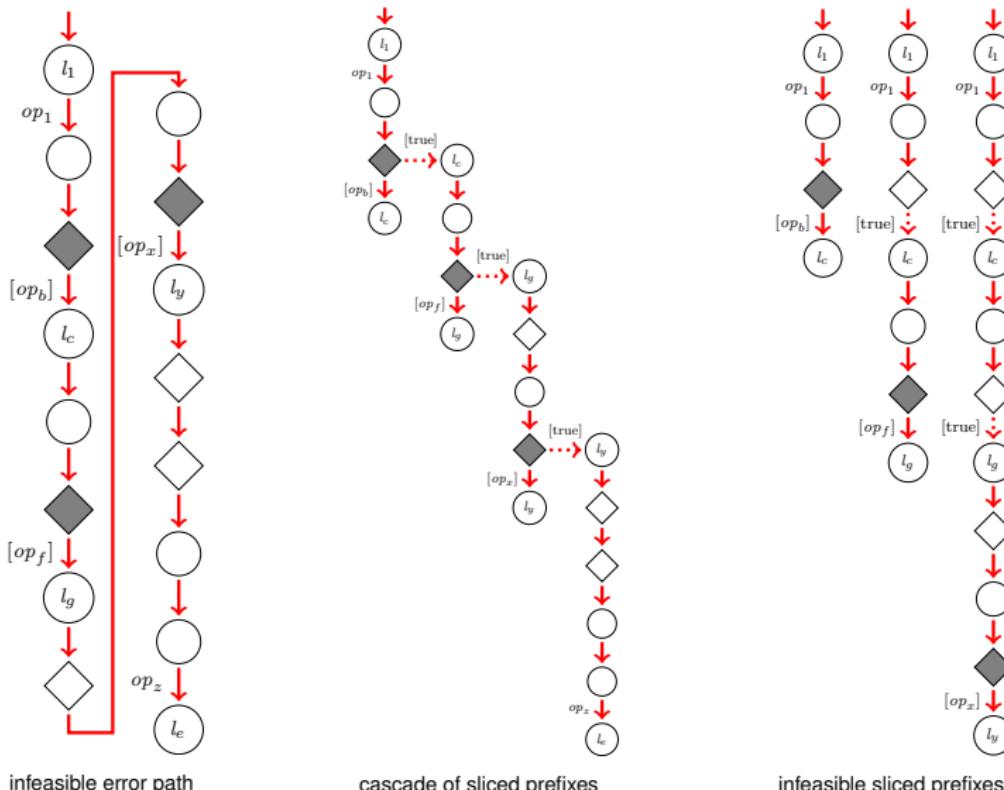
# Extraction of Infeasible Sliced Prefixes — Example



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# Infeasible Sliced Prefixes

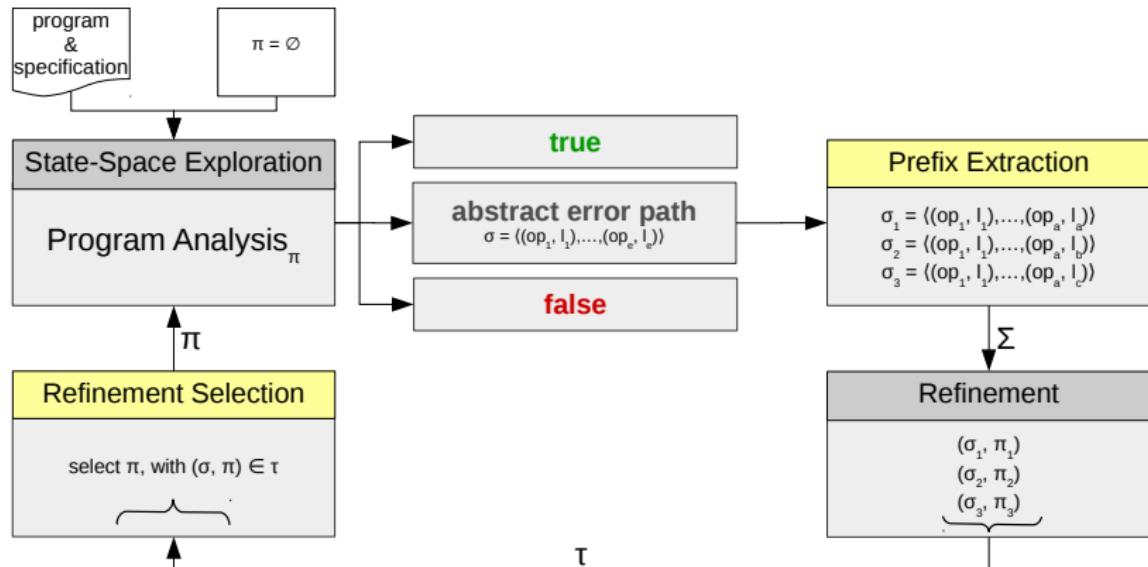
## Theorem

*Any infeasible sliced prefix  $\varphi$ ,  
that is extracted from an infeasible error path  $\sigma$ ,  
can be used for interpolation to exclude the original error path  $\sigma$*

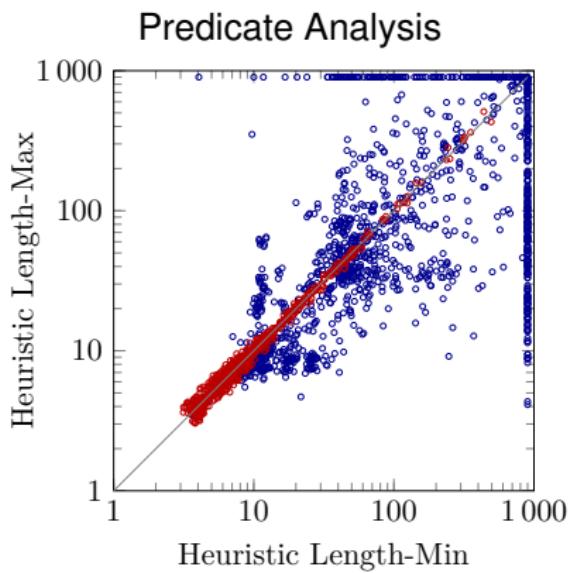
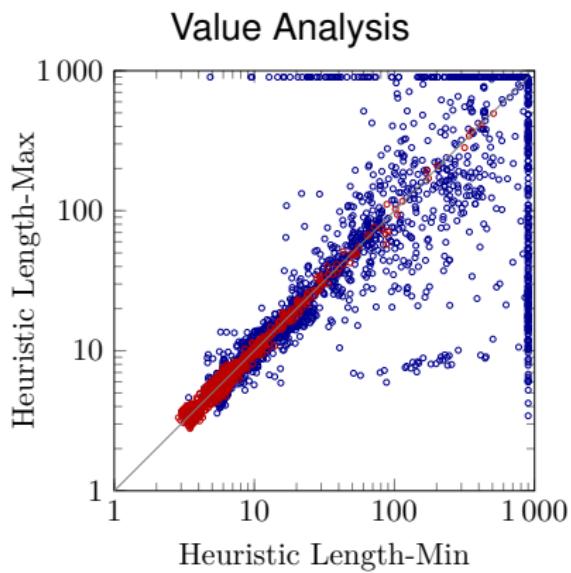
## Proposition

Use different infeasible sliced prefixes to get different interpolants

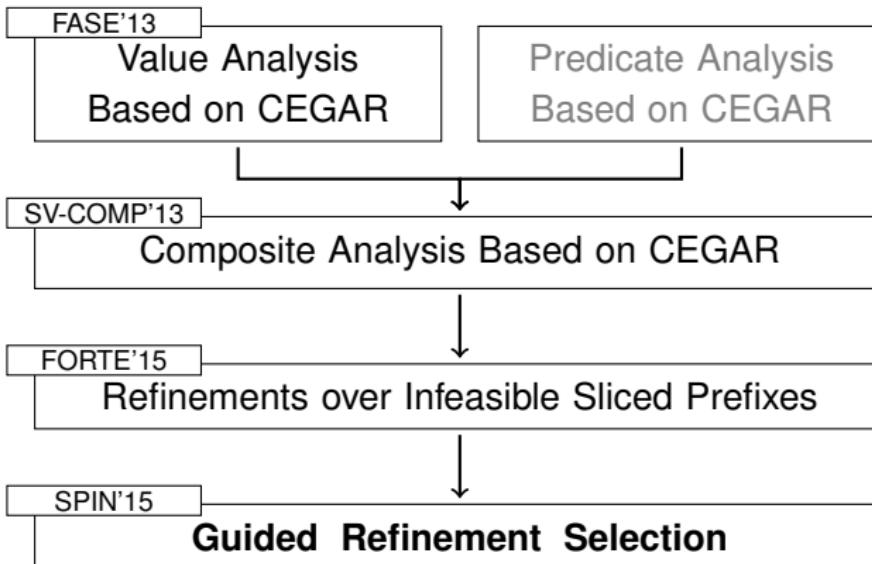
# CEGAR using Infeasible Sliced Prefixes



