

# Explicit-State Model Checking Based on CEGAR and Interpolation

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# State of the art: SV-COMP'12 participants

## Predicate Abstraction

- BLAST
- CPAchecker ABE
- CPAchecker ABM
- QARMC-HSF
- SATABS
- Wolverine

## Bounded Model Checking

- ESBMC
- FShell
- LLBMC

*All these rely on expensive calls to underlying decision procedure*

# ... Dramatization ...

mem_slave_tlm.1.cil.c	safe	120	out of memory	270	out of memory	270	timeout	910	safe
mem_slave_tlm.2.cil.c	safe	560	segmentation fault	210	out of memory	410	timeout	910	safe
mem_slave_tlm.3.cil.c	timeout	910	out of memory	260	timeout	900	timeout	910	safe
mem_slave_tlm.4.cil.c	unknown	220	segmentation fault	390	timeout	900	timeout	910	safe
mem_slave_tlm.5.cil.c	unknown	220	out of memory	300	timeout	900	timeout	910	safe
pipeline.cil.c	timeout	910	safe	16	timeout	900	timeout	900	safe
token_ring.01.cil.c	safe	3.0	safe	3.9	safe	6.9	timeout	910	unsafe
token_ring.02.cil.c	safe	93	safe	7.1	safe	49	timeout	910	unsafe
token_ring.03.cil.c	safe	580	safe	33	timeout	900	timeout	900	unsafe
token_ring.04.cil.c	timeout	910	safe	140	timeout	900	timeout	900	unsafe
token_ring.05.cil.c	timeout	910	out of memory	300	out of memory	550	timeout	900	unsafe
token_ring.06.cil.c	timeout	910	out of memory	380	segmentation fault	650	timeout	910	unsafe
token_ring.07.cil.c	timeout	910	timeout	900	timeout	900	timeout	910	unsafe
token_ring.08.cil.c	timeout	910	timeout	900	timeout	900	timeout	910	unsafe
token_ring.09.cil.c	timeout	910	timeout	900	timeout	900	timeout	900	timeout
token_ring.10.cil.c	timeout	910	timeout	900	timeout	900	timeout	900	timeout
token_ring.11.cil.c	timeout	910	out of memory	880	timeout	900	timeout	900	timeout

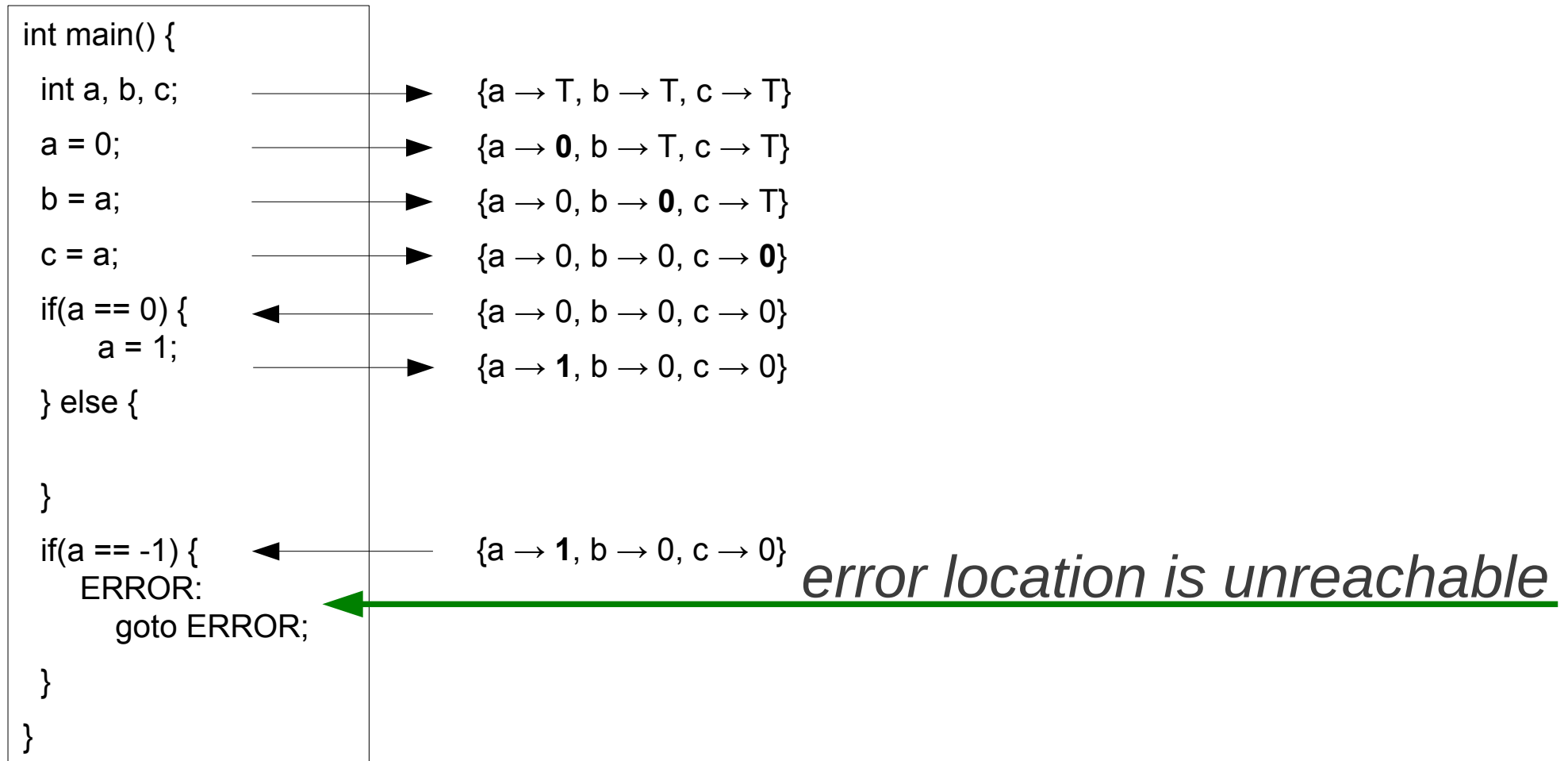
# How to circumvent?

