

INFORMATION REUSE FOR MULTI-GOAL REACHABILITY ANALYSES

Dirk Beyer, *Andreas Holzer*, Michael Tautschnig, and Helmut Veith

Motivation



- Test generation with model checkers
- Model checker: Does a program satisfy a temporal specification?
- If not, produce counterexample: program trace

Motivation

- Test generation with model checkers
- Model checker: Does a program satisfy a temporal specification?
- If not, produce counterexample: program trace
- Encode negation of test goal as specification
 - ▣ Counterexample: Test case
 - ▣ Derive inputs from counterexample
 - ▣ No Counterexample: No test case exists!

White-Box Testing

Program

```
1 if (x > 10)
2     f1 = false;
3 else
4     f1 = true;
5 if (x == 100)
6     f2 = false;
7 if (f1)
8     s = f2;
9 else
10    s = f1;
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Decision Coverage

White-Box Testing

Program

Decision Coverage

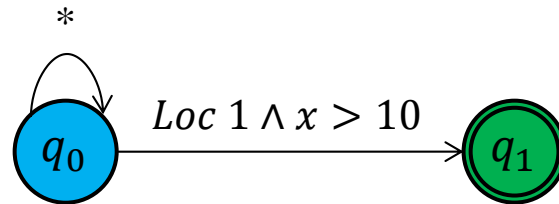
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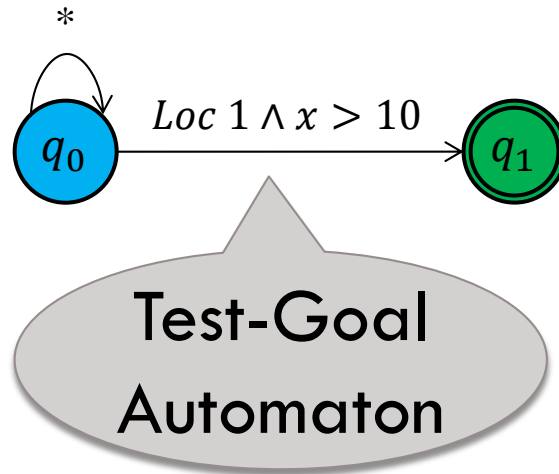


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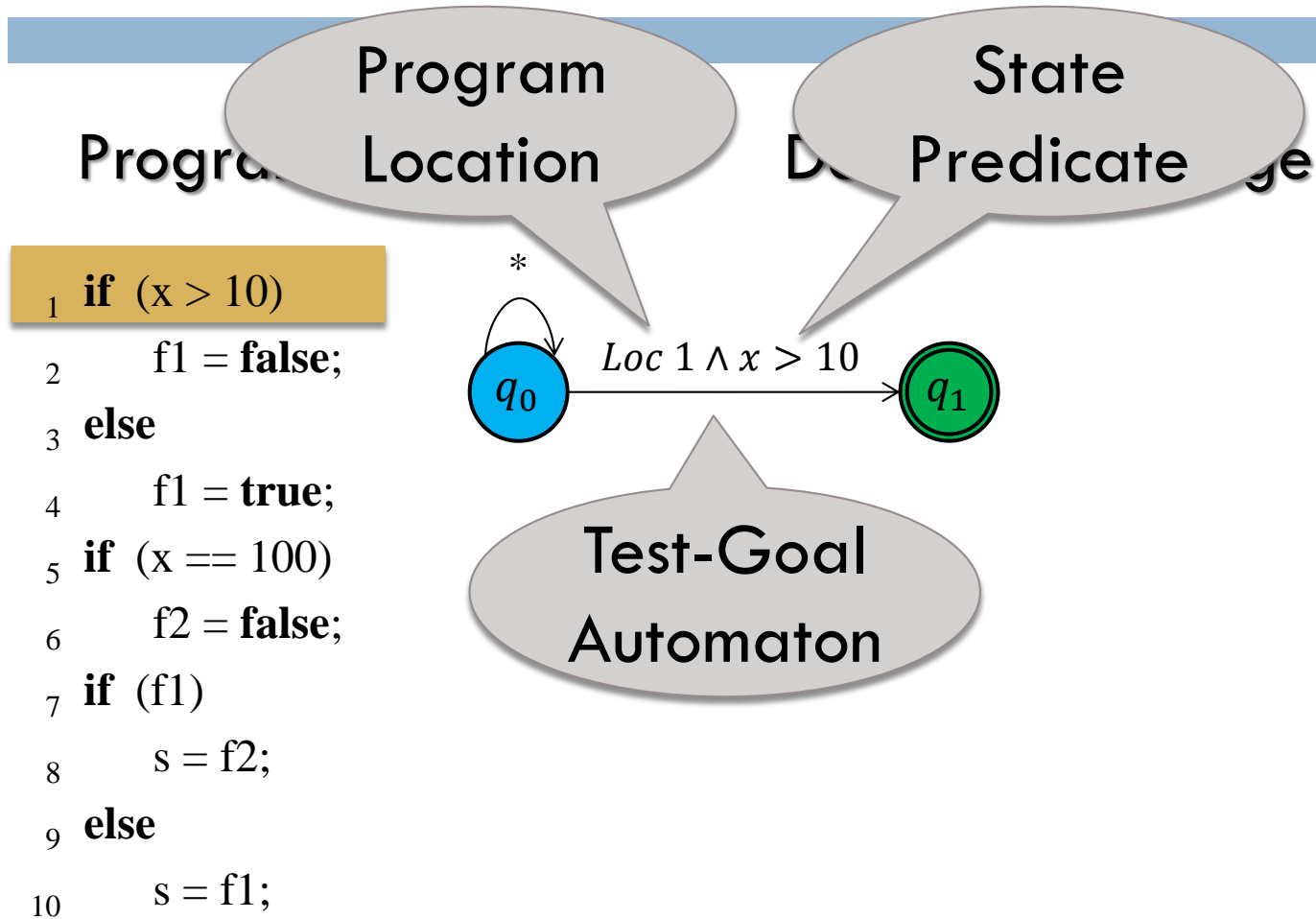
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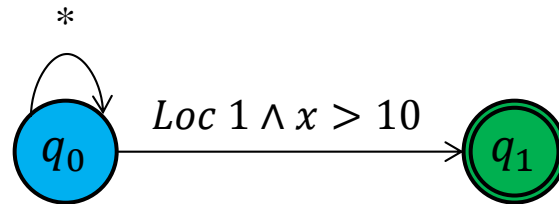


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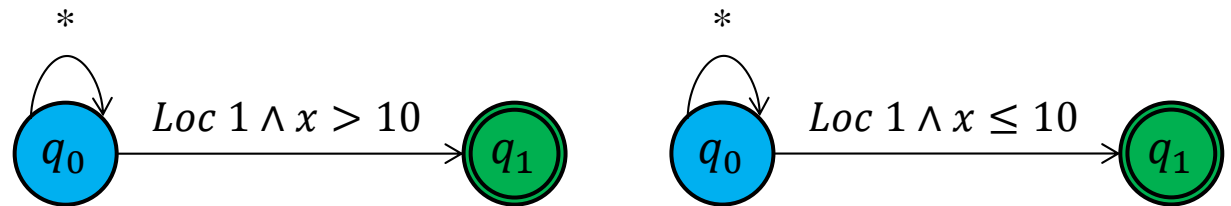


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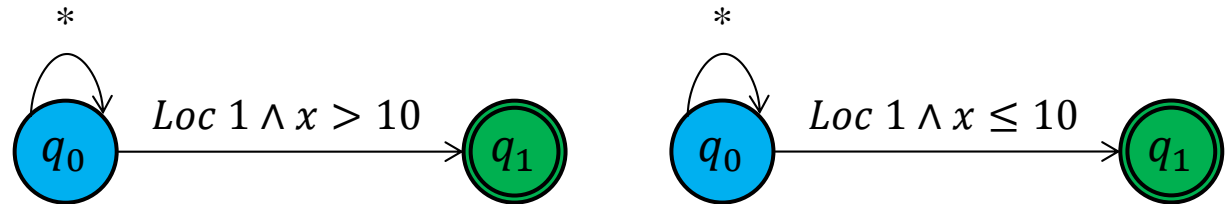


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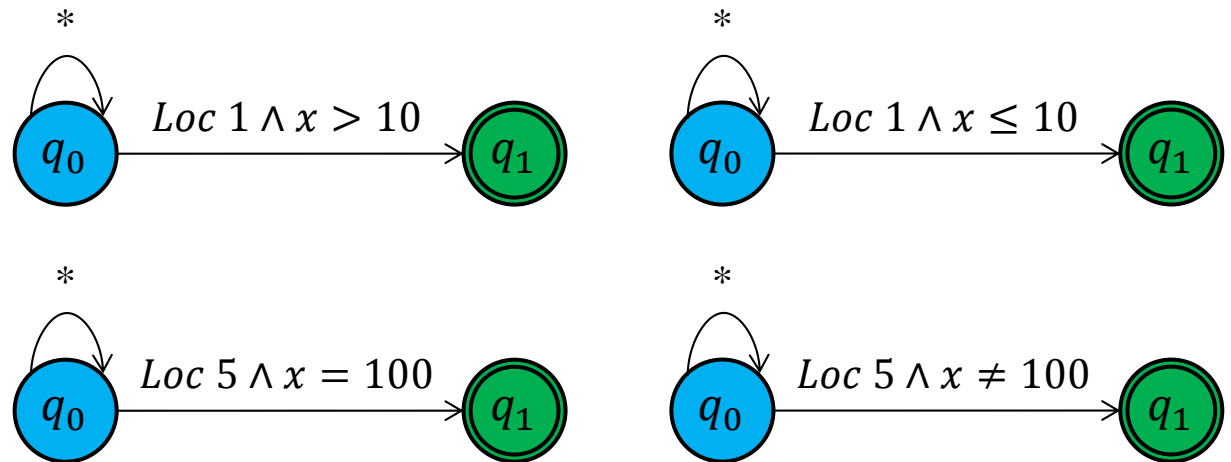


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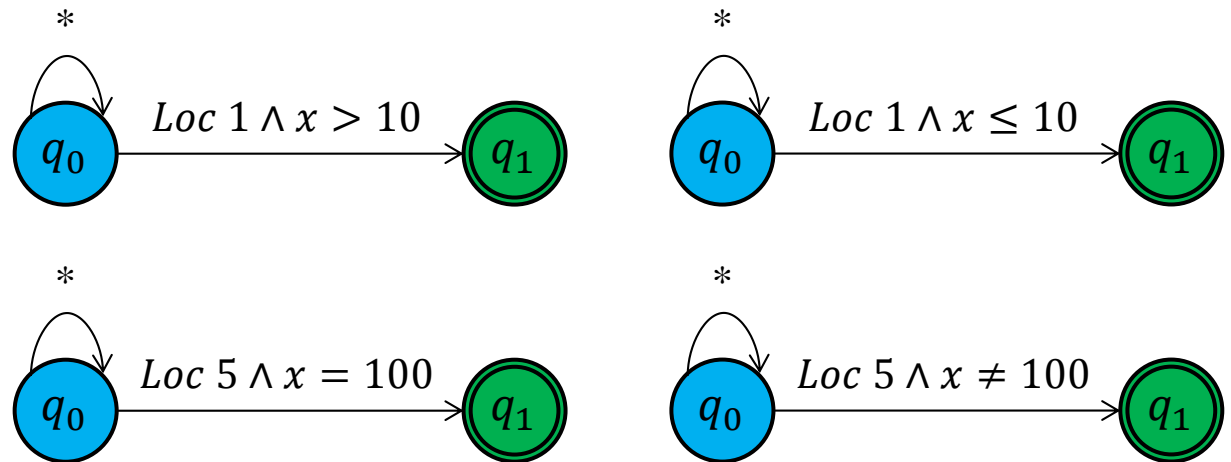


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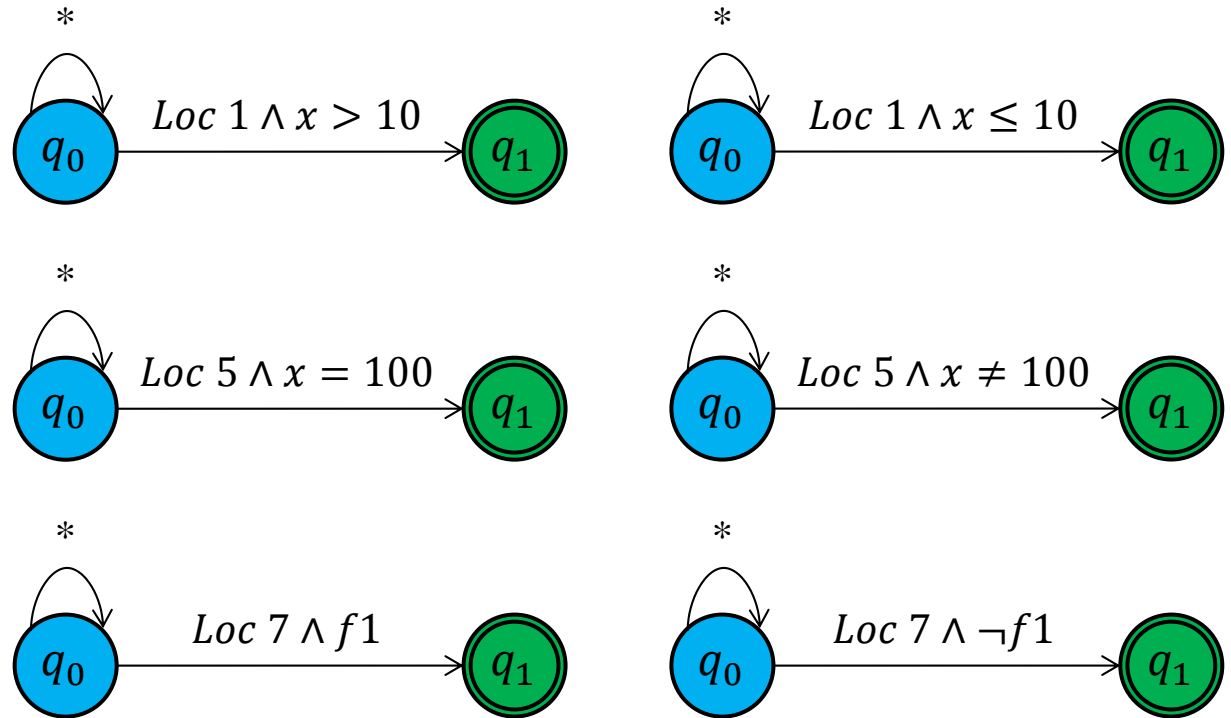


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White-Box Testing

Program

*(Basic Block)*² Coverage

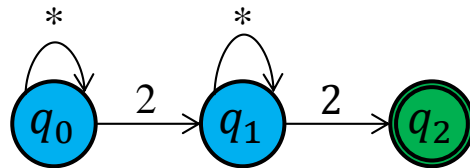
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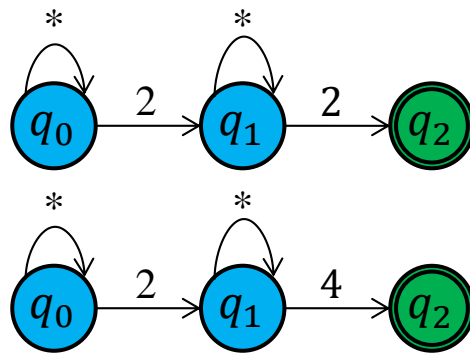


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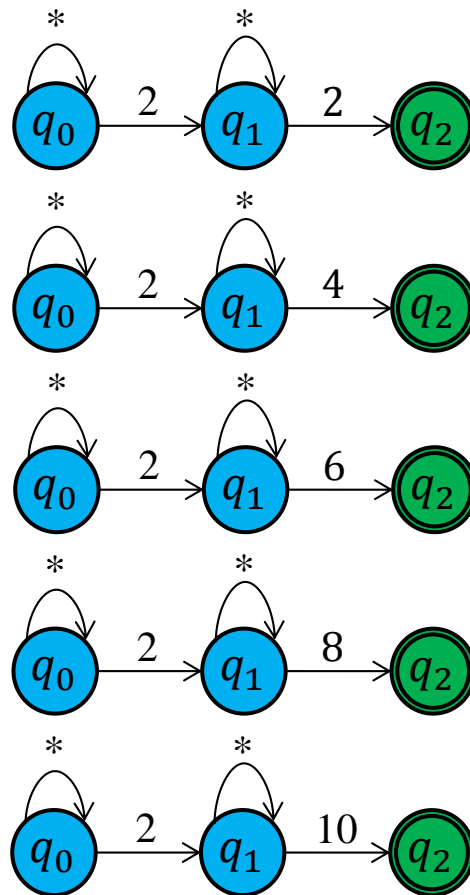


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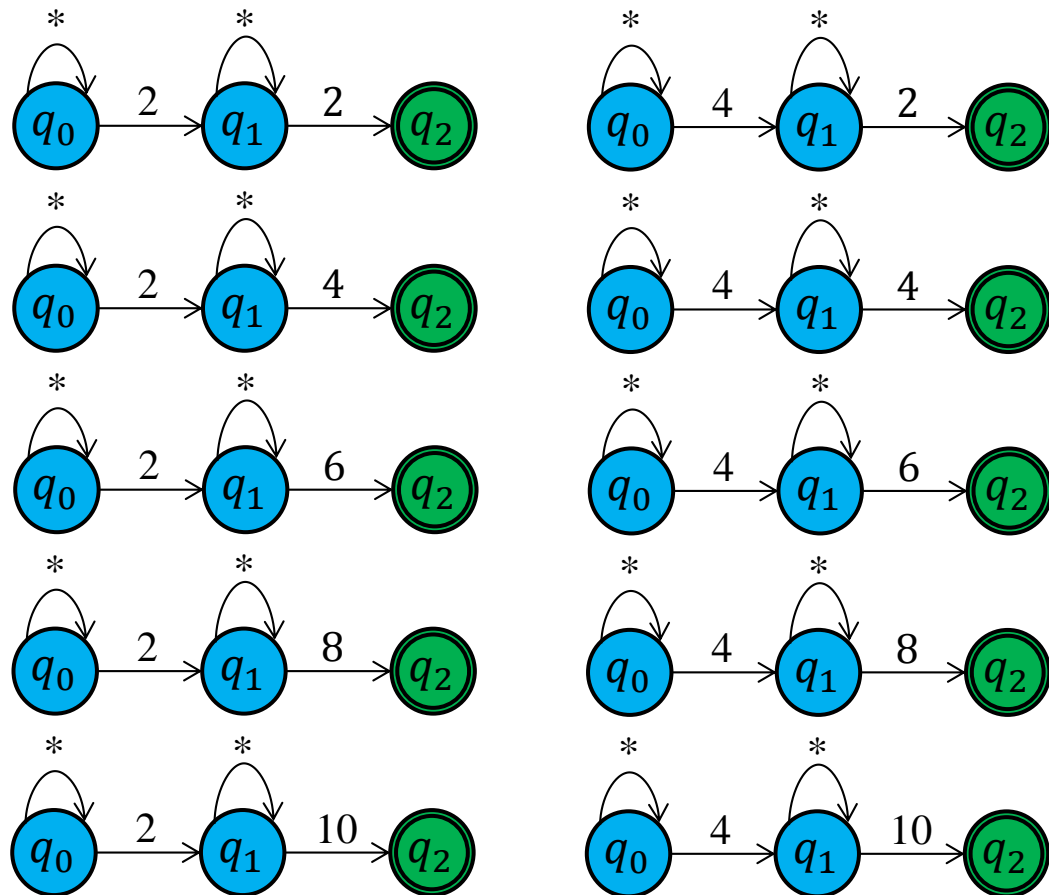


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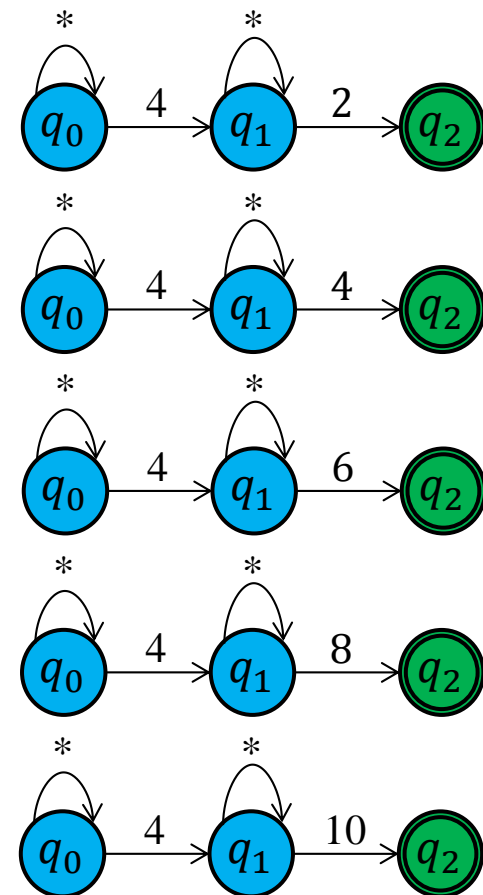
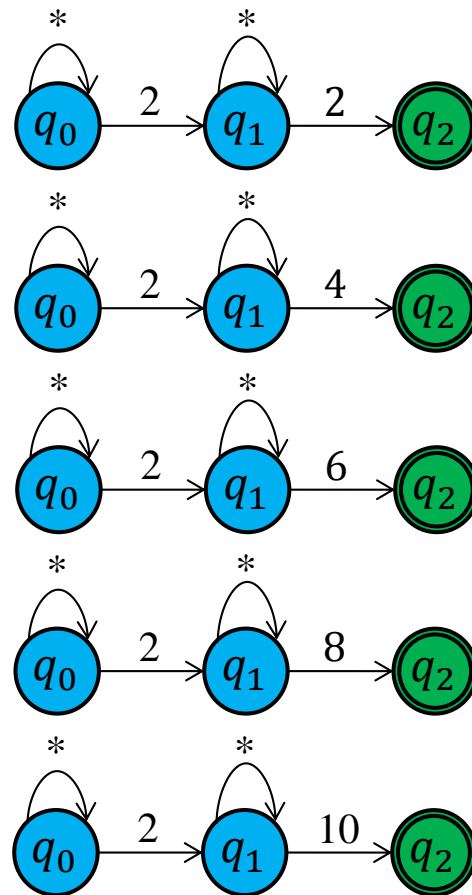


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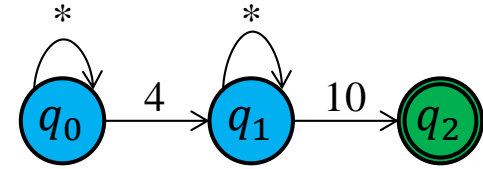