# Infeasible Sliced Prefixes — Impact



# Outline

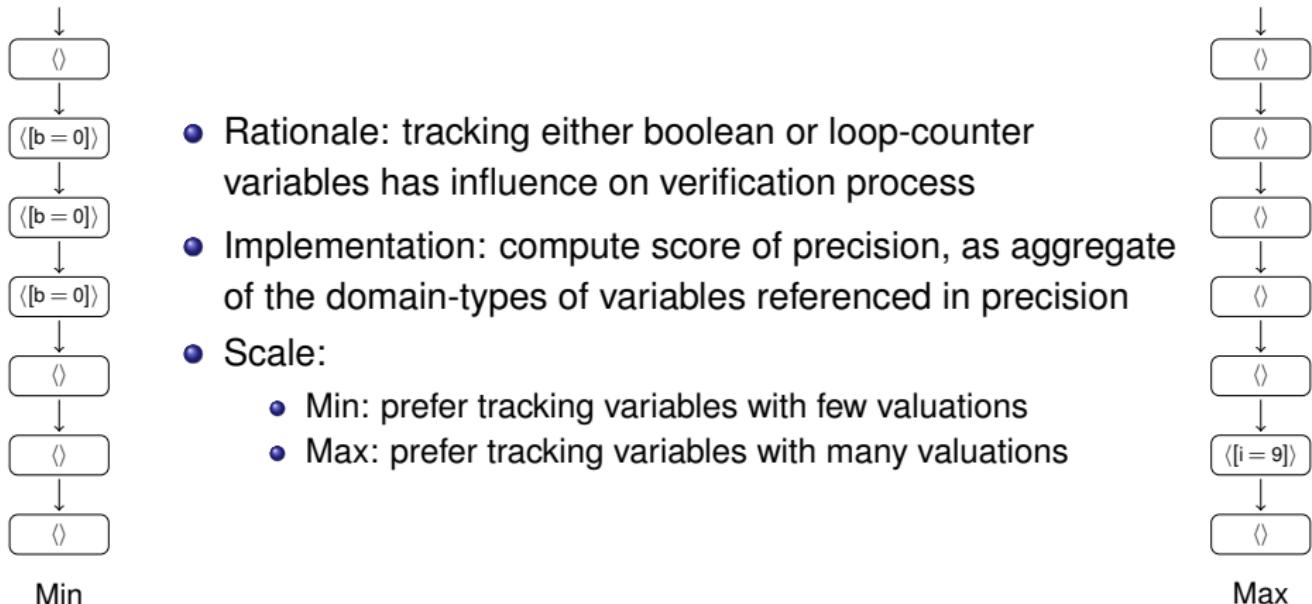


# Refinement Selection

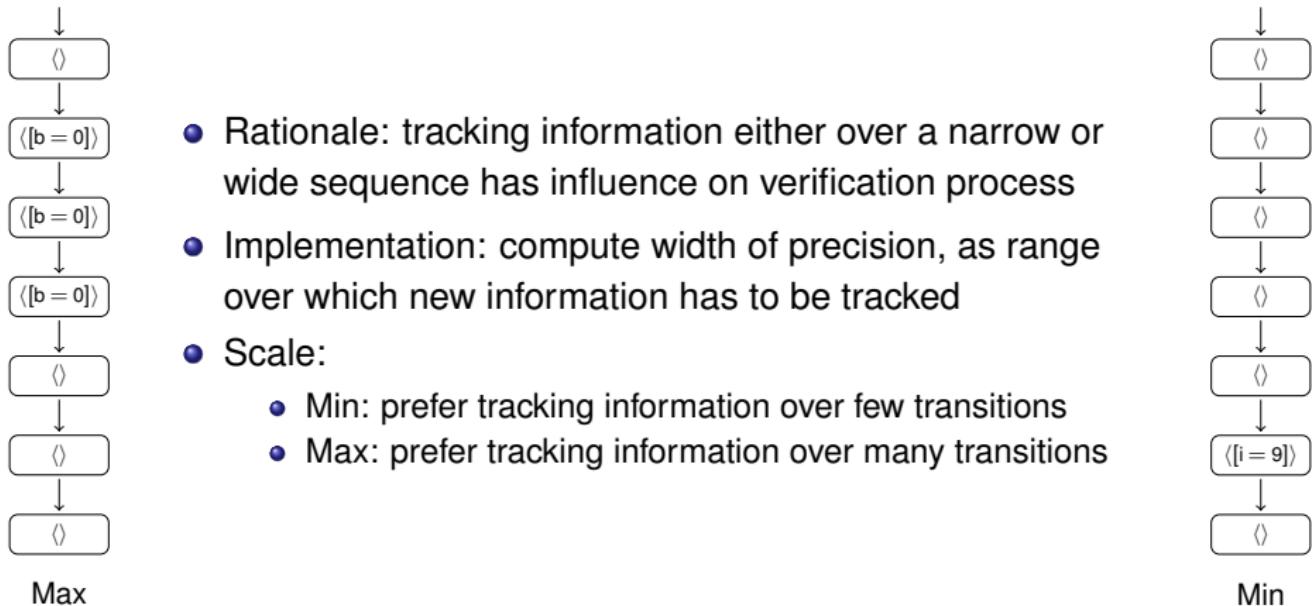
## Proposition

Try to select a favorable refinement  
from the set of available refinement choices

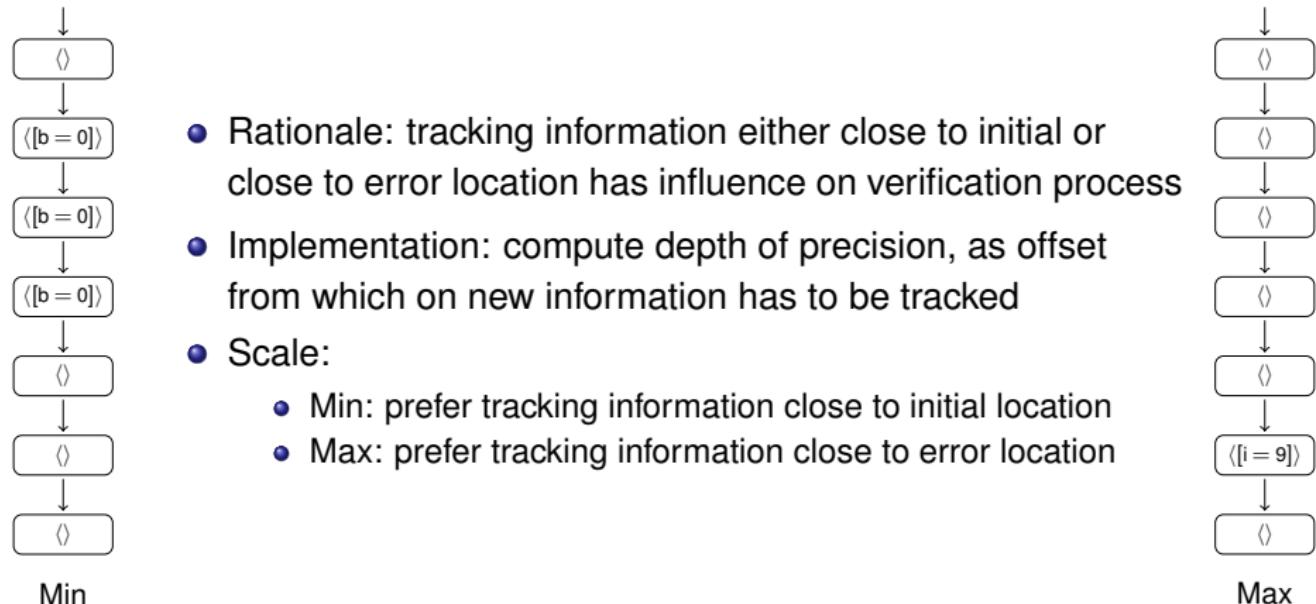
# Refinement Selection by Domain-Type Score