- Use a less expensive domain
  - Signs (-, isZero, +)
  - Explicit values ( $\{ a \rightarrow 1, b \rightarrow -5, c \rightarrow T \}$ )
- More efficient successor computation
- Less precise state representation



state-space explosion still a major issue

# Explicit-Value Model Checking



# The Good

Tool	CPAchecker 1.1-svn				
Test	explicitAnalysis-cbmc				
test/programs/benchmarks/	status	cputime	walltime	total	cpa time
ntdrivers/cdaudio.BUG.i.cil.c	unsafe	6.54	12.43	11.231s	0.083s
ntdrivers/diskperf.BUG.i.cil.c	unsafe	4.69	10.52	8.962s	0.102s
ntdrivers/floppy.BUG.i.cil.c	unsafe	46.73	51.75	50.633s	0.106s
ntdrivers/kbfiltr.BUG.i.cil.c	unsafe	136.67	140.90	139.515s	0.226s
ntdrivers/parport.BUG.i.cil.c	unsafe	7.06	18.60	16.810s	0.134s
ntdrivers/cdaudio.i.cil.c	safe	8.26	11.31	9.725s	0.586s
ssh/s3_srvr.blast.01.BUG.i.cil.c	unsafe	3.07	2.77	1.778s	0.079s
ssh/s3_srvr.blast.02.BUG.i.cil.c	unsafe	2.93	2.84	1.929s	0.071s
ssh/s3_srvr.blast.03.BUG.i.cil.c	unsafe	3.00	3.56	1.836s	0.073s
ssh/s3_srvr.blast.04.BUG.i.cil.c	unsafe	3.07	2.78	1.712s	0.071s
ssh/s3_srvr.blast.01.i.cil.c	safe	61.66	58.75	49.367s	47.898s
ssh/s3_srvr.blast.02.i.cil.c	safe	58.18	54.96	44.955s	43.701s
ssh/s3_srvr.blast.06.i.cil.c	safe	821.48	802.42	763.905s	762.368s
ssh/s3_srvr.blast.07.i.cil.c	safe	589.96	587.35	547.721s	545.769s

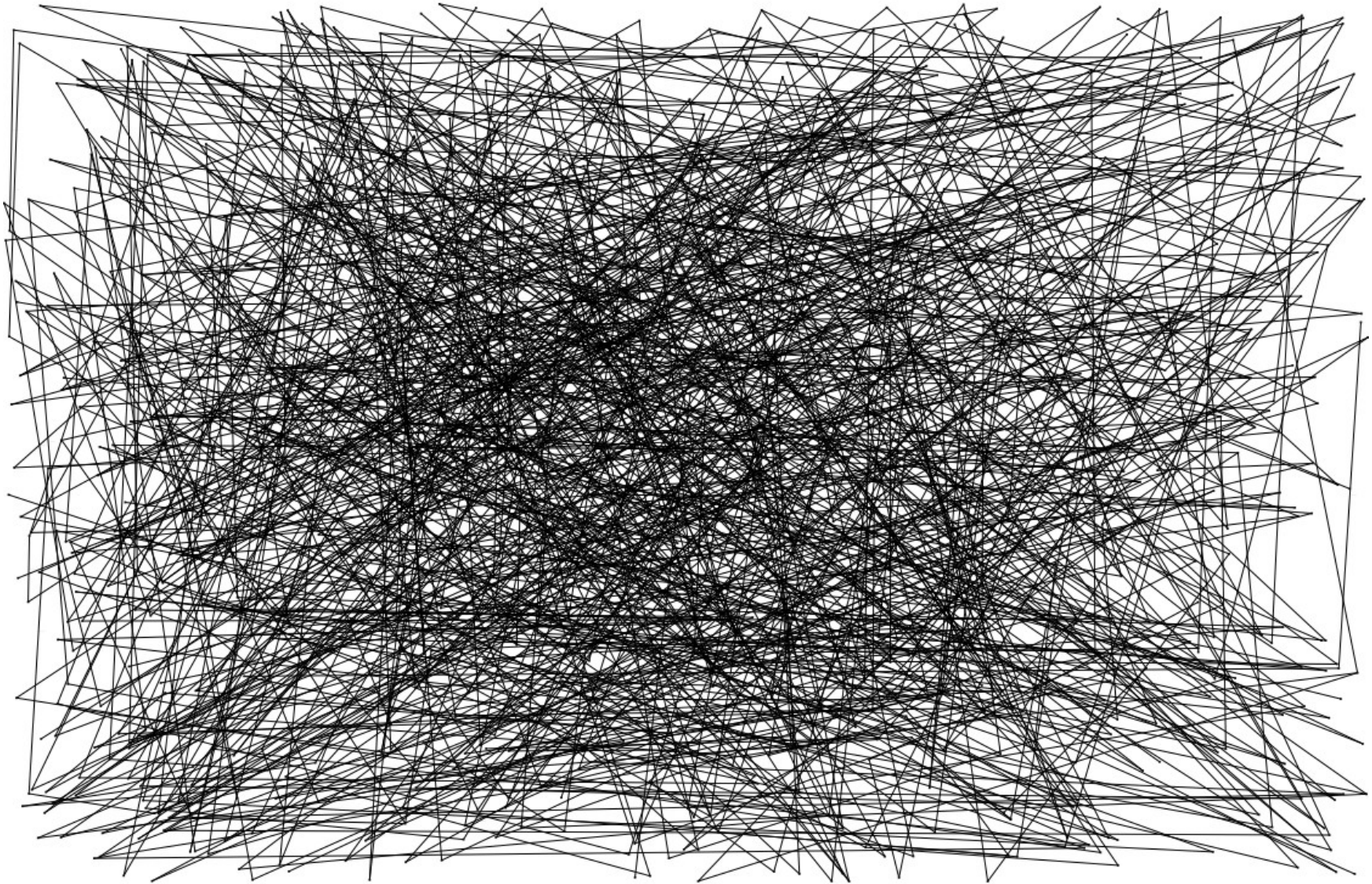
Scores some 200 points in SV-COMP setting – winner had 280