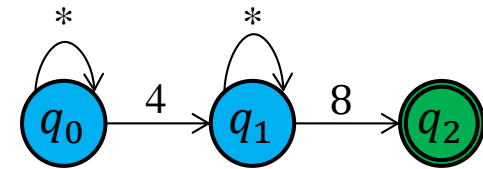
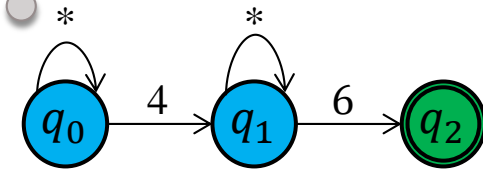
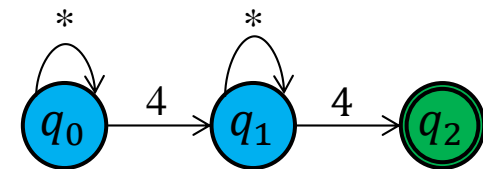
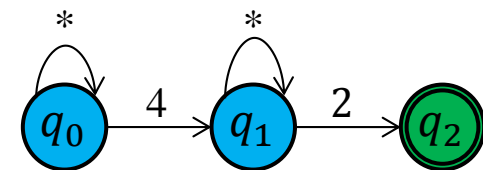
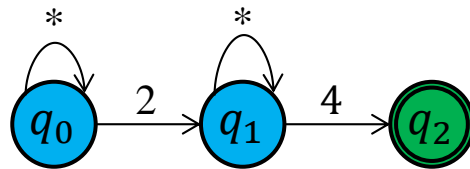
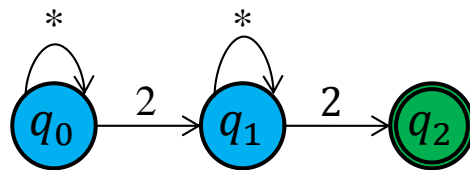
...

White-Box Testing

Program

```
1 if (x > 10)
2   f1 = false;
3 else
4   f1 = true;
5 if (x == 100)
6   f2 = f2';
```

(Basic Block)² Coverage



...

For real-world
programs we get a
huge set of test
goals!

White-Box Testing

Program *(Basic Block)²* Coverage

		*	*	*	*
	Source	Lines of Code	#Goals <i>BB</i>	#Goals <i>BB²</i>	
1	if				
2	kbfilter 1	771	118	13924	
3	else				
4	kbfilter 2	1352	203	41209	
5	kbfilter 3	1349	202	40804	
6	if				
	floppy 1	1510	209	43681	
	floppy 2	1529	209	43681	
	floppy 3	2198	291	84681	
	floppy 4	2198	291	84681	
	cdaudio 1	2997	420	176400	
	cdaudio 2	2992	417	173889	
	diskperf	1477	202	40804	

...

White-Box Testing

- **FShell Query Language (FQL)** [VMCAI'09, ASE'10, HVC'10, FASE'11]

- ▣ Specification Language for Coverage Criteria

- ▣ Decision Coverage:

- `cover @DECISIONEDGE`

- ▣ *Basic Block* Coverage:

- `cover @BASICBLOCKENTRY`

- ▣ *(Basic Block)²* Coverage:

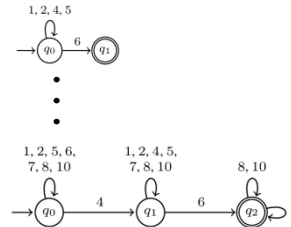
- `cover @BASICBLOCKENTRY -> @BASICBLOCKENTRY`

- ▣ Coverage Criterion gets instantiated to a set of Test Goals

Multi-Goal Reachability Analysis

Test-Goal Automata

A_1, A_2, \dots, A_n



Automaton-Guided
Reachability Analysis

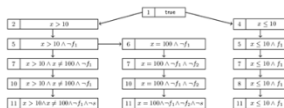
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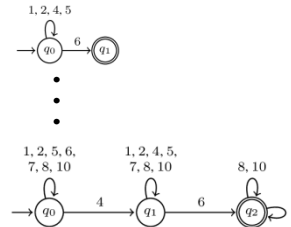
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Witnesses of
Un-/Satisfiability



Multi-Goal Reachability Analysis

Test-Goal Automata
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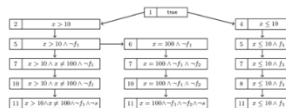


Automaton-Guided
Reachability Analysis

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Witnesses of
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Applications:

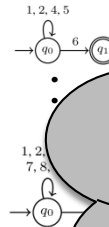
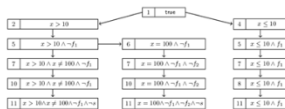
- Whitebox/Model-Based Testing
- Reachability-Oracle for Path-Insensitive Program Analyses
- Program Exploration/Debugging

Multi-Goal Reachability Analysis

Test-Goal Automata
 A_1, A_2, \dots, A_n

Automaton-Guided
Reachability Analysis

Witnesses of
Un-/Satisfiability



How can we reuse
analysis results
throughout different
automata?