# Refinement Selection by Width of Precision



# Refinement Selection by Depth of Pivot Location



- Rationale: tracking information either close to initial or close to error location has influence on verification process
- Implementation: compute depth of precision, as offset from which on new information has to be tracked
- Scale:
  - Min: prefer tracking information close to initial location
  - Max: prefer tracking information close to error location

Min

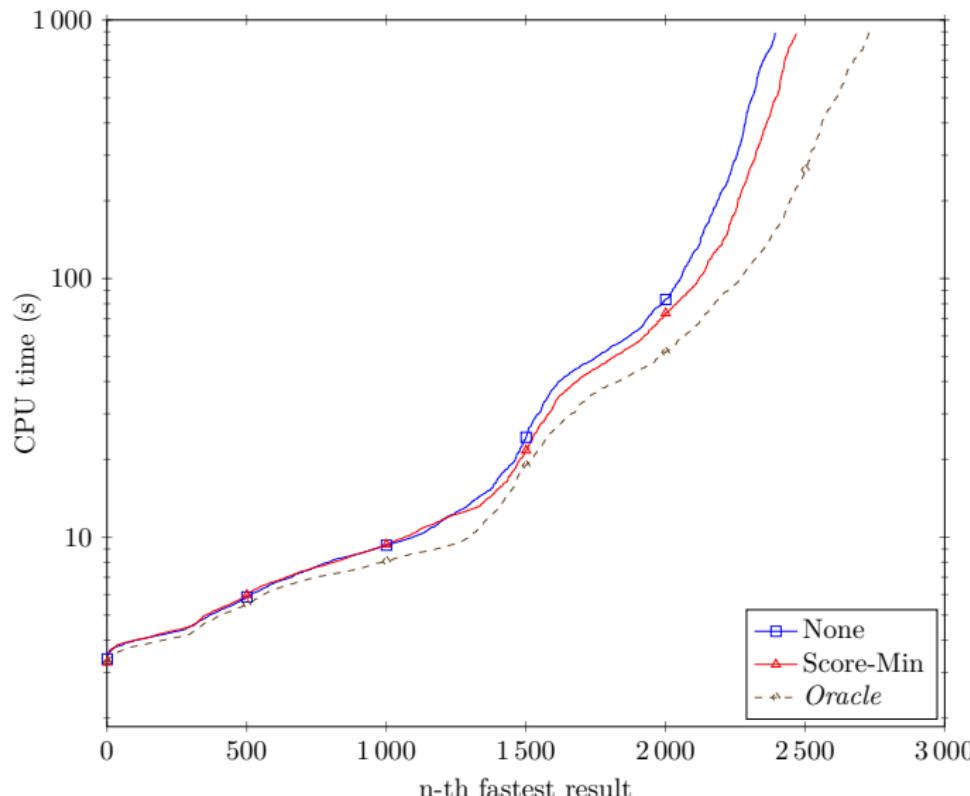
Max

# Refinement Selection — More Effective

		CONTROLFLOW	DD64	ECA	PRODUCTLINES	SEQUENTIAL	OVERALL
total		48	2 120	1 140	597	62	4 283
Length	Min	<b>43</b>	1 471	177	356	27	2 328
	Max	31	1 564	194	332	20	2 385
Width	Min	37	1 464	<b>280</b>	346	24	2 406
	Max	36	1 545	174	312	27	2 337
Depth	Min	34	1 526	152	<b>358</b>	26	2 342
	Max	36	1 468	206	329	24	2 317
Score	Min	40	<b>1592</b>	217	339	<b>29</b>	<b>2470</b>
	Max	23	1 459	191	302	20	2 238
None		42	1 525	218	324	28	2 393
<i>Optimal</i>		43	1 592	280	358	29	2 561
	<i>Oracle</i>	43	1 650	337	412	31	2 732

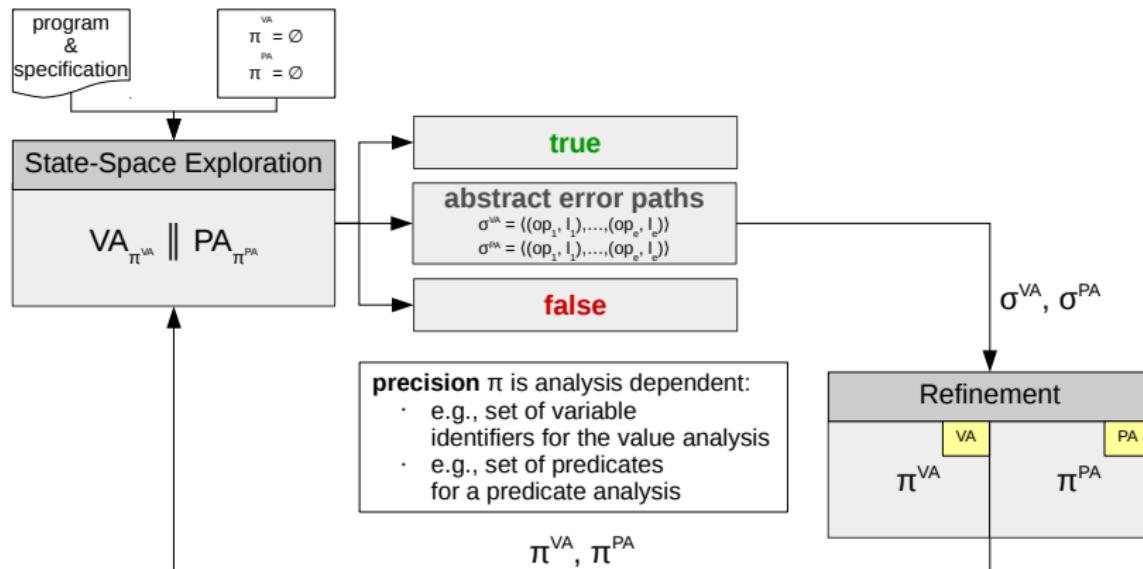
Number of solved verification tasks for the predicate analysis  
with refinement selection using different heuristics

# Refinement Selection — More Efficient



# Bringing Refinement Selection to the Next Level

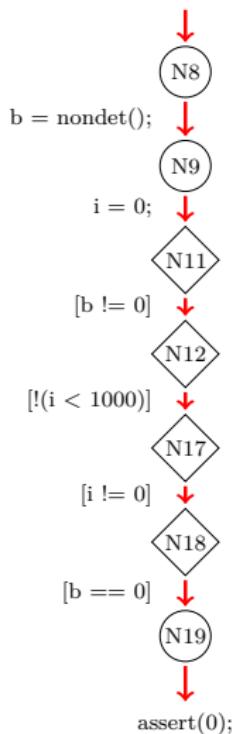
SV-COMP'13, Löwe



# Inter-Analysis Refinement Selection

```

1 #include <assert.h>
2
3 extern int nondet();
4 extern int f(int x);
5
6 int main() {
7
8     int b = nondet();
9     int i = 0;
10
11    if (b != 0) {
12        while (i < 1000) {
13            f(i++);
14        }
15    }
16
17    if (i != 0) {
18        if (b == 0) {
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20        }
21    }
22 }
```



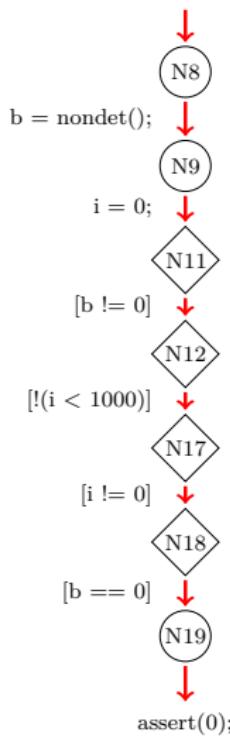
verification task

error path

# Inter-Analysis Refinement Selection

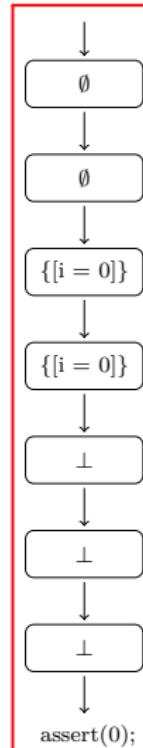
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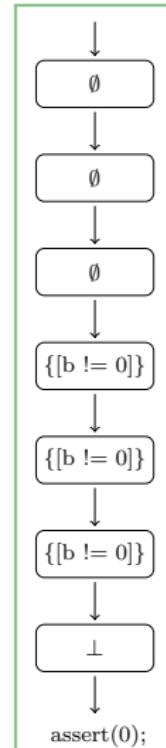