# The Bad

Tool	CPAchecker 1.1-svn				
Test	explicitAnalysis-cbmc				
test/programs/benchmarks/	status	cputime	walltime	total	cpa time
ldv-drivers/usb_urb-drivers-media-dvb-tt...i.pp.cil.c	timeout	1491.19	1441.18		
ldv-drivers/usb_urb-drivers-net-can-usb-...i.pp.cil.c	timeout	909.99	916.13	915.205s	0.409s
ldv-drivers/usb_urb-drivers-net-usb-catc...i.pp.cil.c	timeout	1028.72	1030.08	1027.456s	0.887s
ldv-drivers/usb_urb-drivers-staging-lirc...i.pp.cil.c	timeout	938.86	939.59	928.819s	2.336s
ldv-drivers/usb_urb-drivers-usb-misc-iow...i.pp.cil.c	timeout	1017.04	998.04		
ldv-drivers/module_get_put-drivers-atm-e...i.pp.cil.c	timeout	934.87	934.88	908.204s	899.954s
ldv-drivers/module_get_put-drivers-block...i.pp.cil.c	timeout	1016.88	1030.26		
ldv-drivers/module_get_put-drivers-block...i.pp.cil.c	timeout	937.89	922.41	902.830s	899.955s
ldv-drivers/module_get_put-drivers-bluet...i.pp.cil.c	timeout	1016.43	889.71		
ldv-drivers/module_get_put-drivers-char-...i.pp.cil.c	timeout	6.45	5.18	3.897s	1.233s
ldv-drivers/module_get_put-drivers-gpu-d...i.pp.cil.c	out of memory	605.10	600.54		
ldv-drivers/module_get_put-drivers-hid-h...i.pp.cil.c	timeout	1017.02	930.81		
ldv-drivers/module_get_put-drivers-hwmon...i.pp.cil.c	out of memory	983.87	937.24		
ldv-drivers/module_get_put-drivers-net-a...i.pp.cil.c	timeout	1016.98	959.73		
ldv-drivers/module_get_put-drivers-net-p...i.pp.cil.c	timeout	1016.61	1004.24		
ldv-drivers/module_get_put-drivers-net-s...i.pp.cil.c	timeout	953.26	951.86	908.554s	899.805s
ldv-drivers/module_get_put-drivers-net-t...i.pp.cil.c	timeout	950.36	940.60	910.871s	899.944s
ldv-drivers/module_get_put-drivers-stagi...i.pp.cil.c	timeout	957.40	959.23	912.302s	899.948s
ldv-drivers/module_get_put-drivers-stagi...i.pp.cil.c	timeout	957.40	959.23	912.302s	899.948s

# The Ugly





# Explicit-Value Model Checking

Up to now: plain and simple

- ? Abstraction
- ? Counterexample-Guided Abstraction Refinement
- ? Interpolation

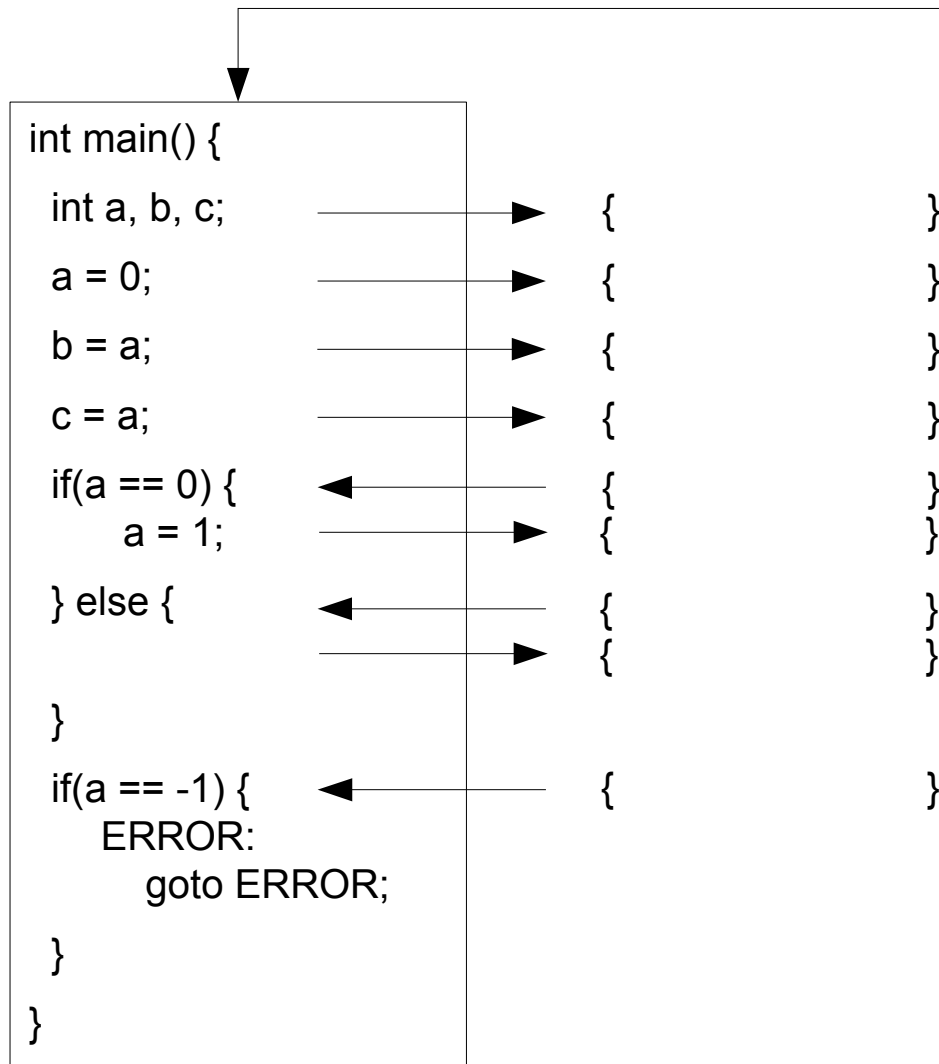
*All known in the predicate domain for years*