Program

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Abstract Reachability Graph

Reachability Analysis

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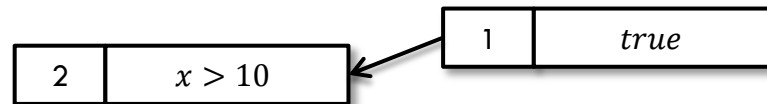
1	<i>true</i>
---	-------------

Reachability Analysis

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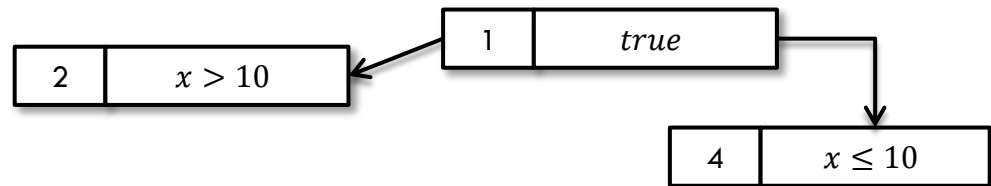


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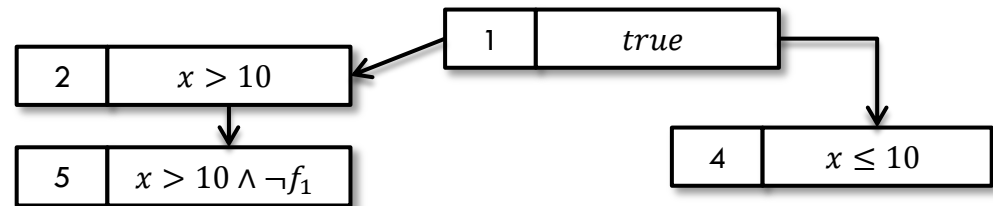


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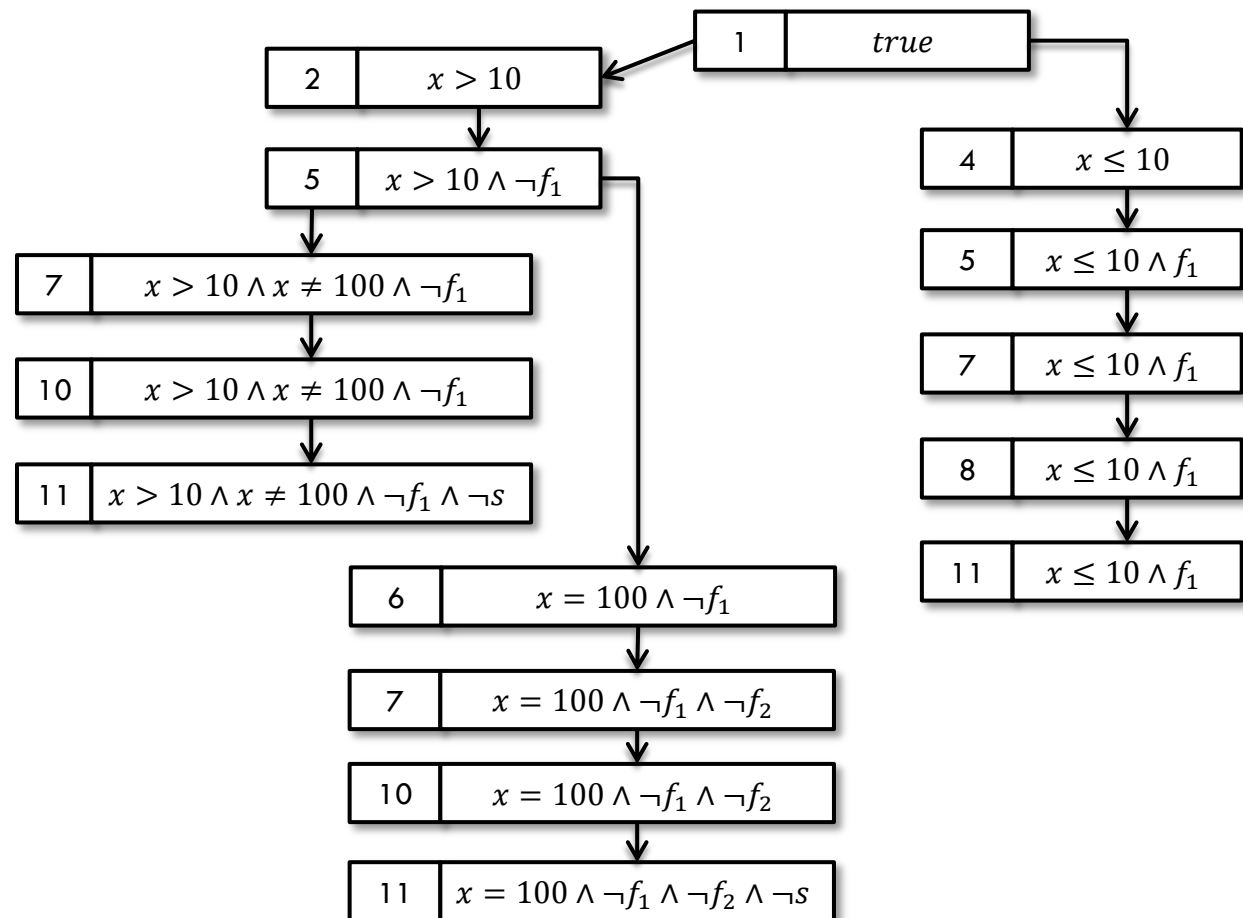


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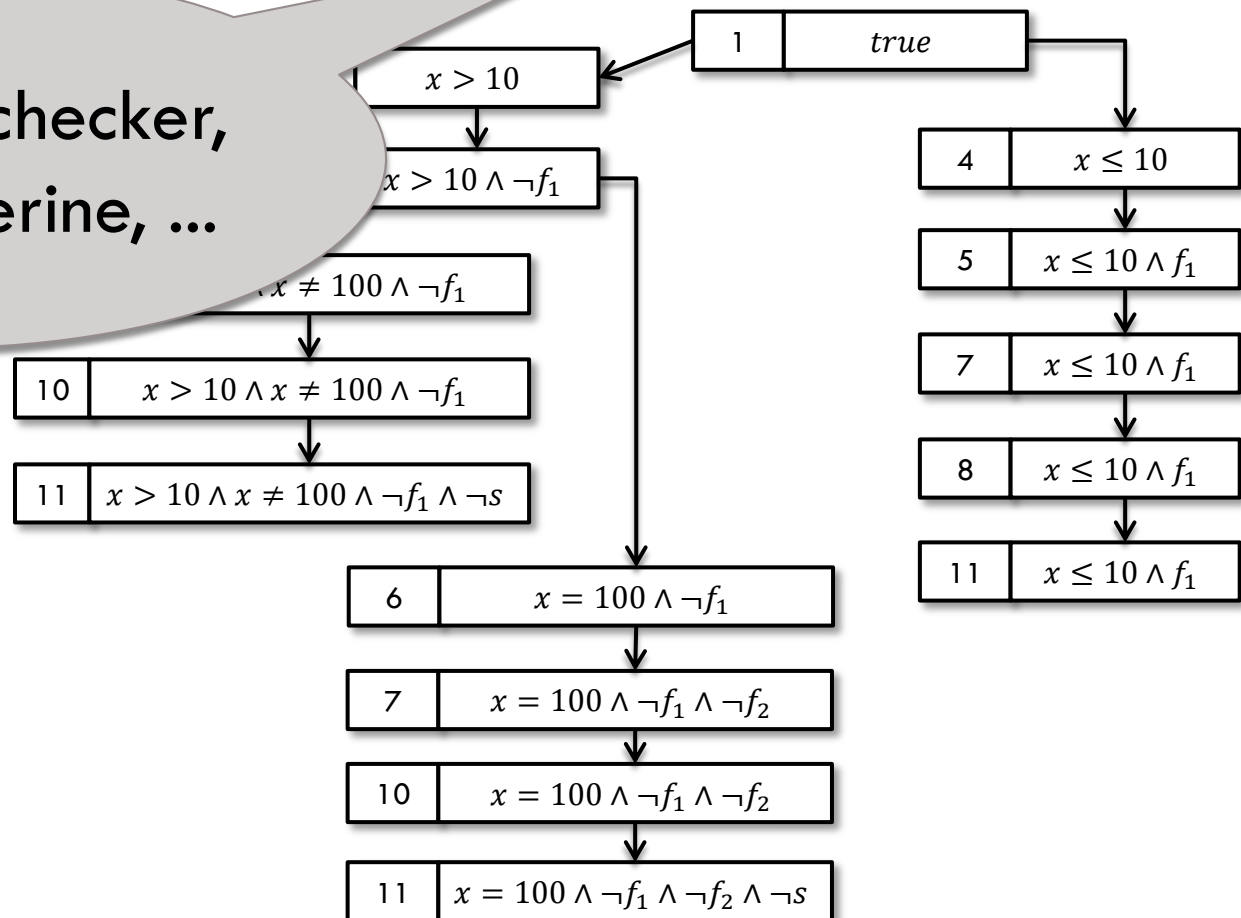
Reachability Analysis

Program

```
1  if (
2    f2 = false,
3    f1)
4    f2 = true;
5  if (f1)
6    s = f2;
7  else
8    s = f1;
```

BLAST, CPAchecker,
UFO, Wolverine, ...

Abstract Reachability Graph

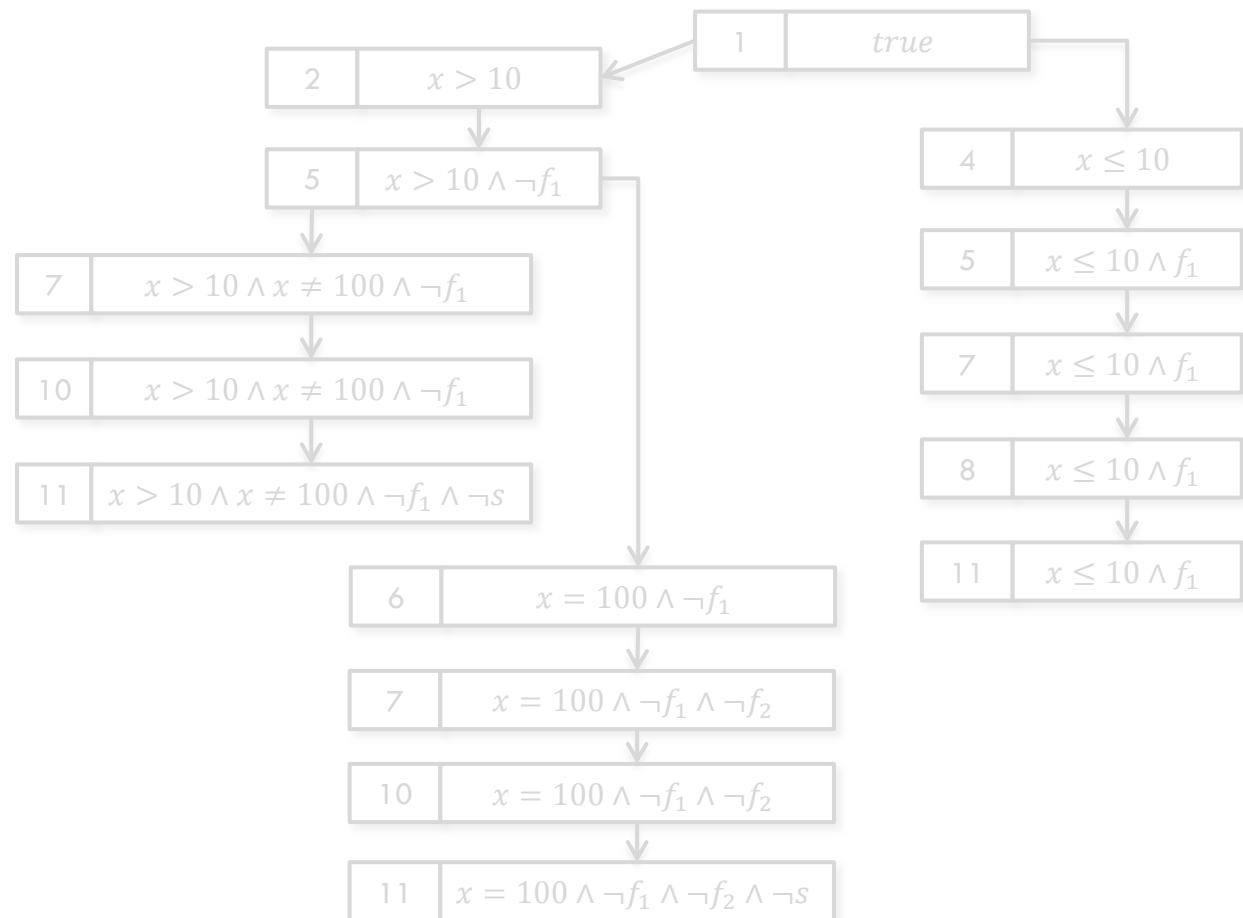


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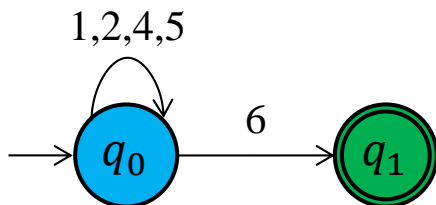


Automaton-Guided Reach. Analysis

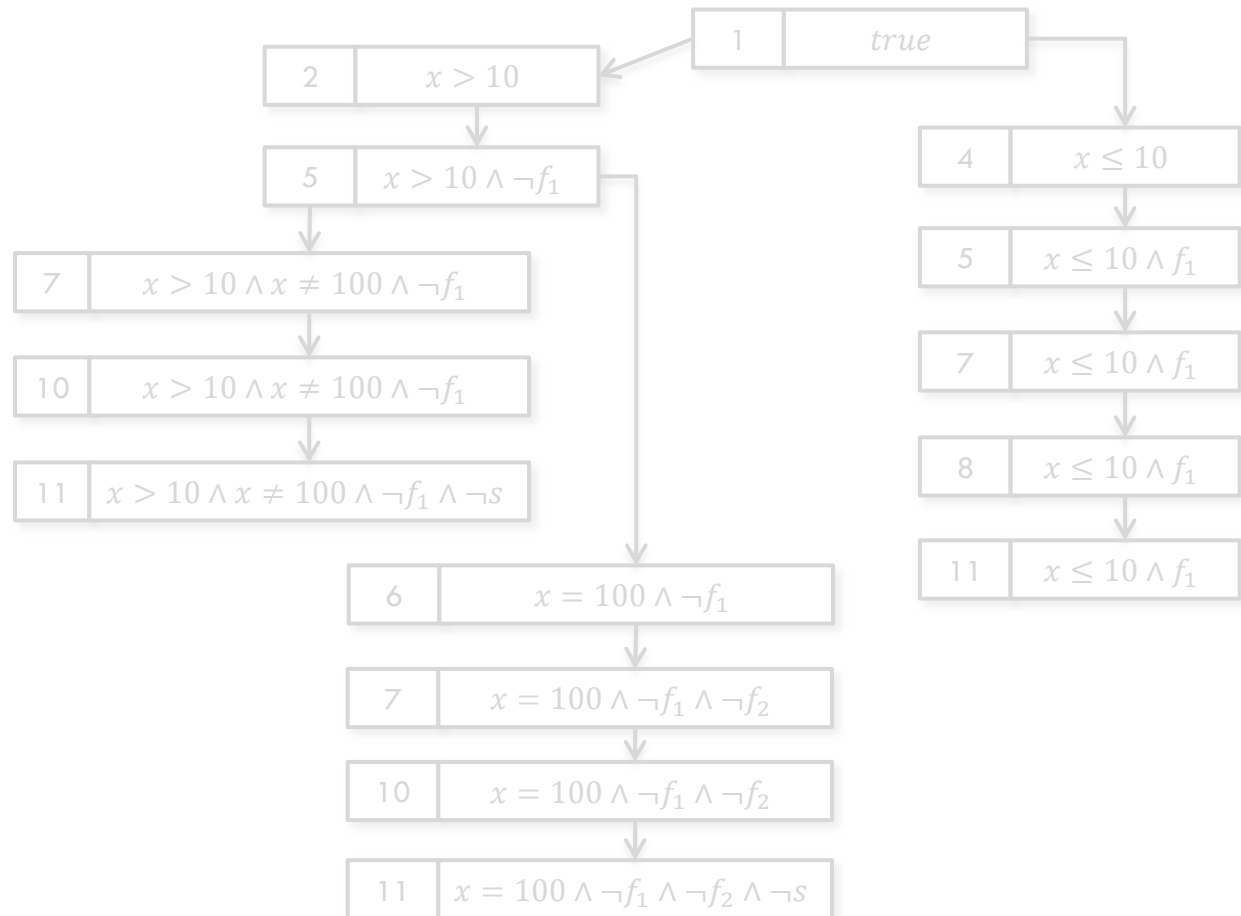
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Automaton



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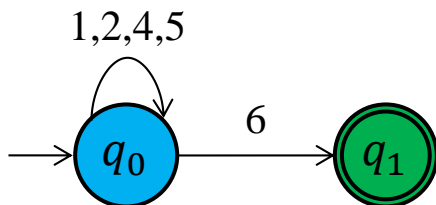


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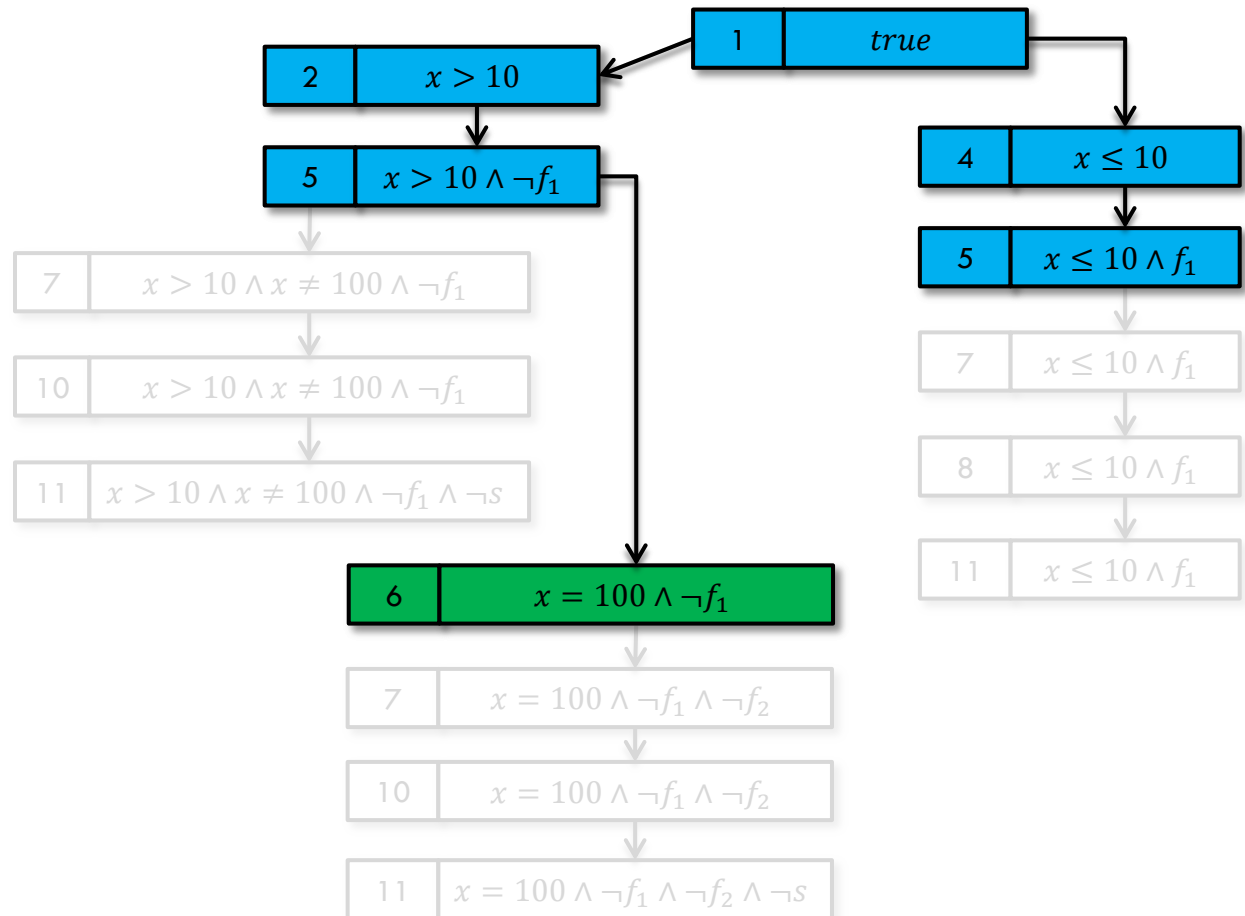