verification task

error path

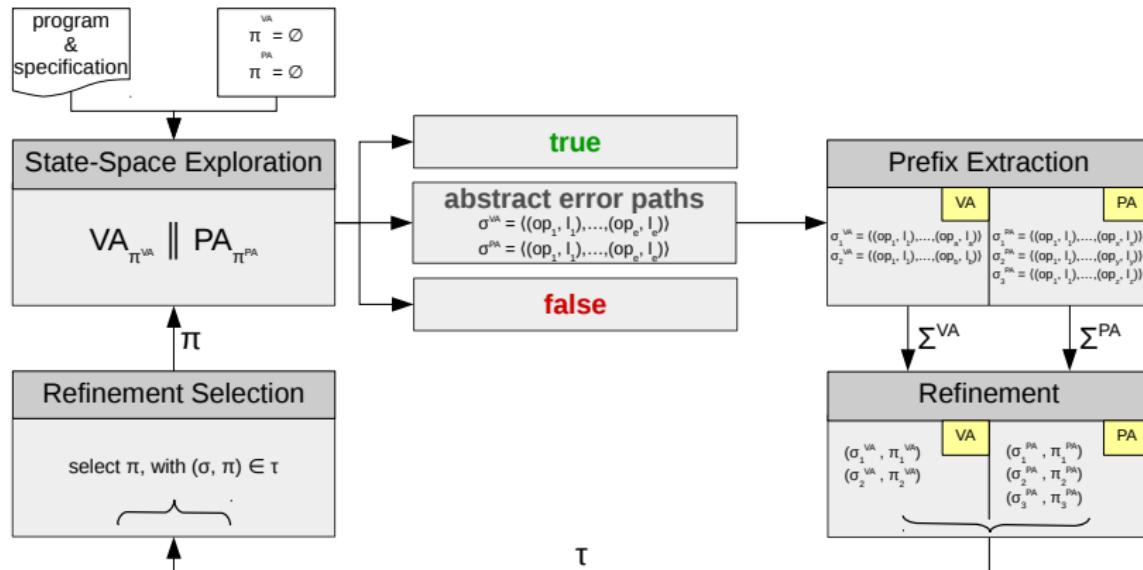


bad sequence



good sequence

# CEGAR with Inter-Analysis Refinement Selection



# Inter-Analysis Refinement Selection — Most Effective

	BITVECTORS	CONTROL FLOW	DD64	ECA	FLOATS	LOOPS	PRODUCTLINES	SEQUENTIAL	SIMPLE	OVERALL
total	48	48	2 120	1 140	81	141	597	62	46	4 283
PA	43	42	1 525	218	73	97	321	28	43	2 390
VA-PA-Composition	43	<b>45</b>	1 561	<b>484</b>	73	89	<b>390</b>	<b>38</b>	<b>46</b>	2 769
VA-PA-Composition-RefSel	<b>44</b>	<b>45</b>	<b>1652</b>	472	<b>74</b>	<b>98</b>	373	32	45	<b>2835</b>

SV-COMP'16, Löwe

Verifier based on inter-analysis refinement selection wins  
gold medal in category “DeviceDrivers64”

# Inter-Analysis Refinement Selection — Most Effective

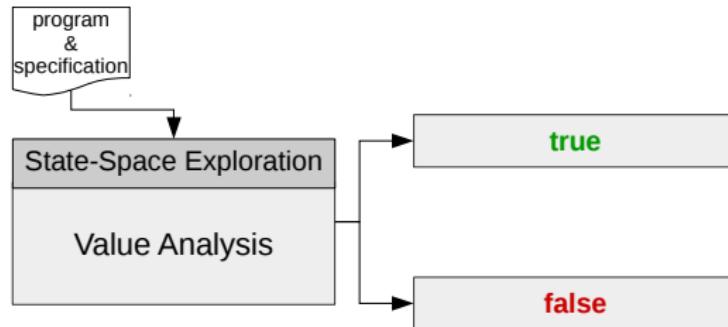
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SV-COMP'16, Löwe

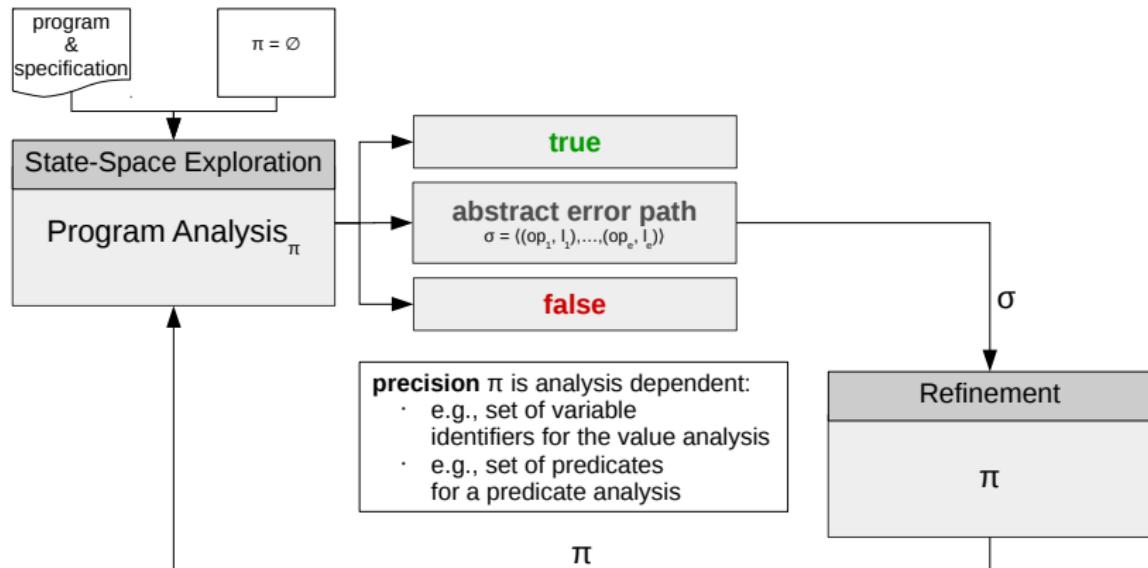
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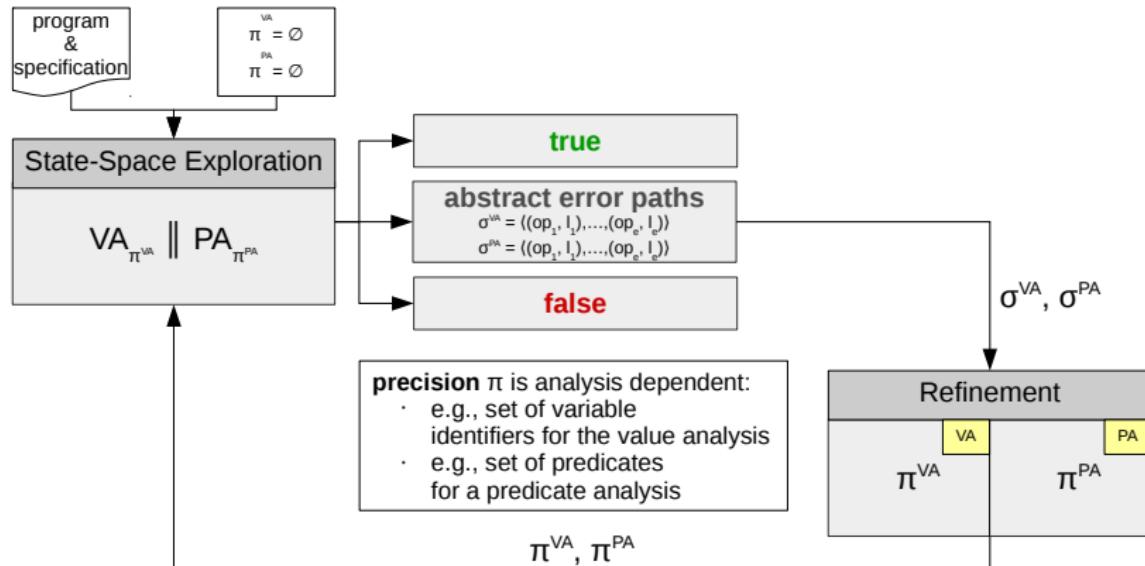
# Summary: Value Analysis Plain and Simple