# Explicit-Value Model Checking

As of now: with CEGAR and Interpolation

- Abstraction – Easy, just drop information
  - Counterexamples – We get these for free
  - Refinement – This is the hardest part
- Explicit-Value Model Checking  
based on *CEGAR*  
and *Interpolation*

# Abstraction



This spurious counterexample trace will always be reported ...

... unless we define a *precision*  $\pi$ ,  
i.e. a *mapping from program locations to a set of variable identifiers*,  
e.g.  $\{N2 \rightarrow \{a, b\}, N7 \rightarrow \{a, c\}\}$

# Craig Interpolation

For a pair of *formulas*  $\varphi^-$  and  $\varphi^+$  such that,  $\varphi^- \wedge \varphi^+$  is *unsatisfiable*, a Craig interpolant  $\psi$  is a *formula* that fulfills the following requirements:

- 1)  $\varphi^-$  implies  $\psi$
- 2)  $\psi \wedge \varphi^+$  is *unsatisfiable*
- 3)  $\psi$  only contains symbols that are common to both  $\varphi^-$  and  $\varphi^+$ .

→ use this for the Explicit Domain



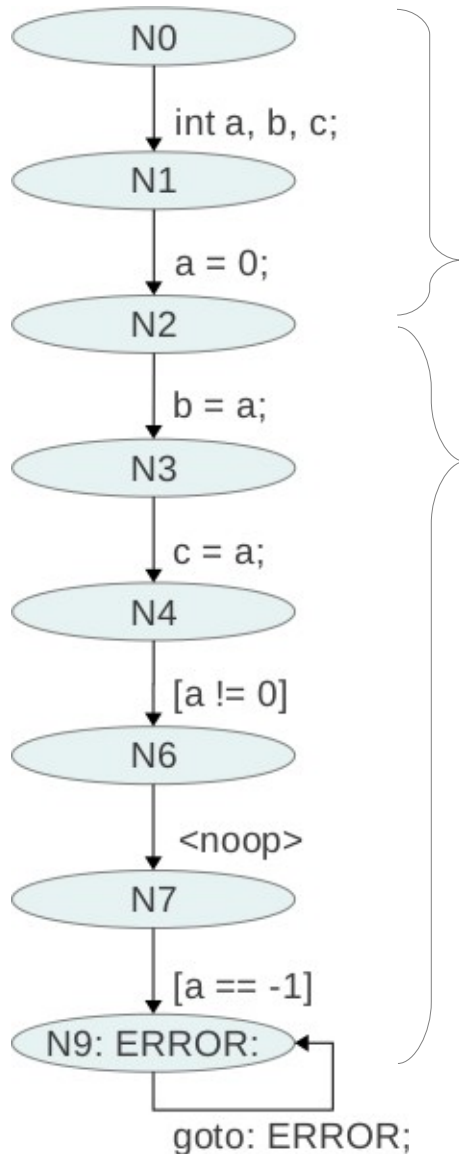
# “Explicit” Craig Interpolation (1)

For a pair of *path assignments*  $\varphi^-$  and  $\varphi^+$  such that,  $\varphi^-$  and  $\varphi^+$  are *contradicting*, a Craig interpolant  $\psi$  is a *variable assignment* that fulfills the following requirements:

- 1)  $\varphi^-$  implies  $\psi$
- 2)  $\psi$  and  $\varphi^+$  are *contradicting*
- 3)  $\psi$  only contains symbols that are common to both  $\varphi^-$  and  $\varphi^+$ .