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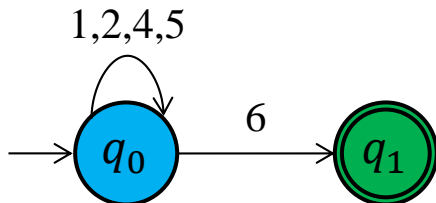


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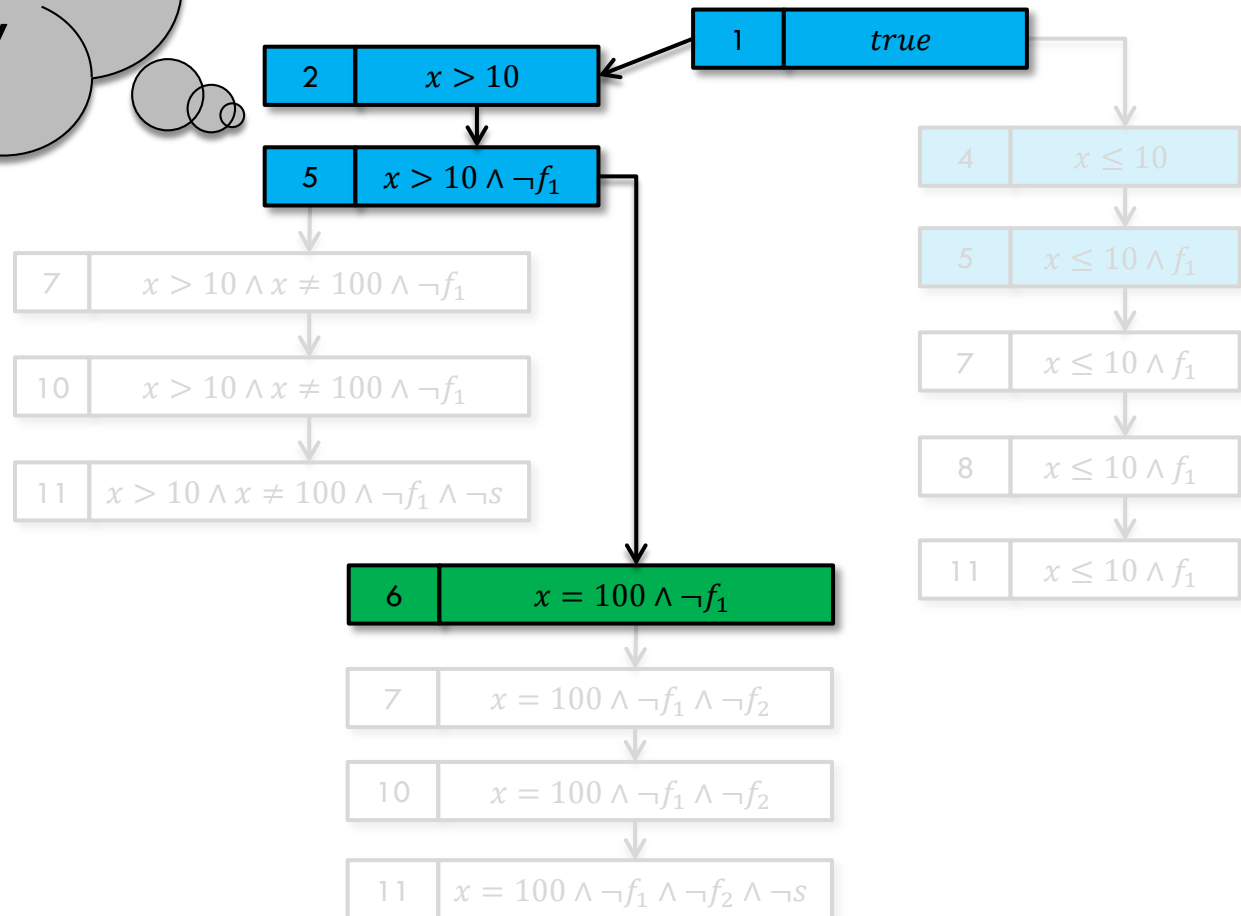
Witness of
Satisfiability

3
4 $f_1 = \text{true};$
5 **if** ($x == 100$)
6 $f_2 = \text{false};$
7 ...

Automaton



Abstract Reachability Graph



Automaton-Guided Reach. Analysis

Program

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Abstract Reachability Graph

Automaton

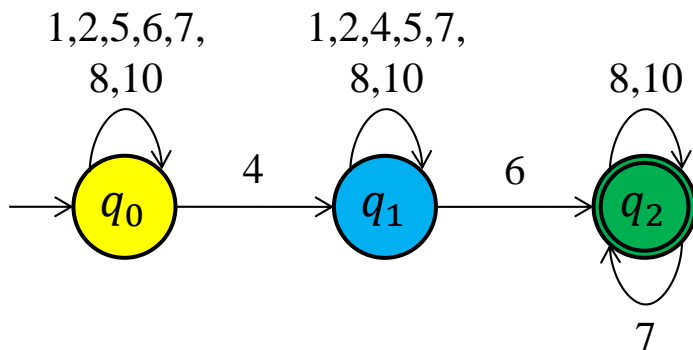
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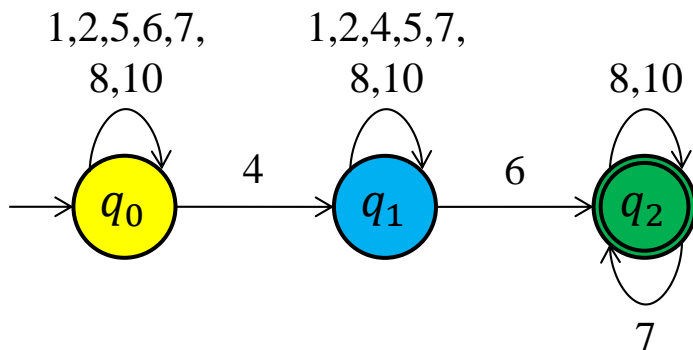


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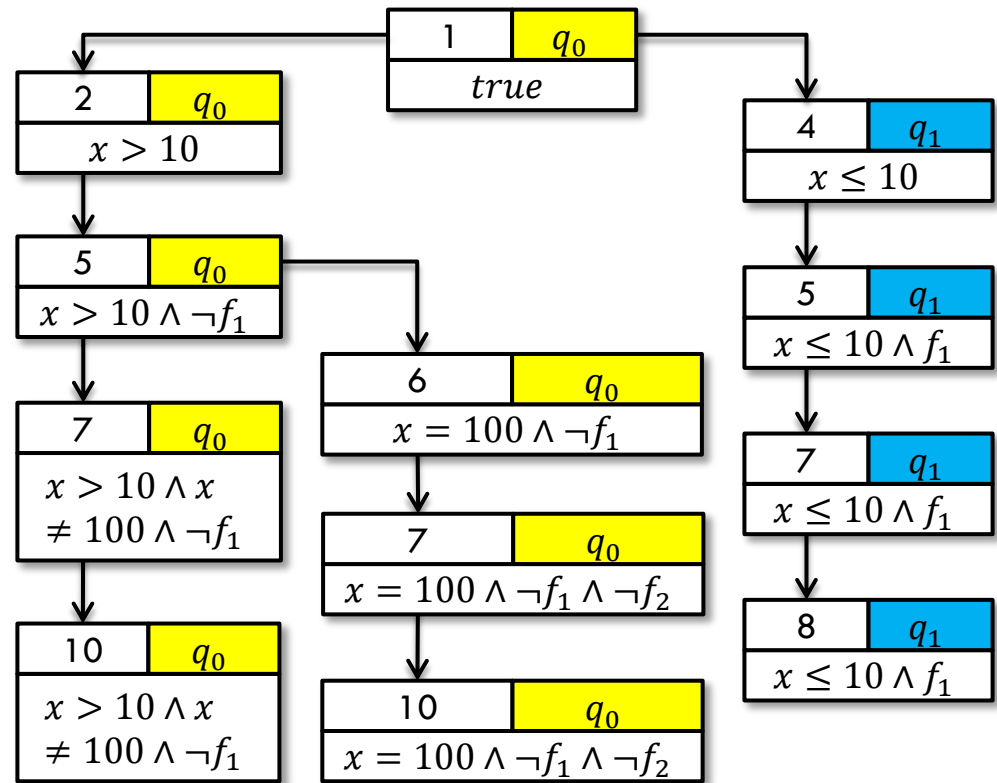
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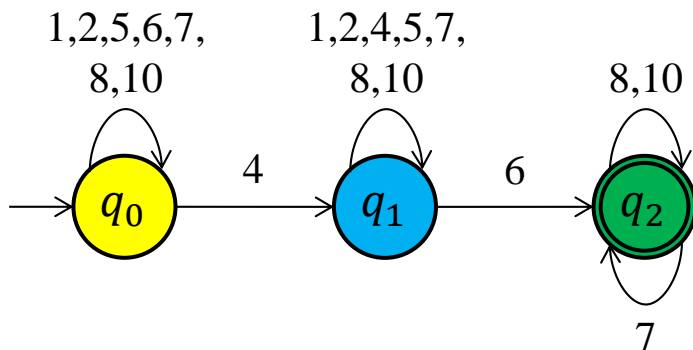


Automaton-Guided Reach. Analysis

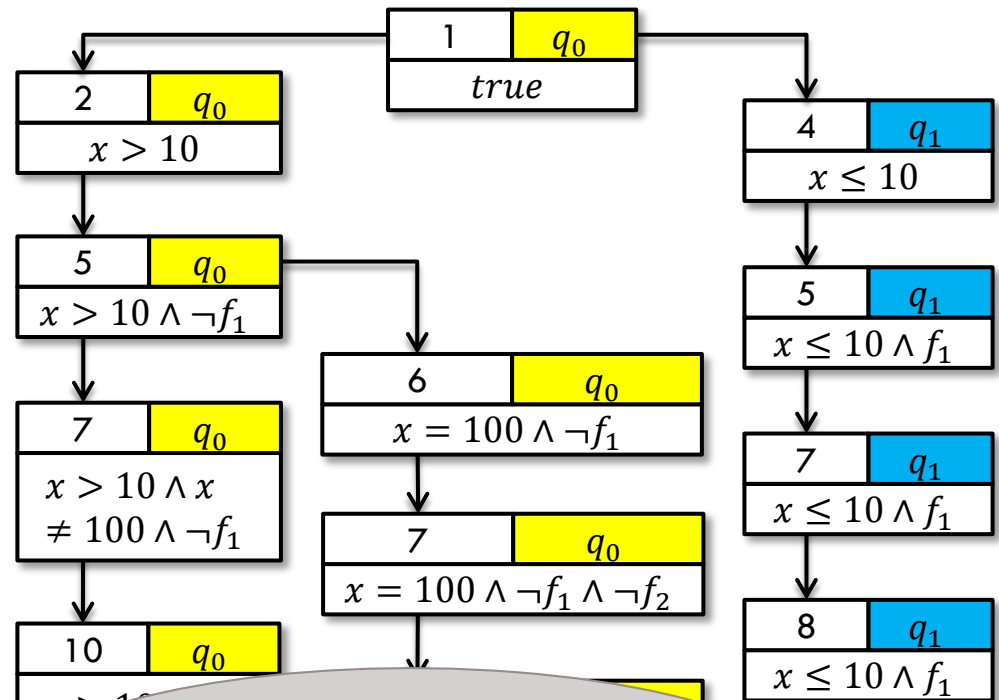
Program

```
1 if (x > 10)
2   f1 = false;
3 else
4   f1 = true;
5 if (x == 100)
6   f2 = false;
7 ...
```

Automaton



Abstract Reachability Graph



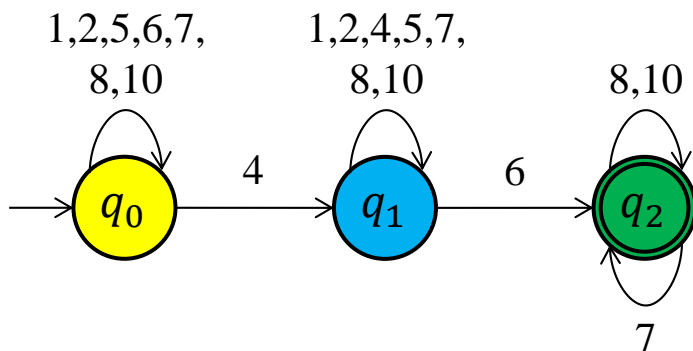
Automaton-Guided Re

Witness of
Unsatisfiability

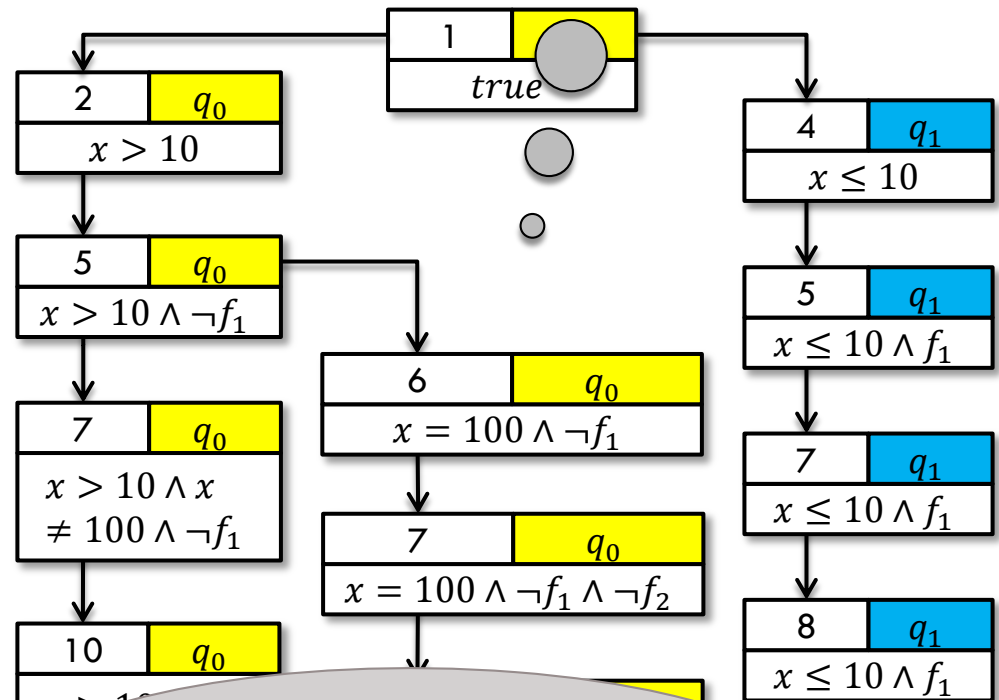
Program

```
1 if (x > 10)
2   f1 = false;
3 else
4   f1 = true;
5 if (x == 100)
6   f2 = false;
7 ...