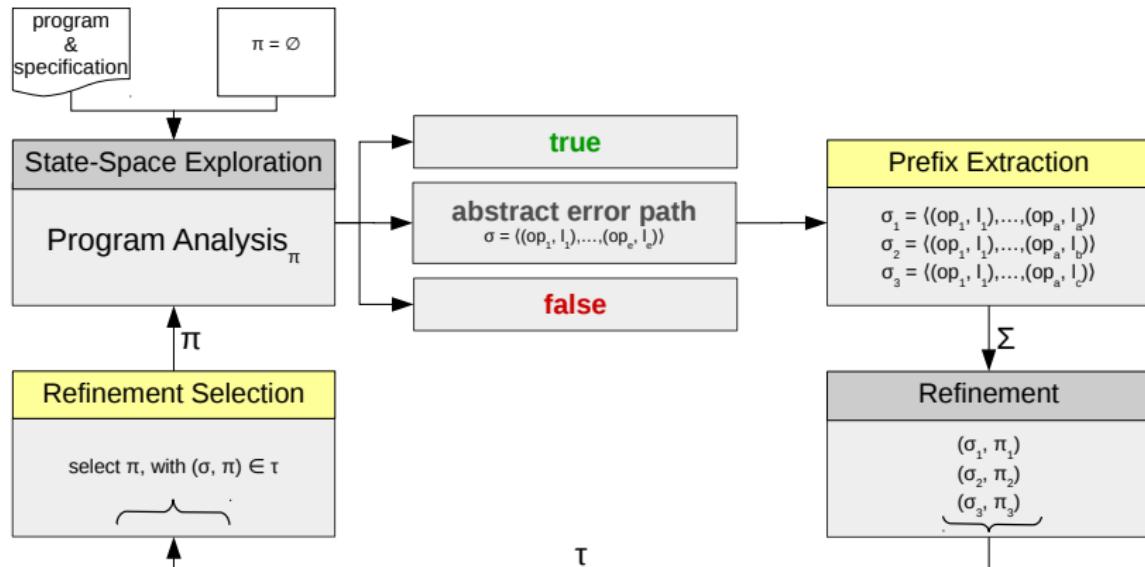
# Summary: Value Analysis Based on CEGAR



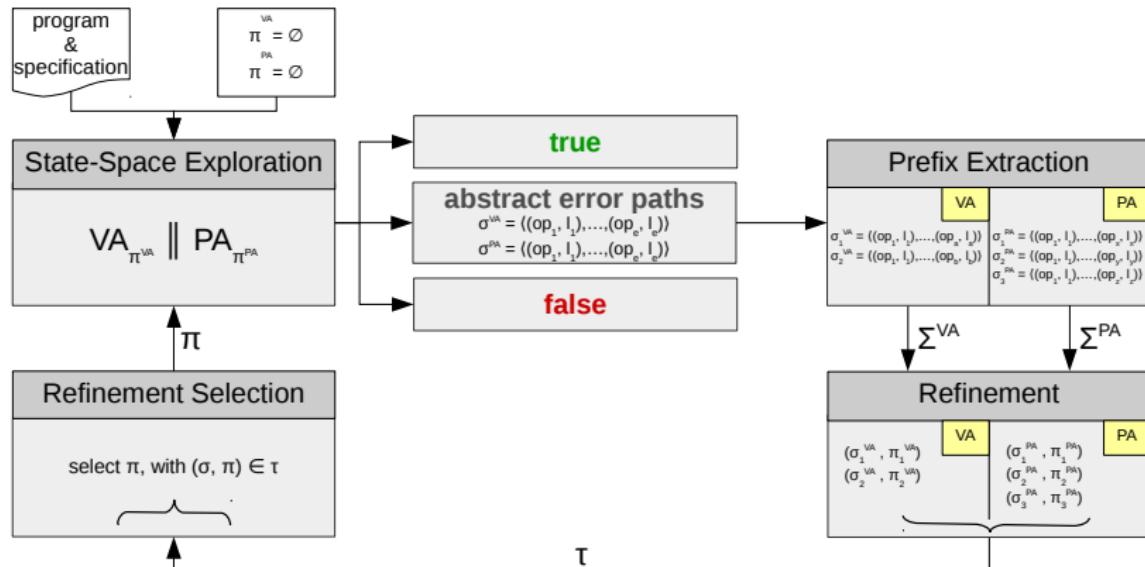
# Summary: Composite Analysis Based on CEGAR



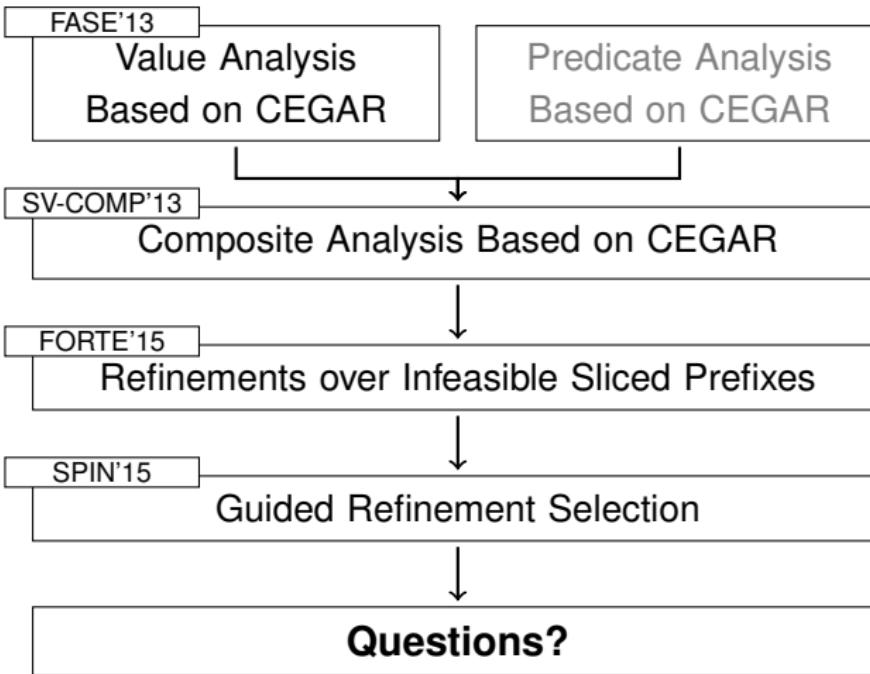
# Summary: CEGAR with Guided Refinement Selection



# Summary: CEGAR with Inter-Analysis Refinement Selection



# The End



# Achievements

- Value Analysis Based on CEGAR  
(FASE'13)
- CPAchecker-Explicit  
(SV-COMP'13)
- Infeasible Sliced Prefixes  
(FORTE'15)
- Refinement Selection  
(SPIN'15)
- CPA-RefSel  
(SV-COMP'16)
- Precision Reuse  
(FSE'13)
- BenchExec  
(SPIN'15)
- Wins & Medals at SV-COMP  
(SV-COMP'12 – '16)
- Gödel-Medal  
(VSL'14)
- Linux Driver Verification  
(2012 — 2016)

# Craig Interpolation

JSL'57, Craig

## Theorem

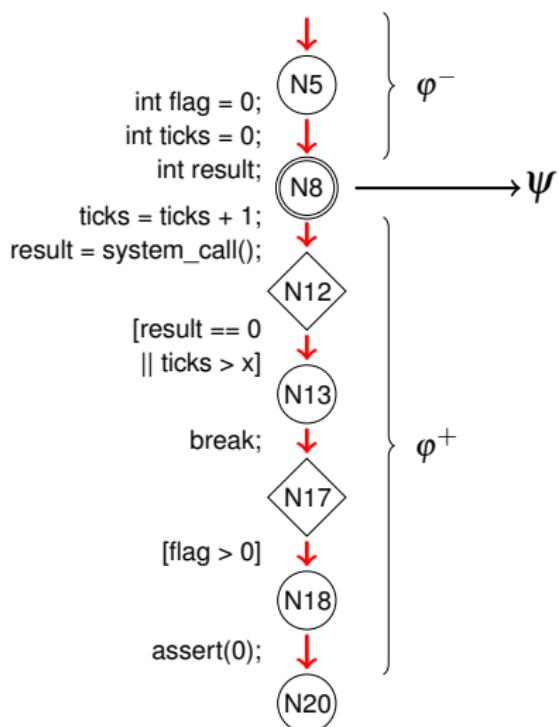
For a pair of formulas  $\varphi^-$  and  $\varphi^+$  such that  $\varphi^- \wedge \varphi^+$  is unsatisfiable, a Craig interpolant  $\psi$  is a formula that fulfills the following three requirements:

- ① the implication  $\varphi^- \implies \psi$  holds,
- ② the conjunction  $\psi \wedge \varphi^+$  is unsatisfiable, and
- ③  $\psi$  only contains symbols that occur in both  $\varphi^-$  and  $\varphi^+$