# „Explicit“ Craig Interpolation (2)



✓ Check if path is infeasible

$$\varphi_2^- = \{a \rightarrow 0\}$$

$$\varphi_2^+ = \{a \rightarrow -1\}$$

$$\psi = \{a \rightarrow 0\}$$

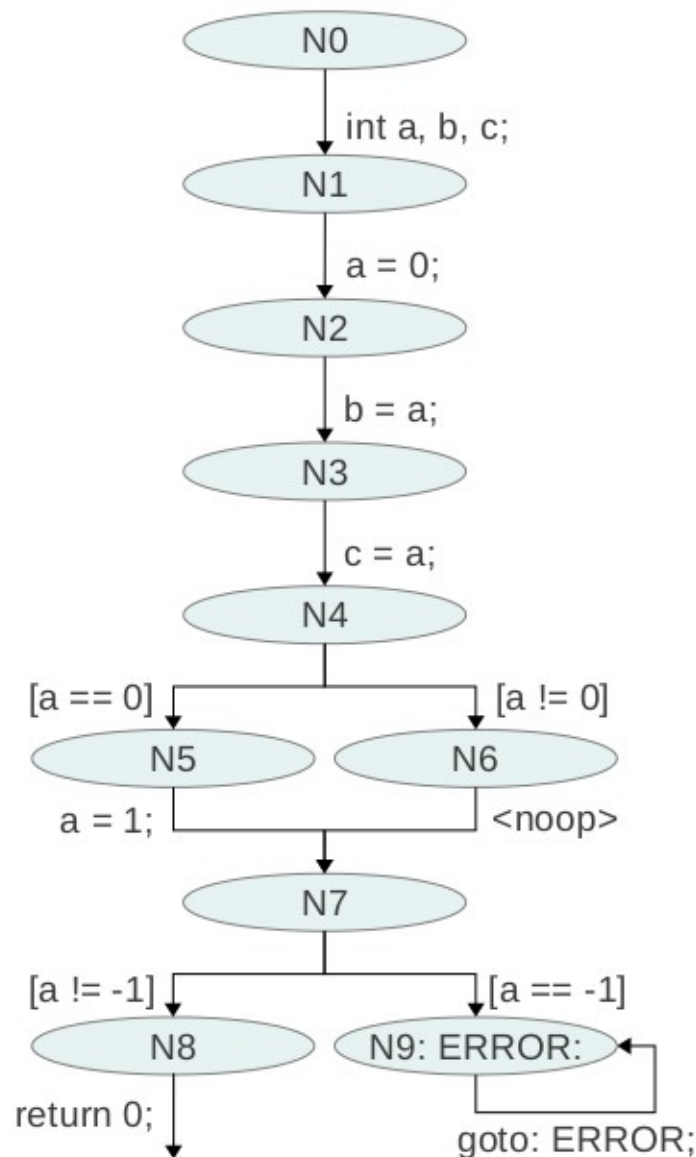