```

Automaton



Abstract Reachability



No abstract state
labeled with q_2 !



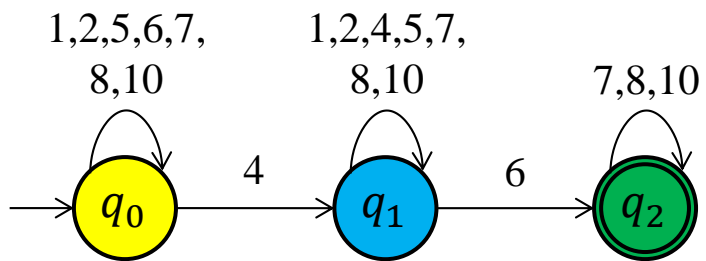
Information Reuse

Reuse Information for Shared Parts



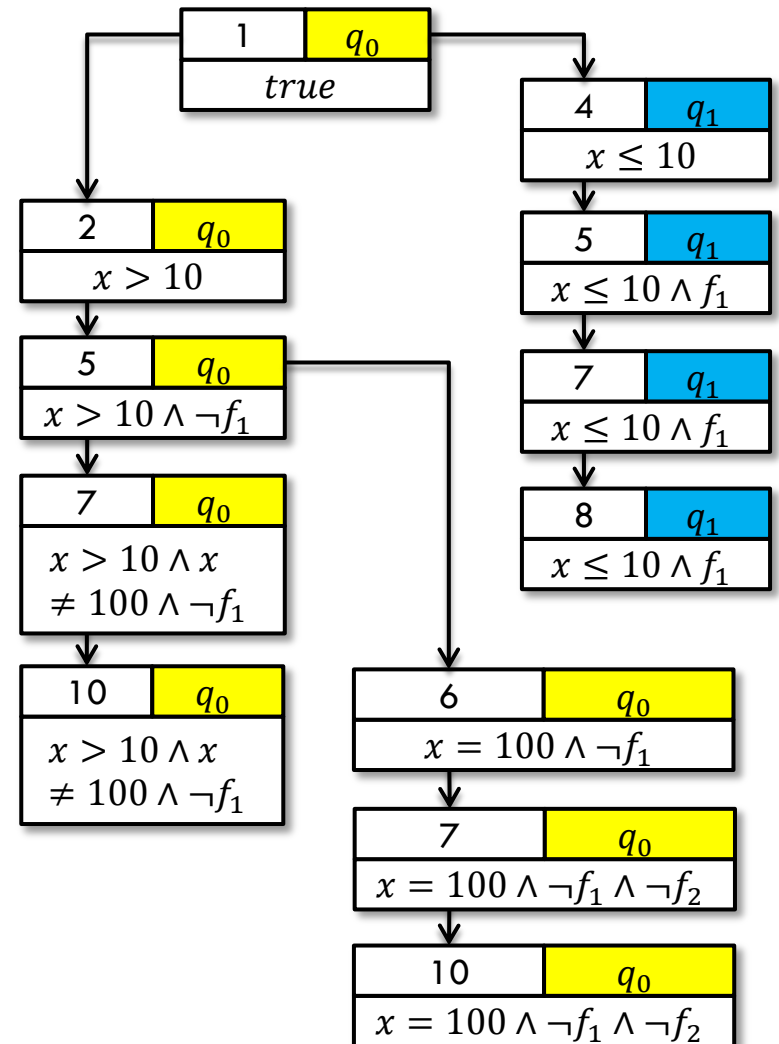
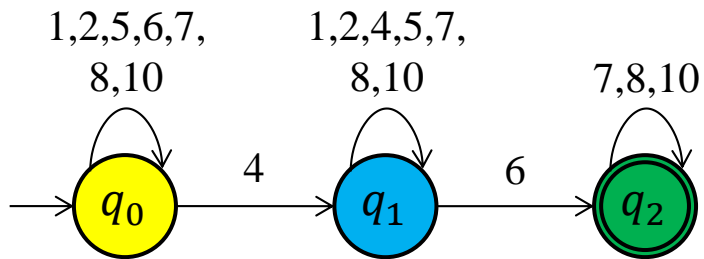
Reuse Information for Shared Parts

Automaton A



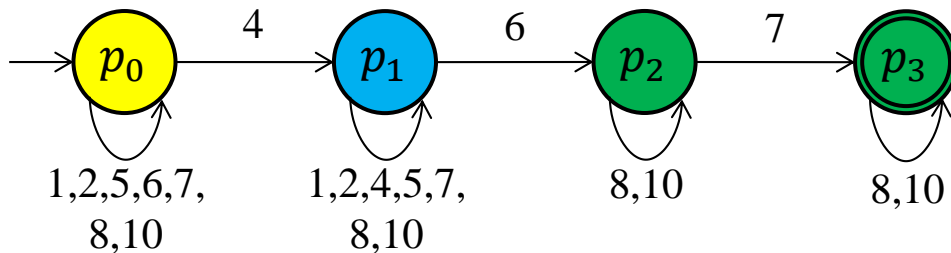
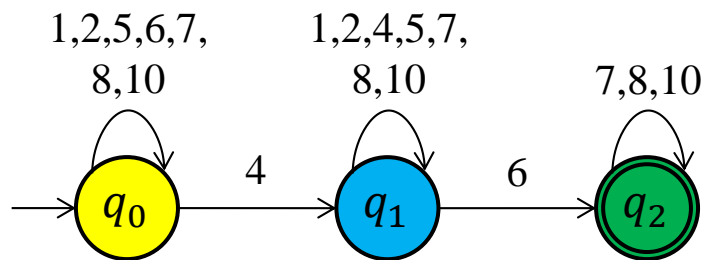
Reuse Information for Shared Parts

Automaton A

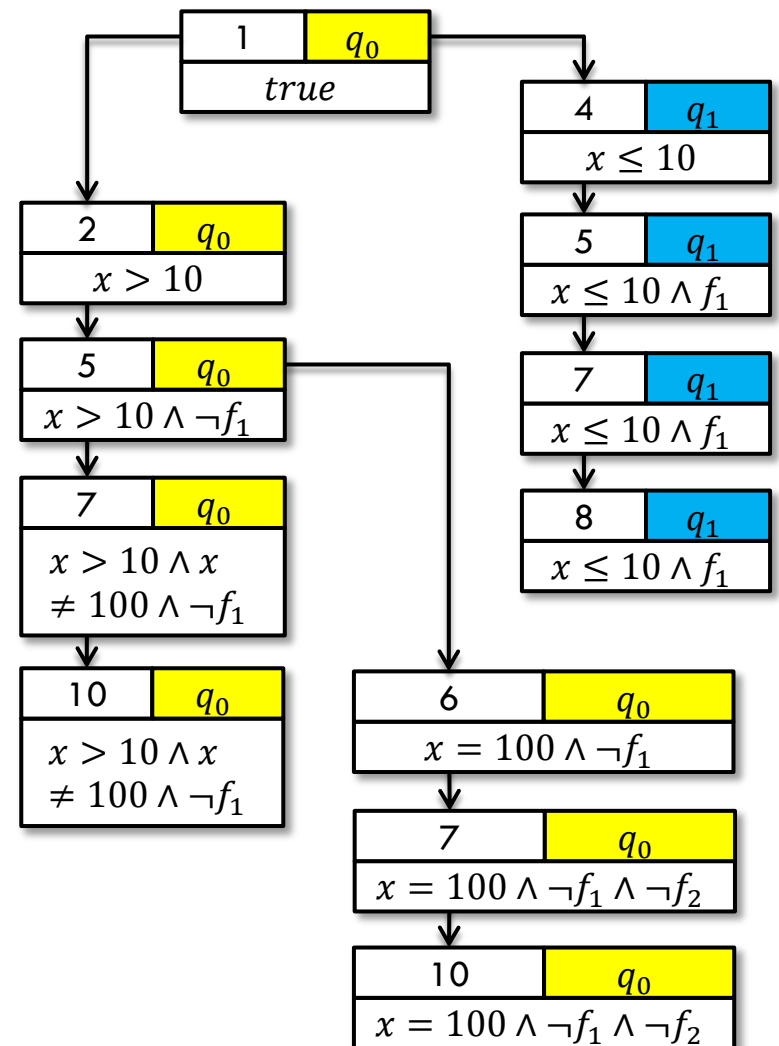


Reuse Information for Shared Parts

Automaton A

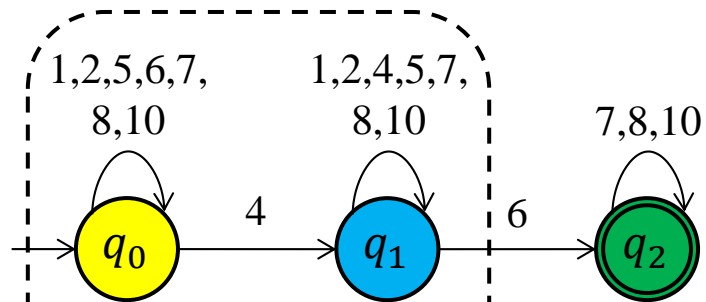


Automaton B

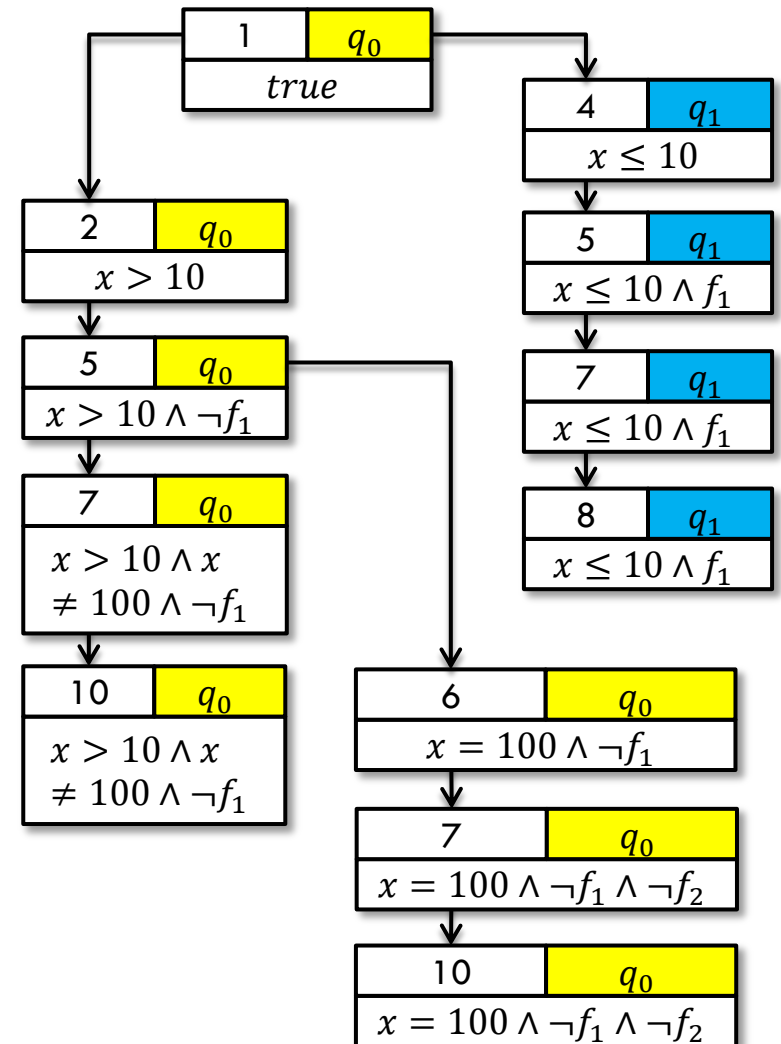
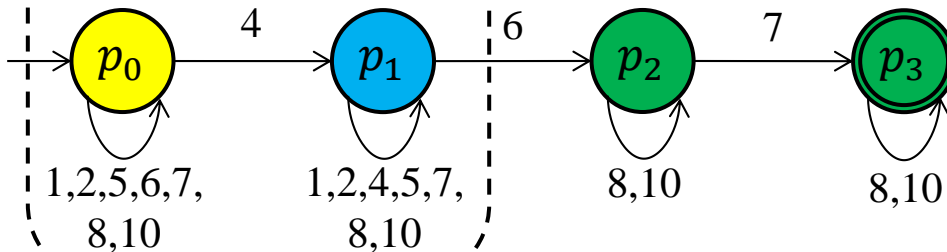


Reuse Information for Shared Parts

Automaton A

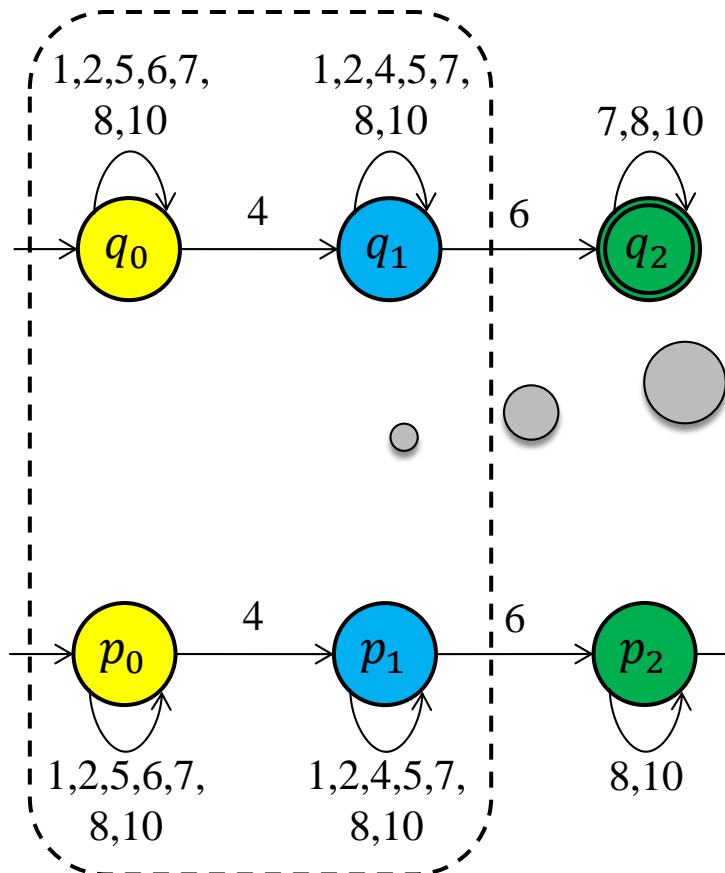


Automaton B

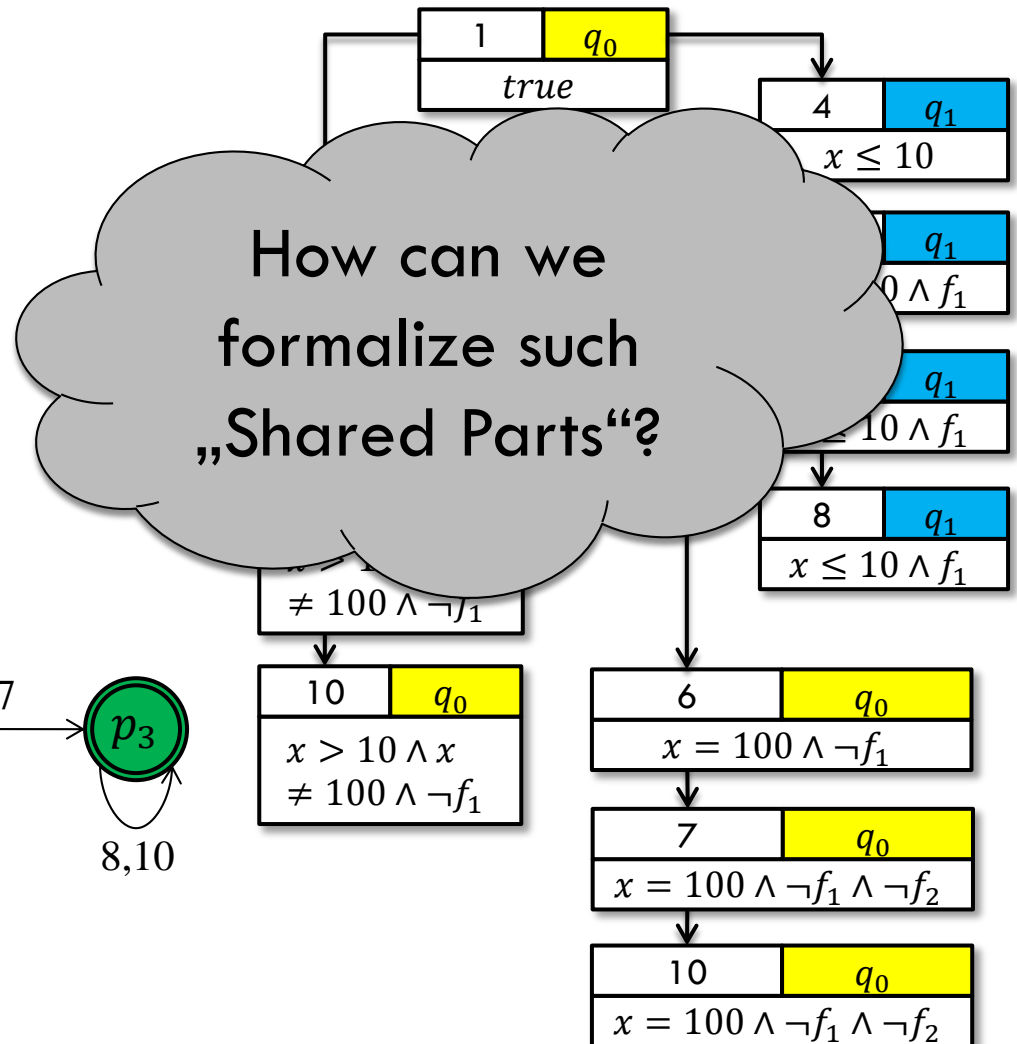
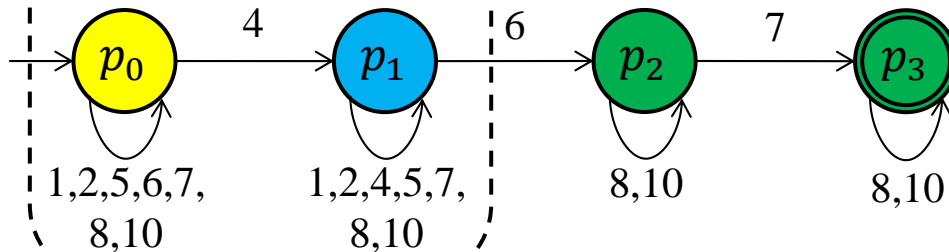


Reuse Information for Shared Parts

Automaton A