Such an interpolant is guaranteed to exist for many useful theories

# Interpolation to Obtain Abstractions from Proofs

POPL'04, Henzinger, Jhala, Majumdar, McMillan

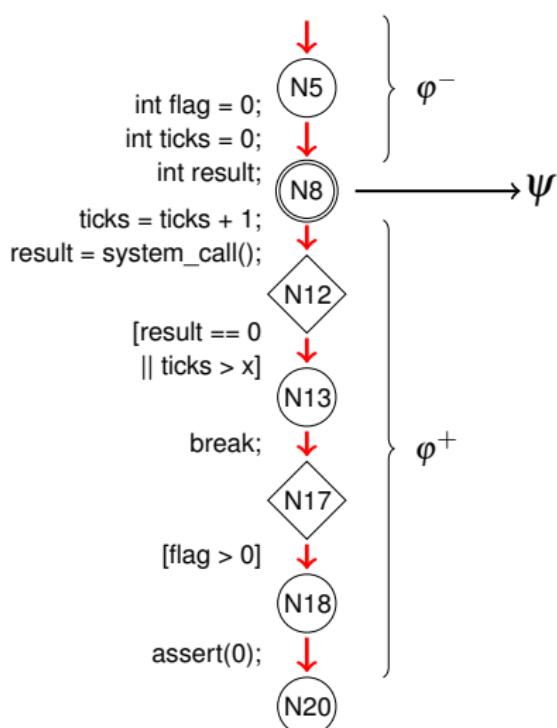


The interpolant  $\psi$  at N8 could be:

- $[\text{flag} = 0]$
- $[\text{flag} \leq 0]$
- $[\text{flag} < 1]$
- $[\text{flag} = 0 \wedge \text{ticks} = 0]$
- $[\text{flag} \leq 0 \wedge \text{ticks} = 0]$
- $[\text{flag} < 1 \wedge \text{ticks} = 0]$
- ...

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POPL'04, Henzinger, Jhala, Majumdar, McMillan



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- $[\text{flag} < 1 \wedge \text{ticks} = 0]$
- ...

# Value Interpolation does not Compute a Value Refinement

## Problem

The Value Interpolation does not return a refined precision

## Proposition

Use the Value Interpolation to compute a Value Refinement

# Value Interpolation does not Compute a Value Refinement

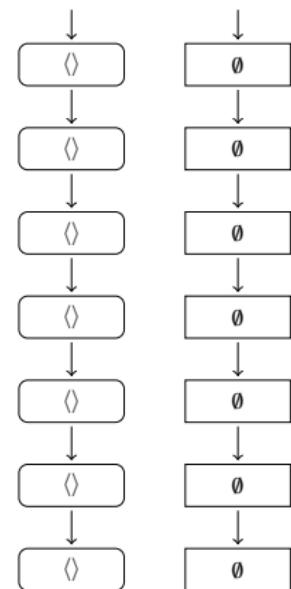
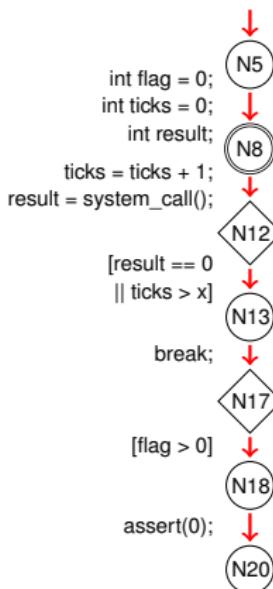
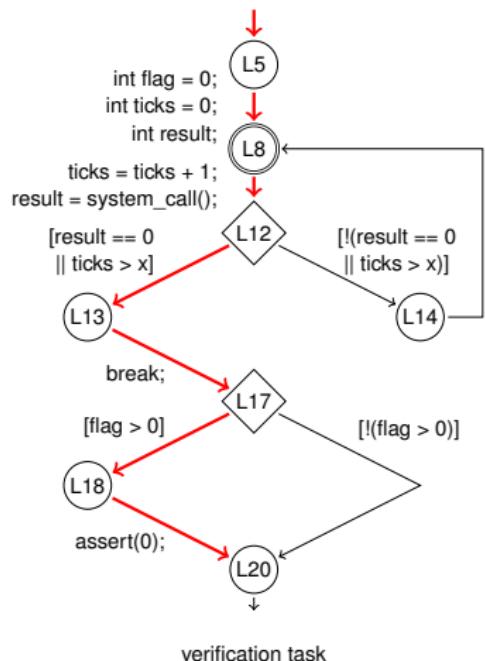
## Problem

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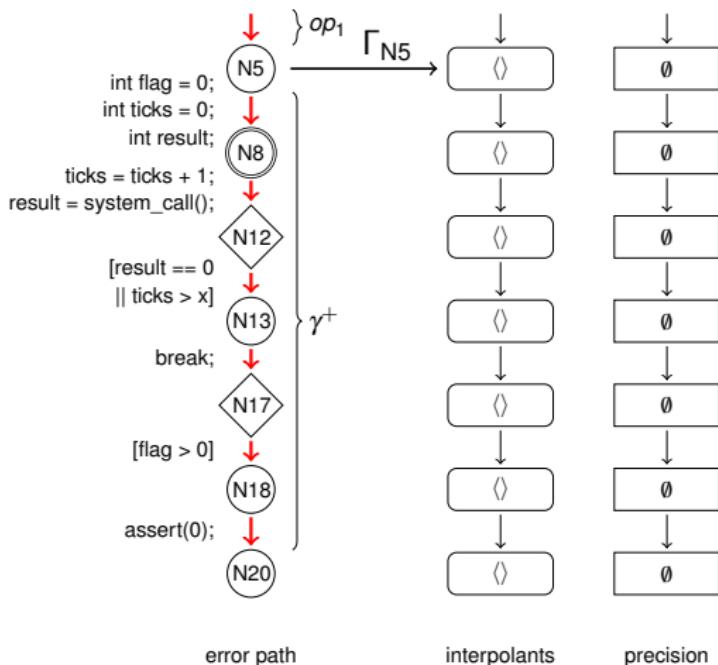
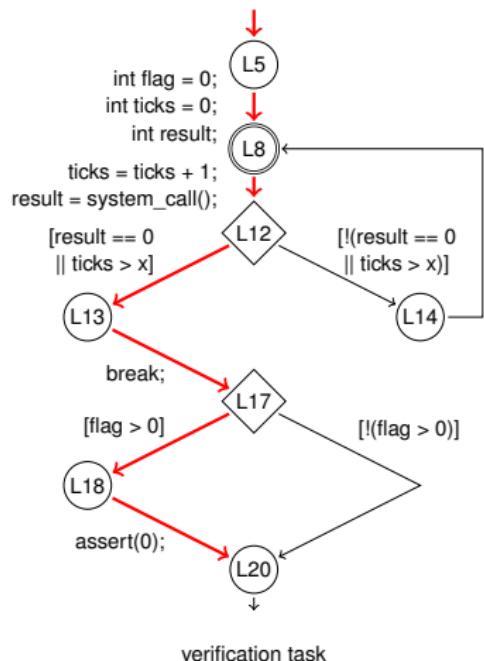
## Proposition