✓  $\varphi_2^-$  implies  $\psi$

✓  $\varphi_2^-$  and  $\varphi_2^+$  are contradicting

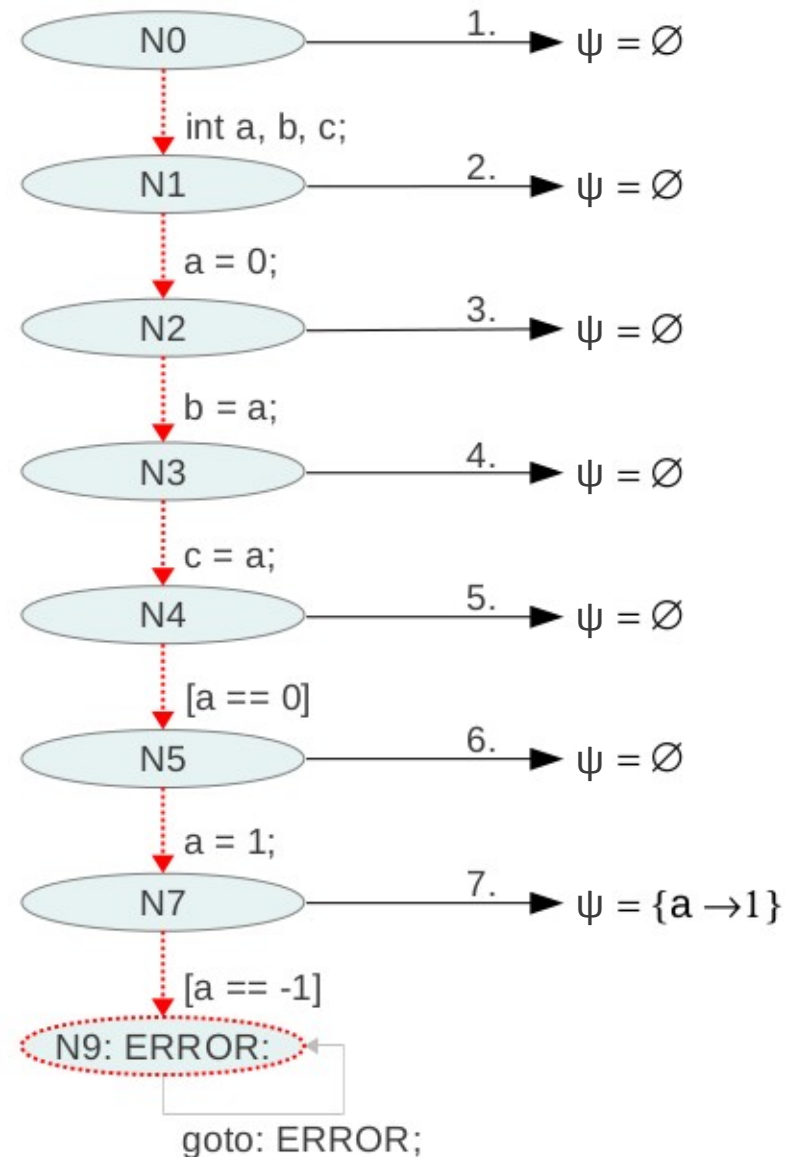
✓ common symbols

➤ Add  $[N2 \rightarrow \{a\}]$  to the precision

# „Explicit“ Craig Interpolation (3)

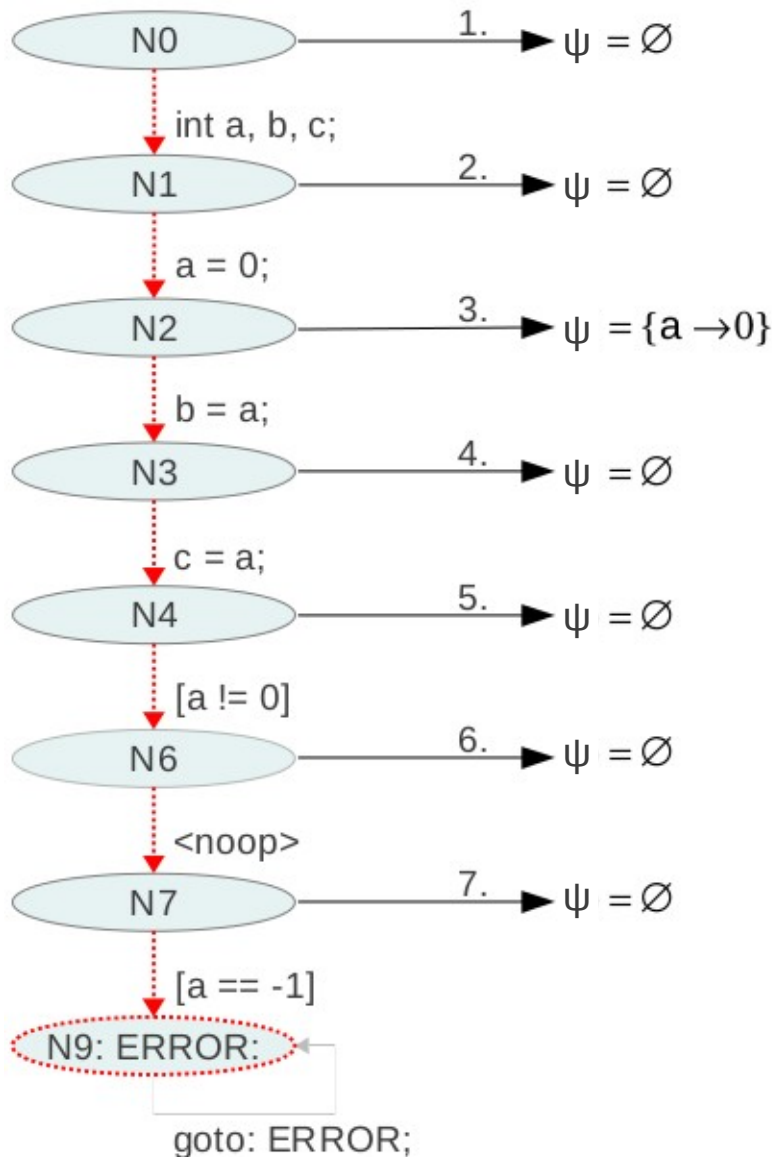