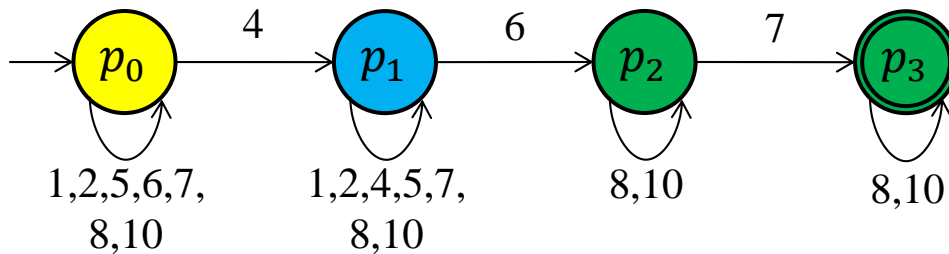
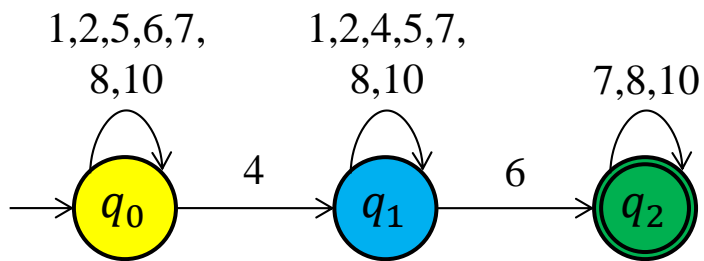


Automaton B



Shared Parts: Simulation Relation

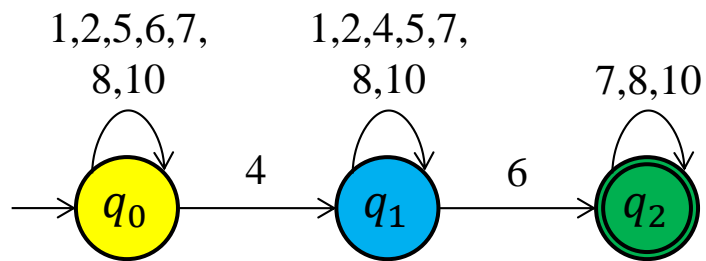
Automaton A



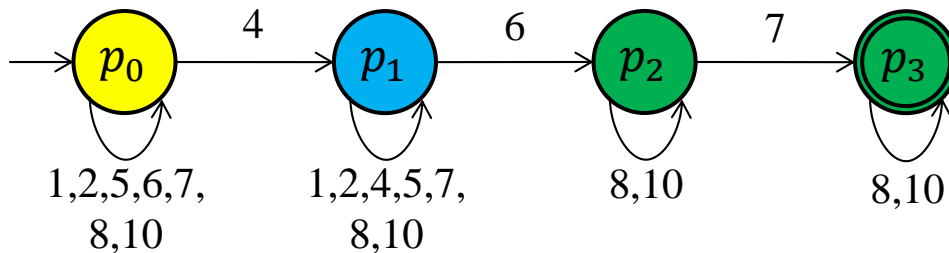
Automaton B

Shared Parts: Simulation Relation

Automaton A



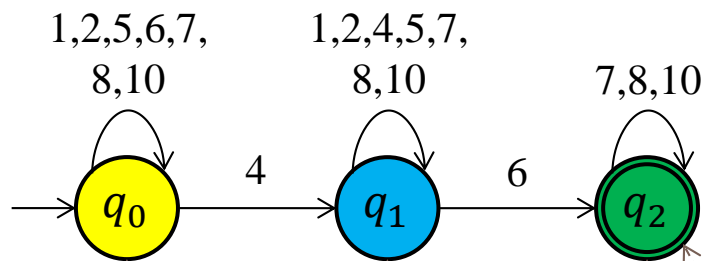
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:



Automaton B

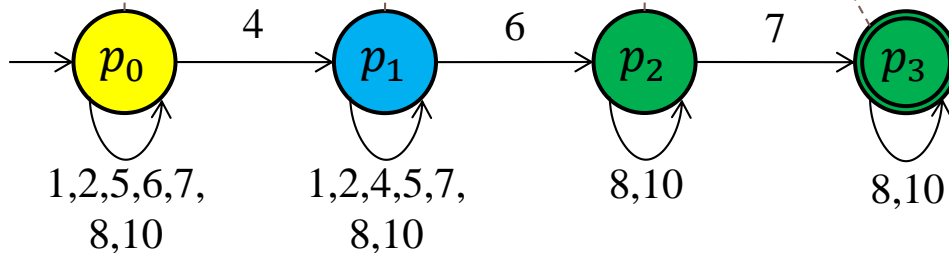
Shared Parts: Simulation Relation

Automaton A



A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

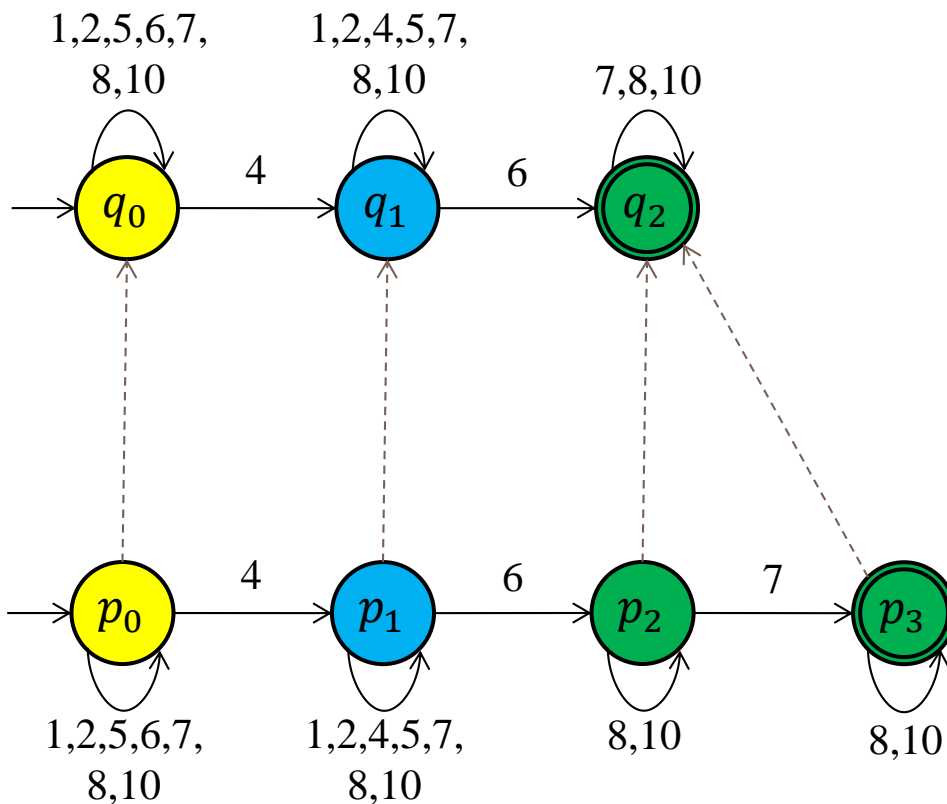
H



Automaton B

Shared Parts: Simulation Relation

Automaton A



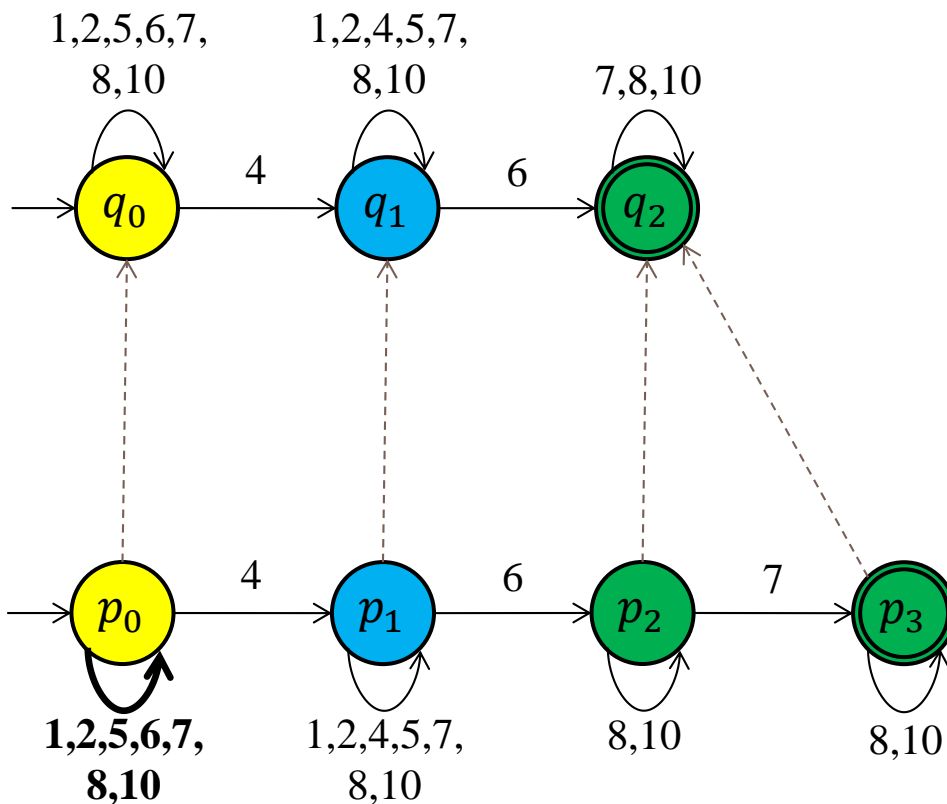
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



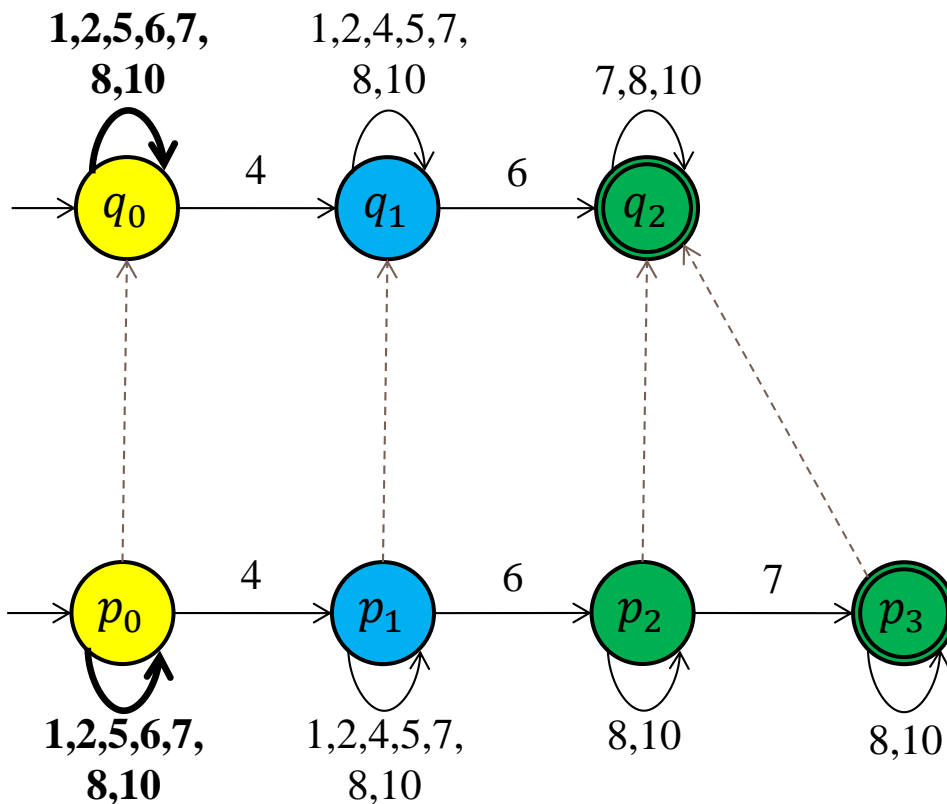
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



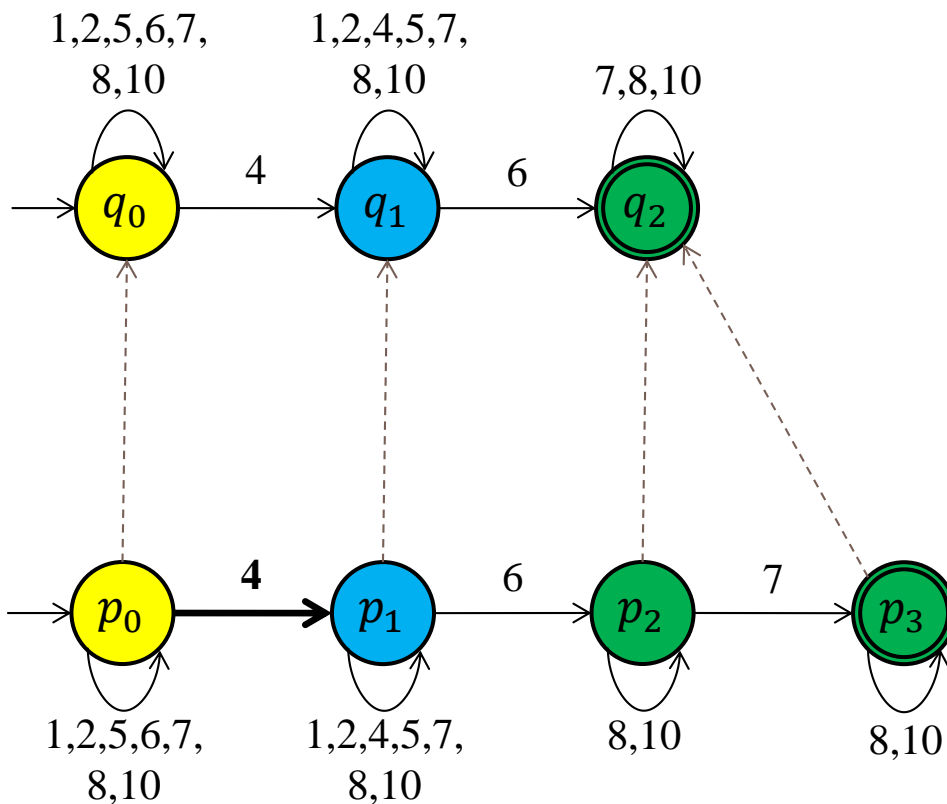