Use the Value Interpolation to compute a Value Refinement

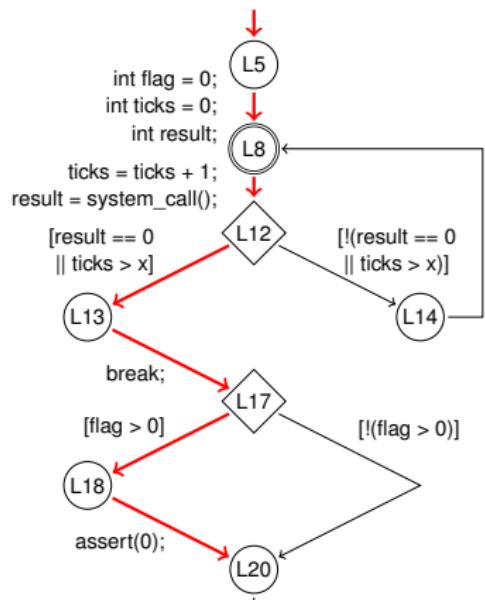
# Value Refinement



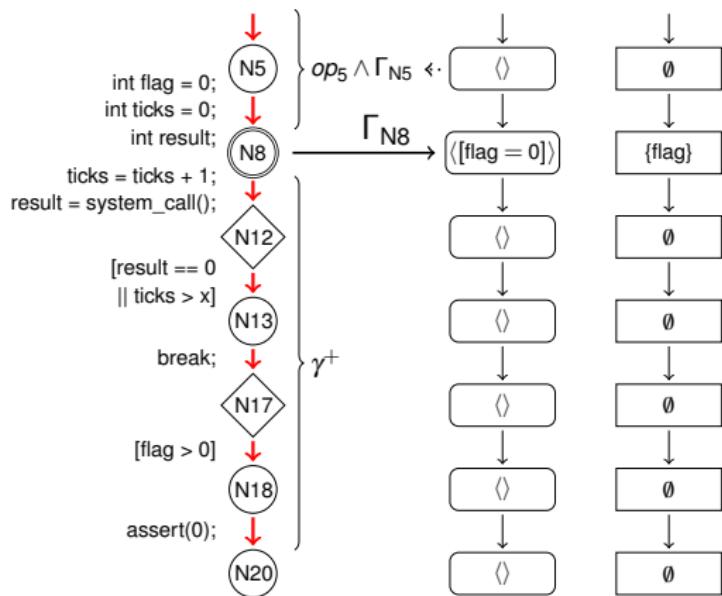
# Value Refinement at Node 5



# Value Refinement at Node 8



verification task

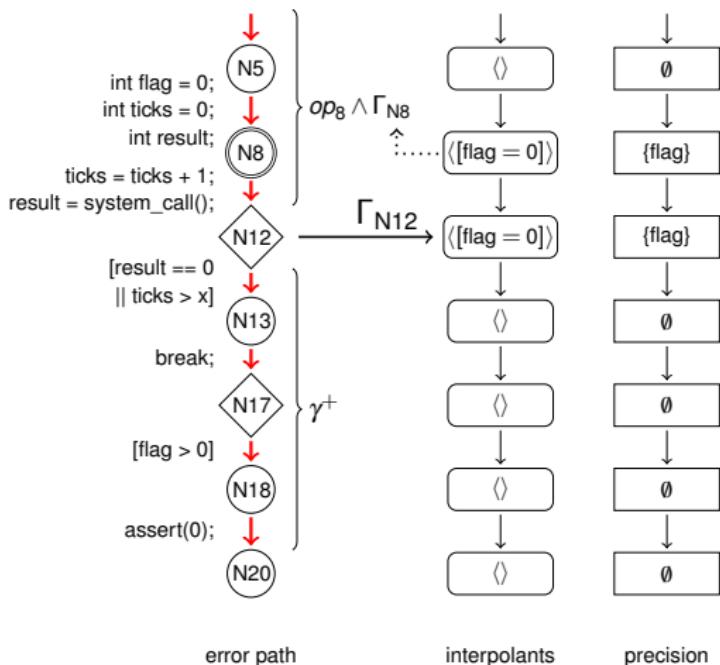
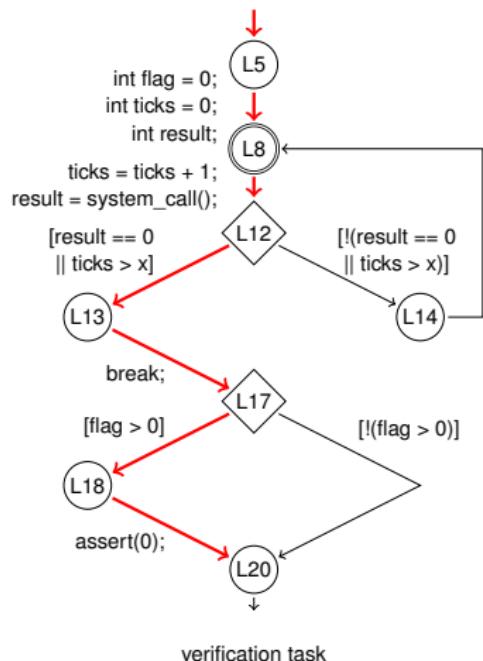