CFA

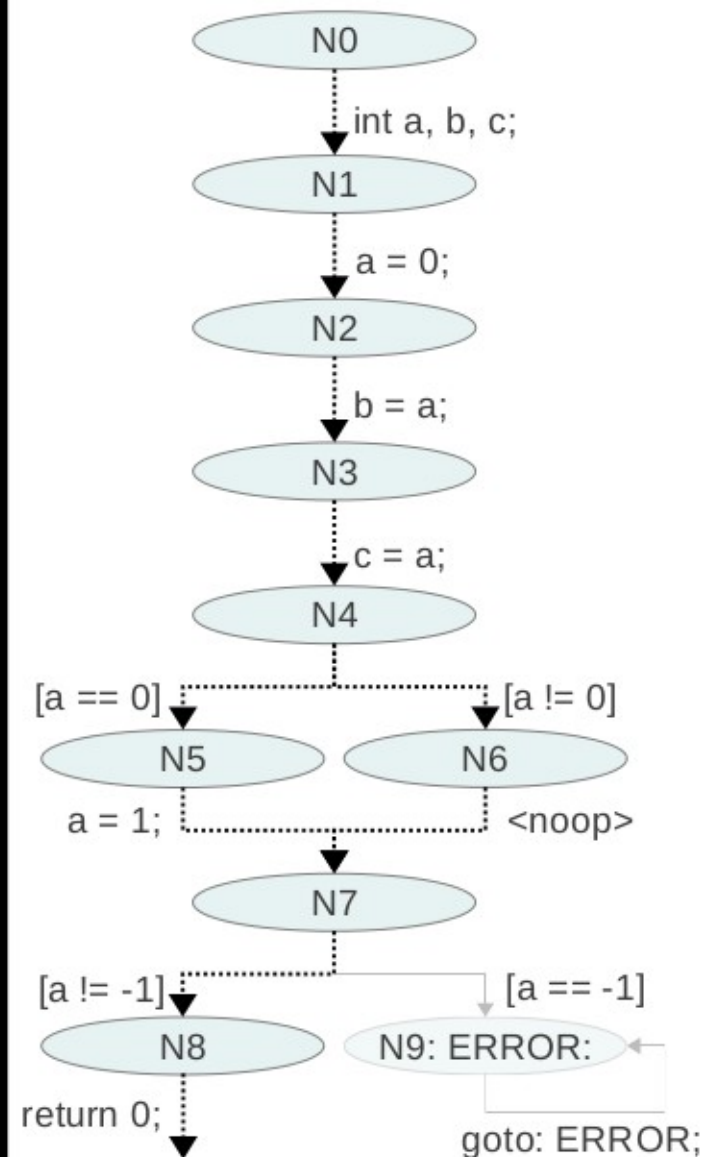


$\Pi_1 = [N7 \rightarrow \{a\}]$

# „Explicit“ Craig Interpolation (4)



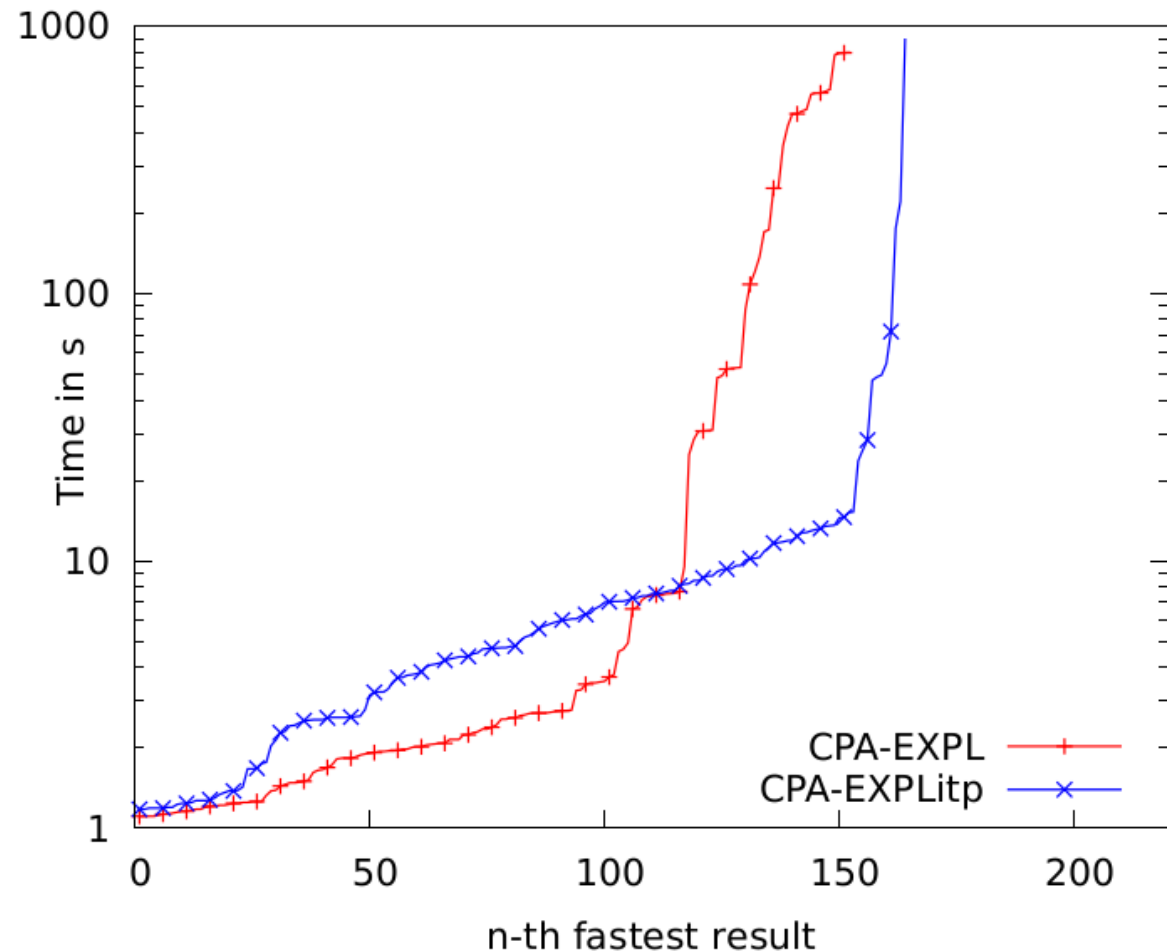
$$\Pi_2 = \Pi_1 \cup [N2 \rightarrow \{a\}]$$