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



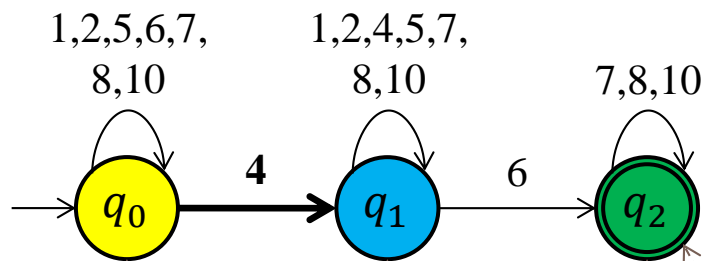
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

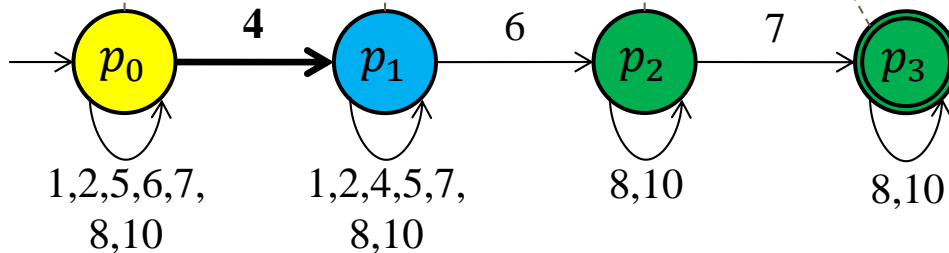
For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



H



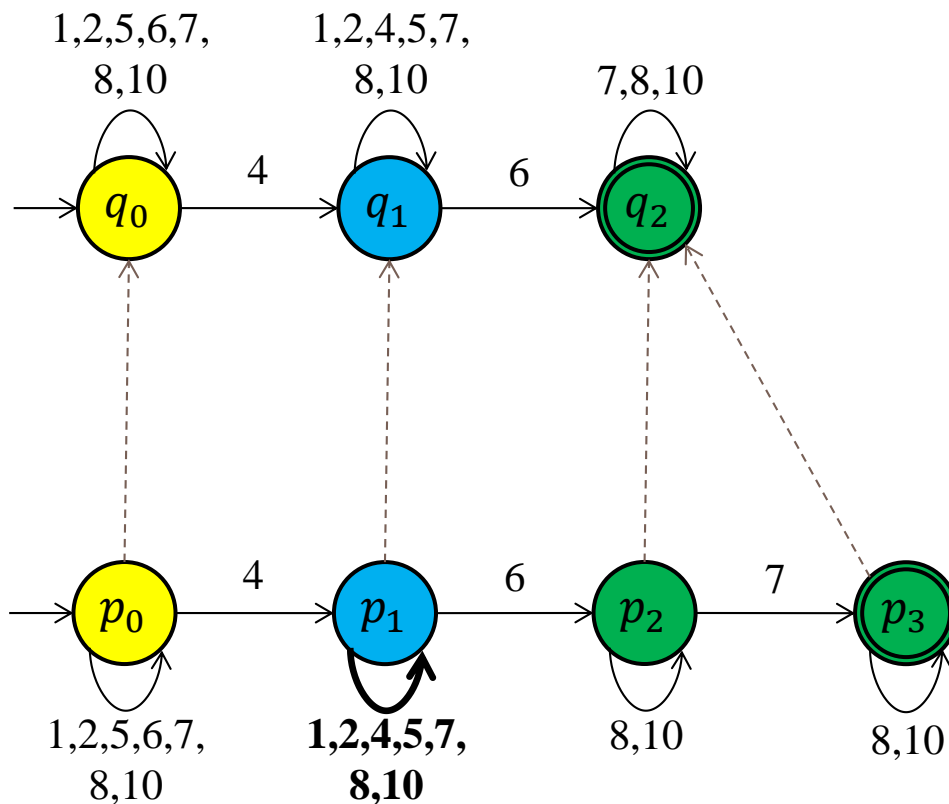
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



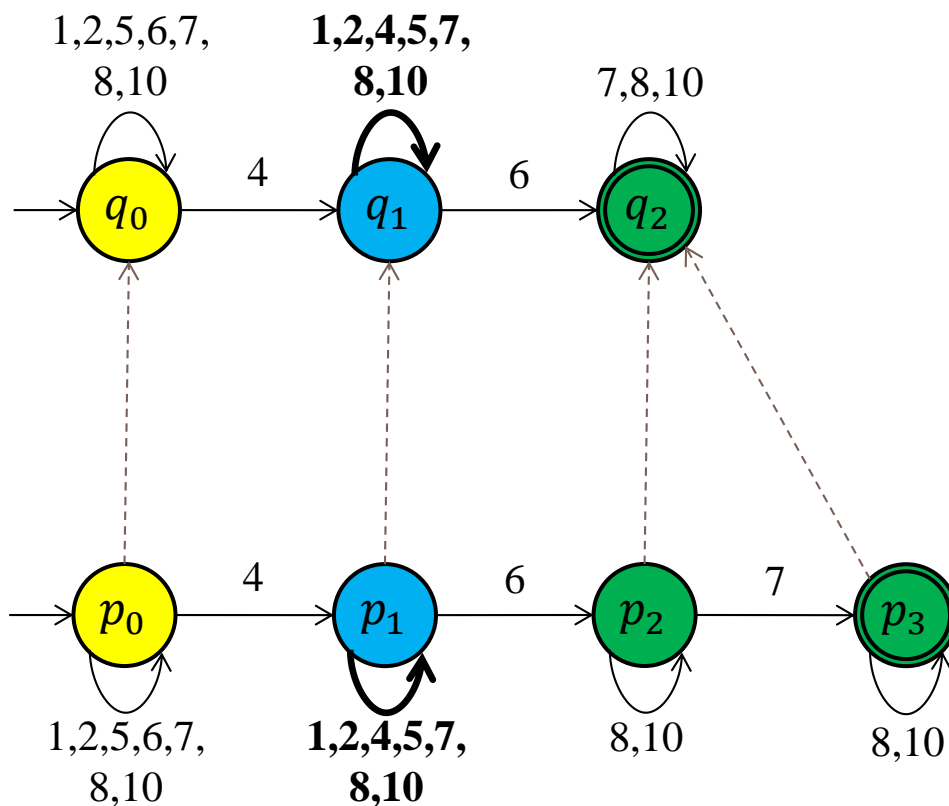
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



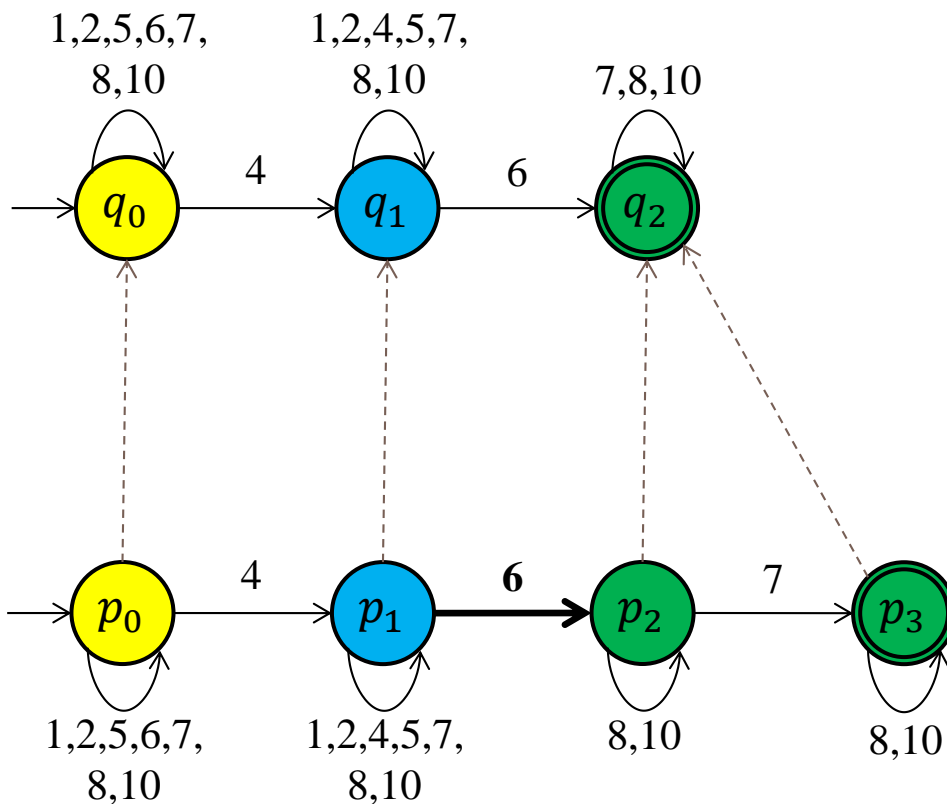
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



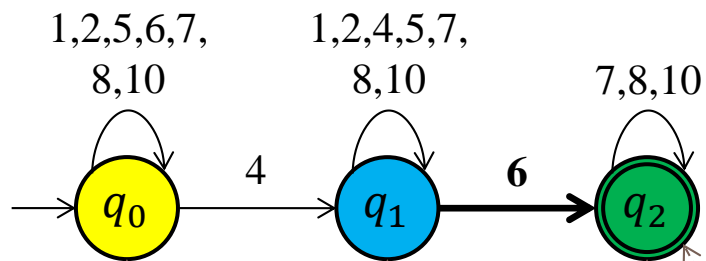
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

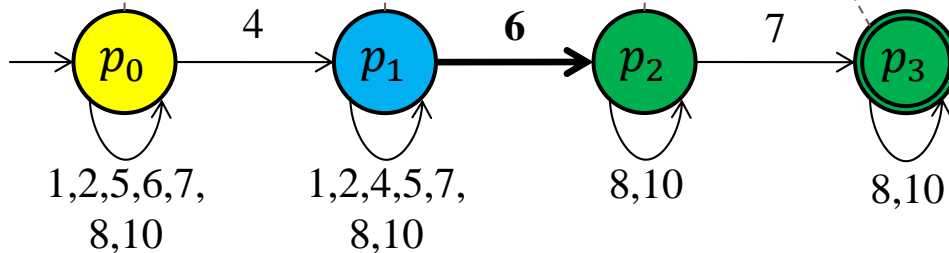
For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



H



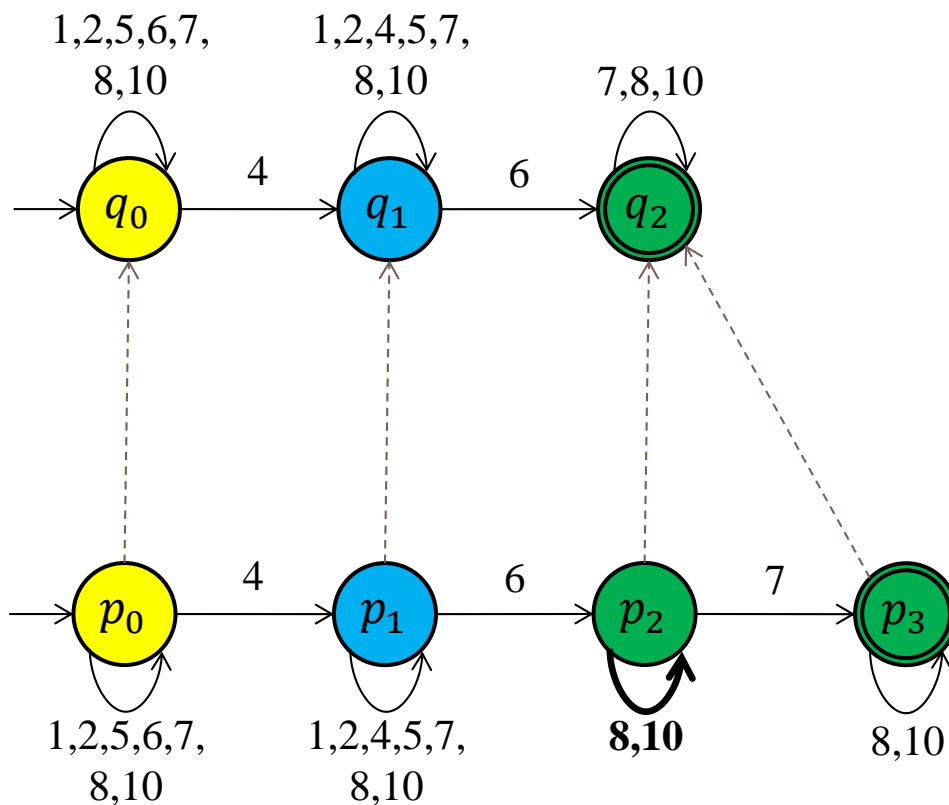
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



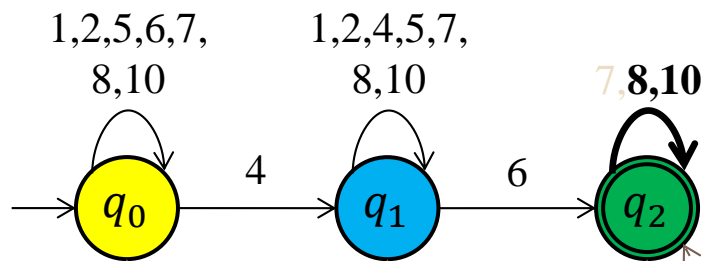