error path

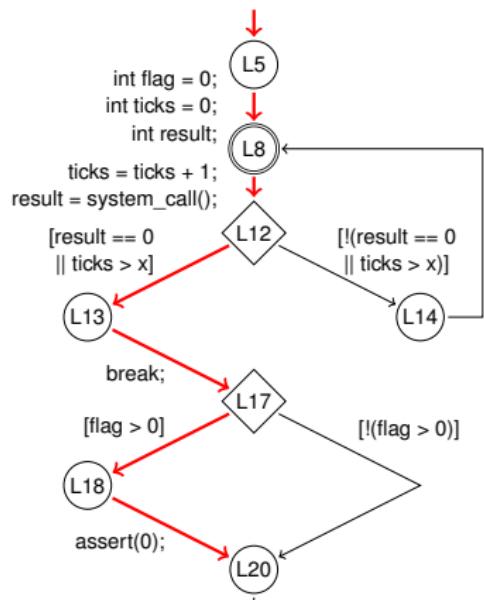
interpolants

precision

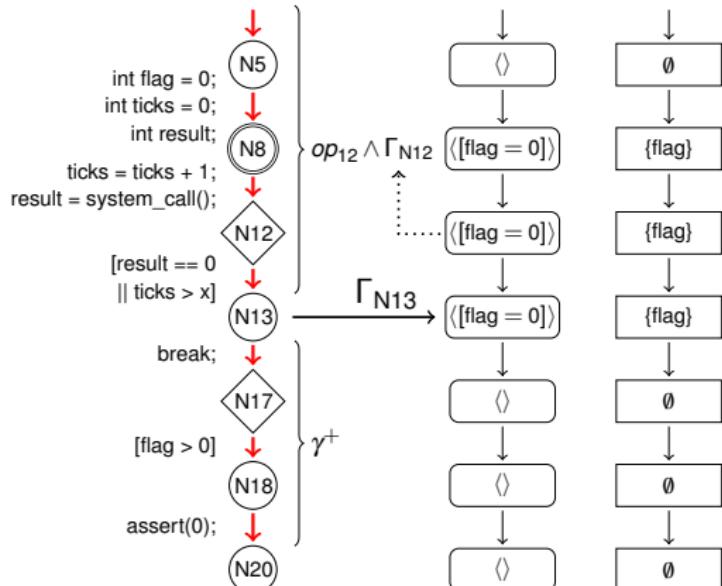
# Value Refinement at Node 12



# Value Refinement at Node 13



verification task

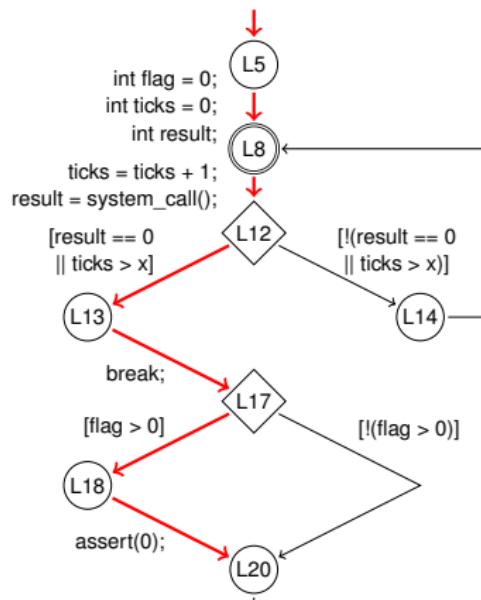


error path

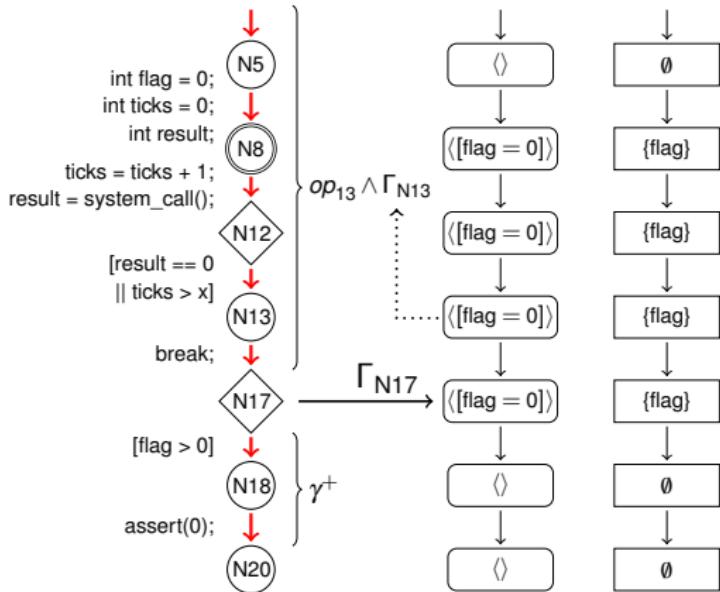
interpolants

precision

# Value Refinement at Node 17



verification task

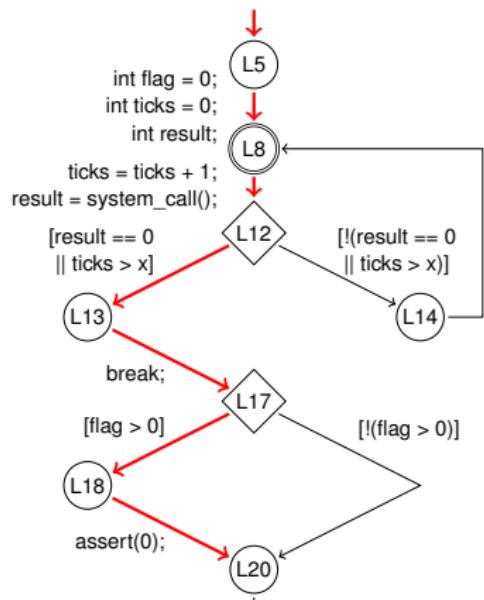


error path

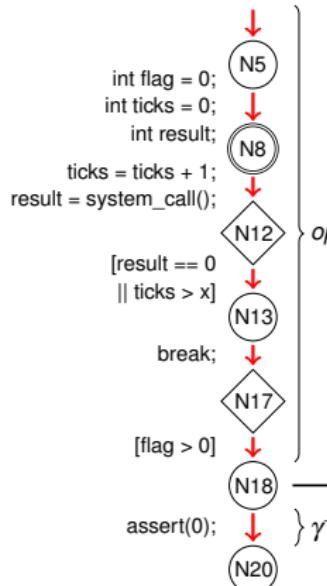
interpolants

precision

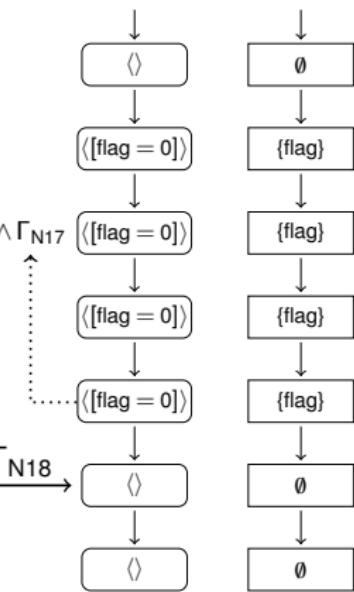
# Value Refinement at Node 18



verification task



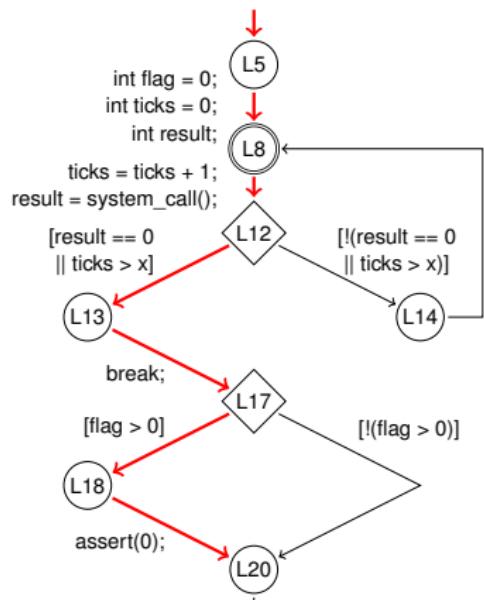
error path



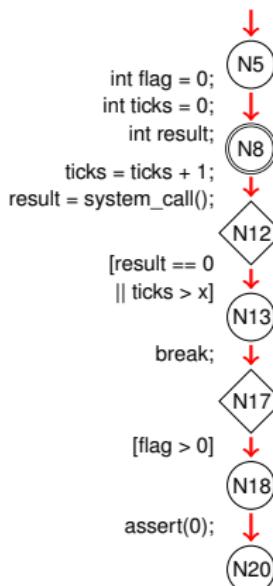
interpolants

precision

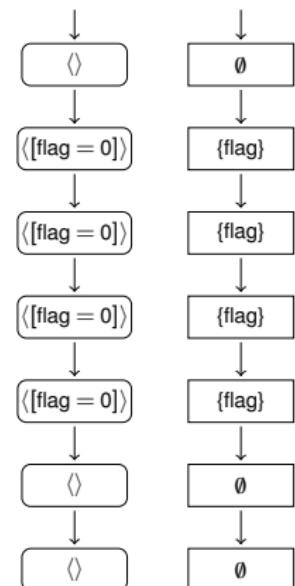
# Value Refinement Completed



verification task



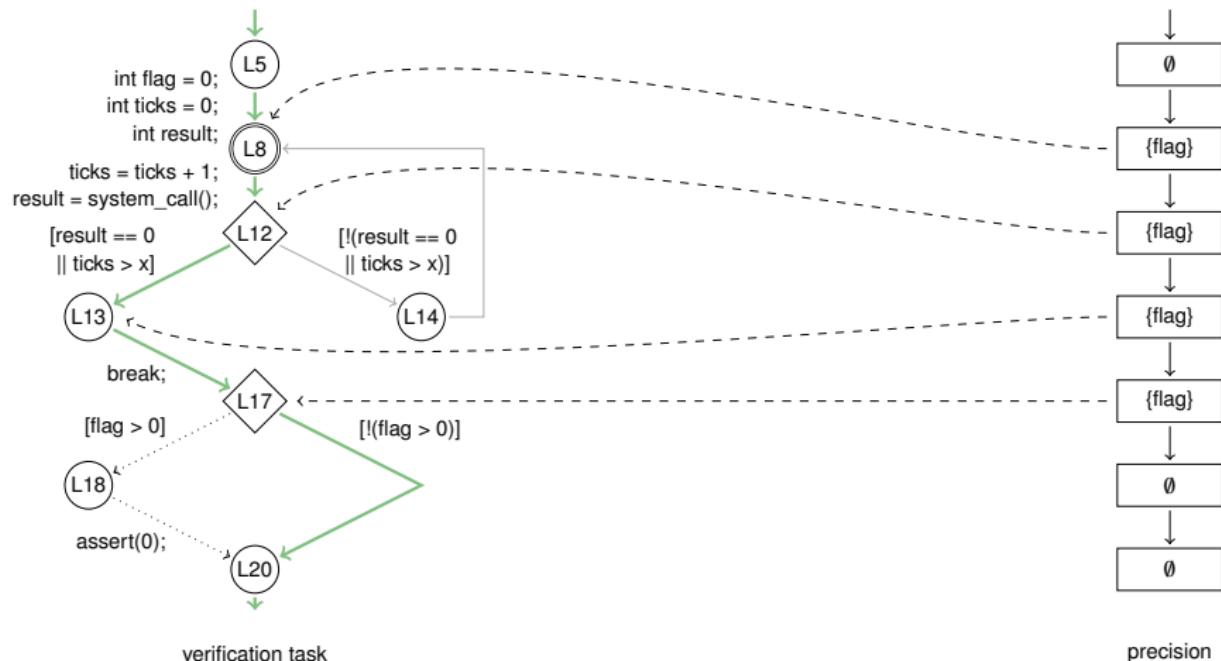
error path



interpolants

precision

# Value Refinement Avoids Counterexample and Loop



# Refinement Selection by Other Heuristics

- Length of infeasible sliced path
- Combinations of heuristics
- Domain knowledge

# Refinement Selection for Value Analysis — More Effective

		DD64	ECA	PRODUCTLINES	SEQUENTIAL	OVERALL
total		2 120	1 140	597	62	4 283
Length	Min	1 646	489	449	37	2 951
	Max	<b>1764</b>	507	361	31	2 995
Width	Min	1 661	508	469	39	3 007
	Max	1 746	481	357	35	2 950
Depth	Min	1 724	530	388	<b>42</b>	3 014
	Max	1 665	519	448	38	3 002
Score	Min	<b>1764</b>	534	414	37	3 081
	Max	1 665	394	364	29	2 784
Width & Score		1 665	510	<b>472</b>	39	3 016
None		1 661	<b>575</b>	453	<b>42</b>	3 062
<i>Optimal</i>		1 764	575	472	42	3 186
	<i>Oracle</i>	1 809	631	502	47	3 322

# Refinement Selection for Value Analysis — More Efficient