*Program proven safe*

# What do we have so far?

- ✓ Abstraction
- ✓ CEGAR
- ✓ Interpolation

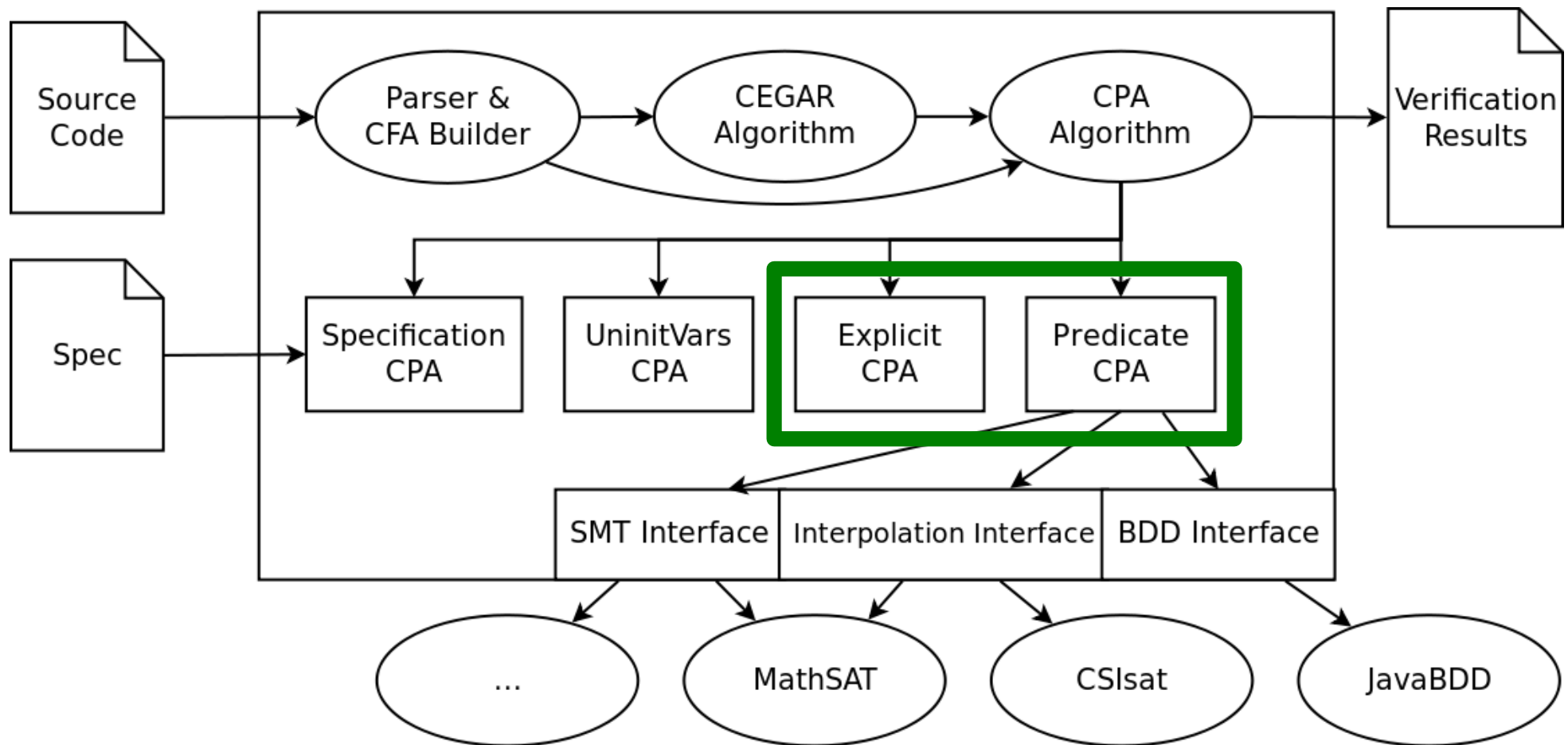


✗ Precise state representation

✗ Inequalities  $[a \neq b]$

✗ Intervals  $[a < b]$

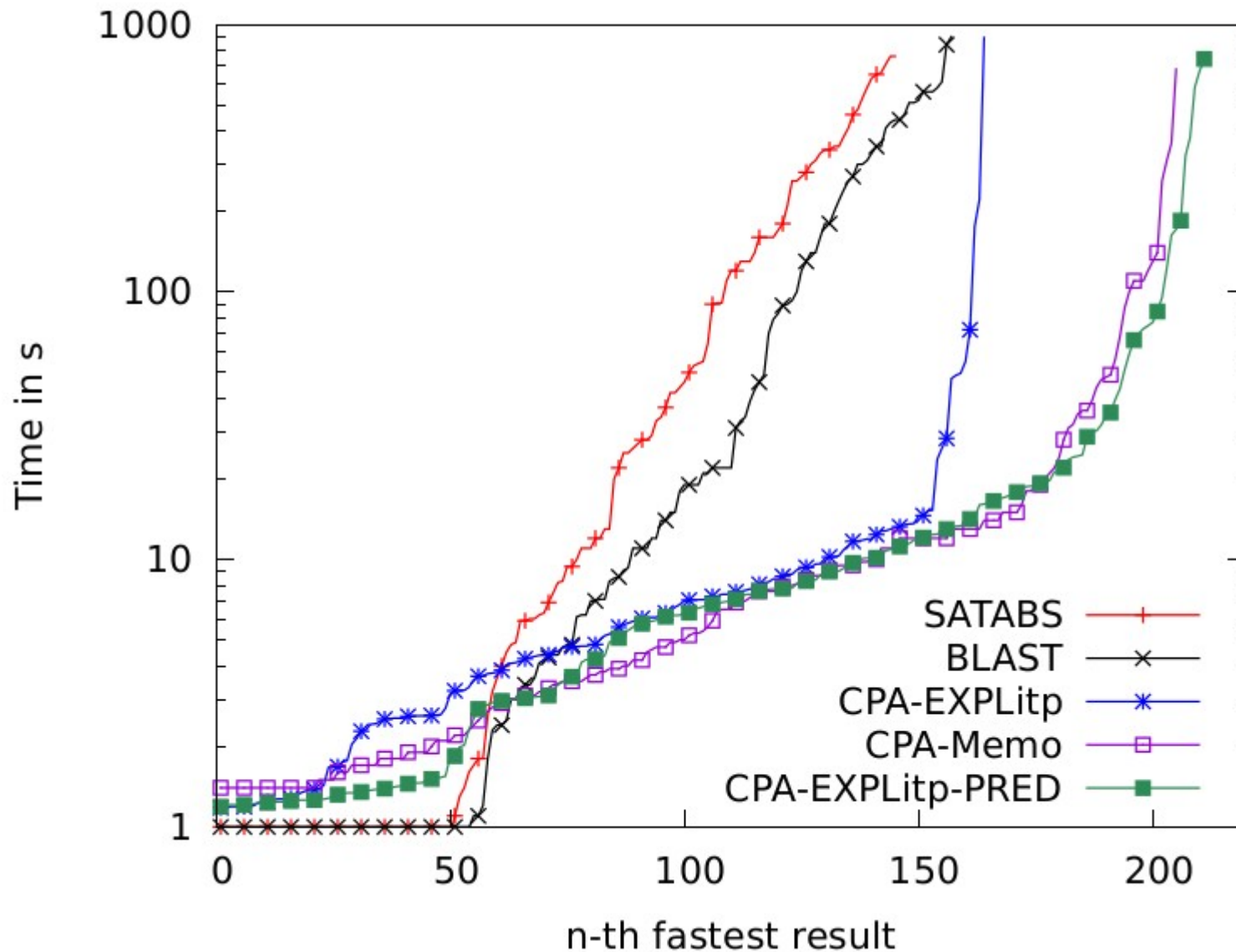
# CPAchecker: Architecture



- Add auxiliary predicate analysis
- Refinement of both domains based on (lack of) expressiveness
- Predicate analysis tracks only what is beyond explicit domain



# Comparison with SV-COMP Run Times



# Comparison with SV-COMP Scores

	Results taken from SV-COMP'12			Results from our experiments		
	BLAST 2.7	SATABS	CPA-Memo	CPA-Expl	CPA-Expl- ltp	CPA-Expl- ltp-Pred
ControlFlow	71	75	140	124	123	141
Drivers32	72	71	51	53	53	71
Drivers64	55	32	49	5	33	37
Heap	--	--	4	1	1	8
SystemC	33	57	36	34	34	61
Overall	231	236	<b>280</b>	217	<b>244</b>	<b>318</b>

# Conclusion

- We defined abstraction, CEGAR and Craig interpolation for the explicit domain
- Results are very encouraging
  - Valid methods to lower size of reached set
    - Circumvent state-space explosion
- ExplicitCPA proofs to be competitive
- Especially in combination with auxiliary predicate analysis

# Questions ?