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

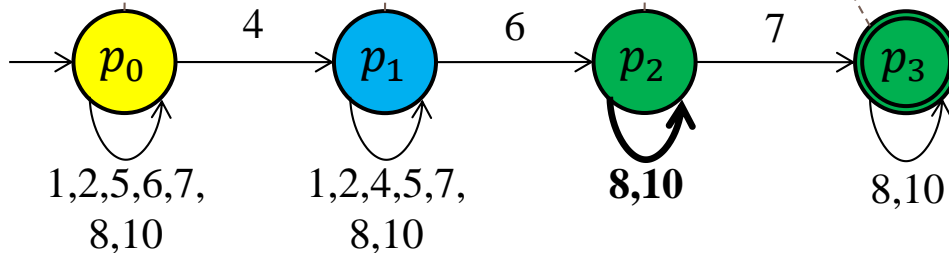
Automaton B

Shared Parts: Simulation Relation

Automaton A



H



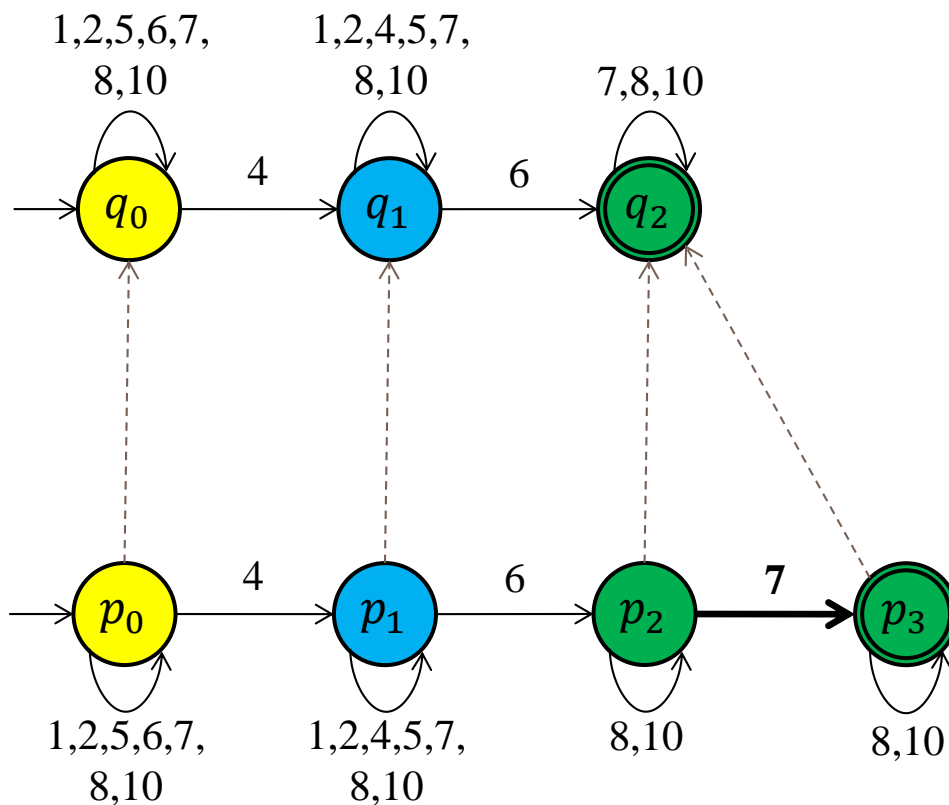
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



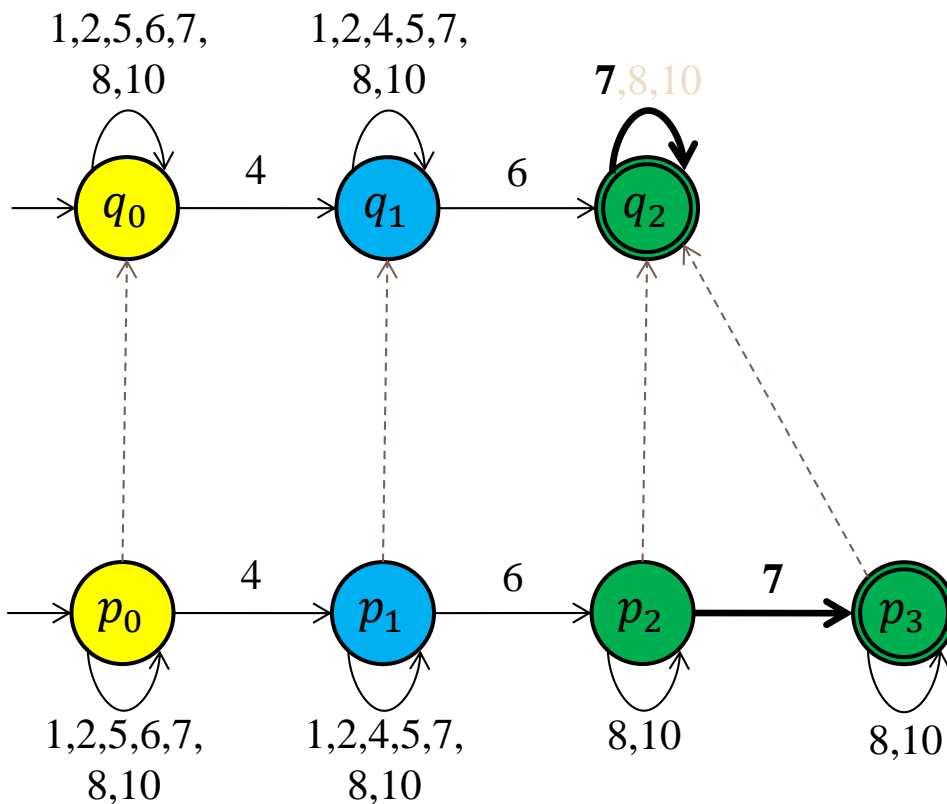
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



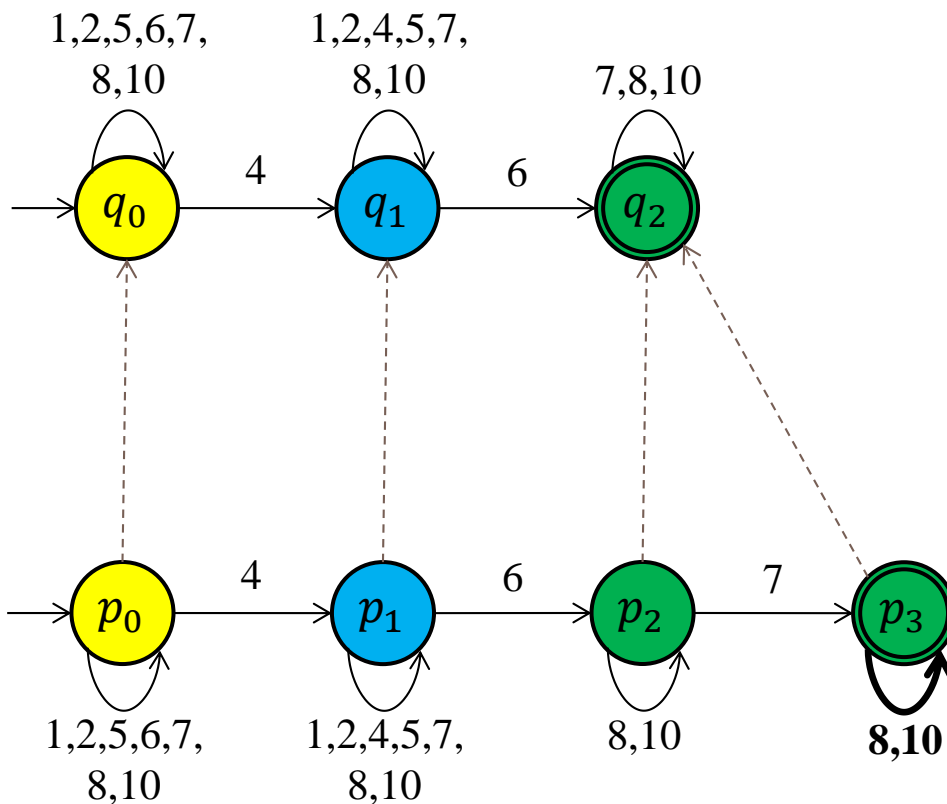
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



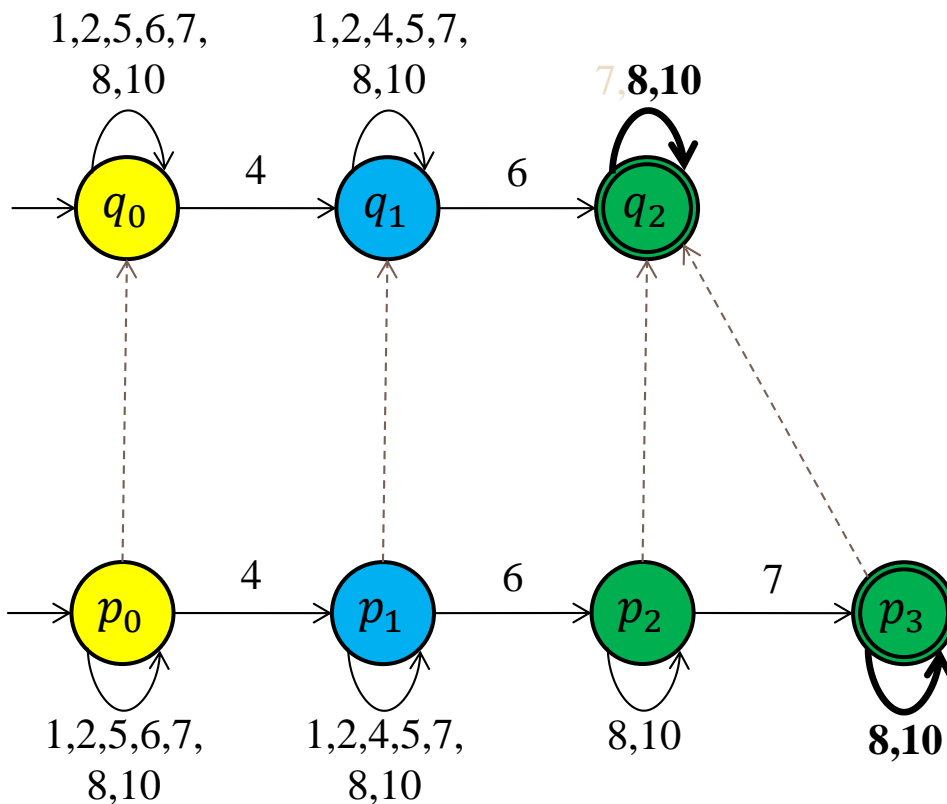
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



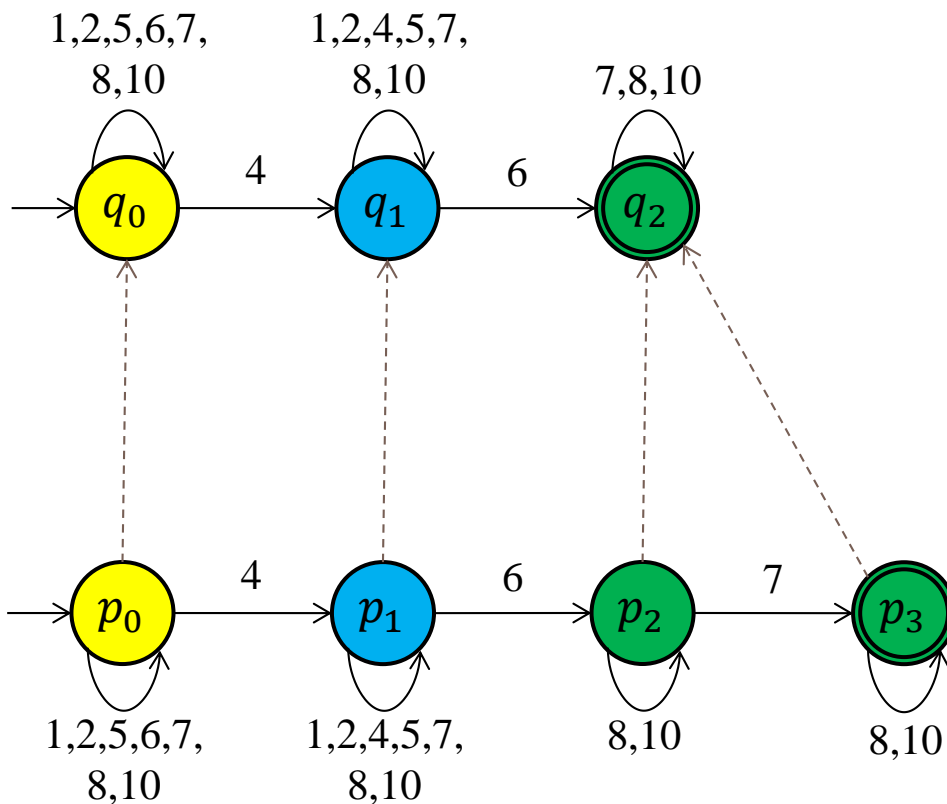
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Automaton B

Shared Parts: Simulation Relation

Automaton A



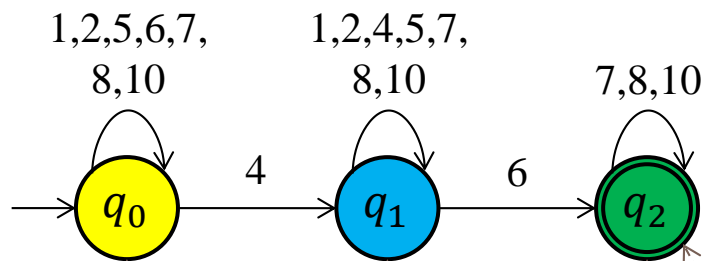
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

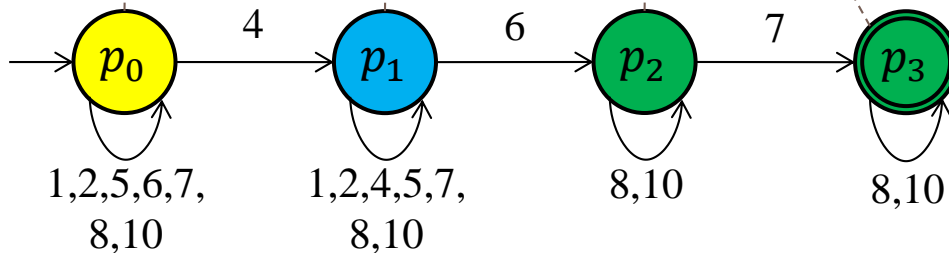
For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



H



Automaton B

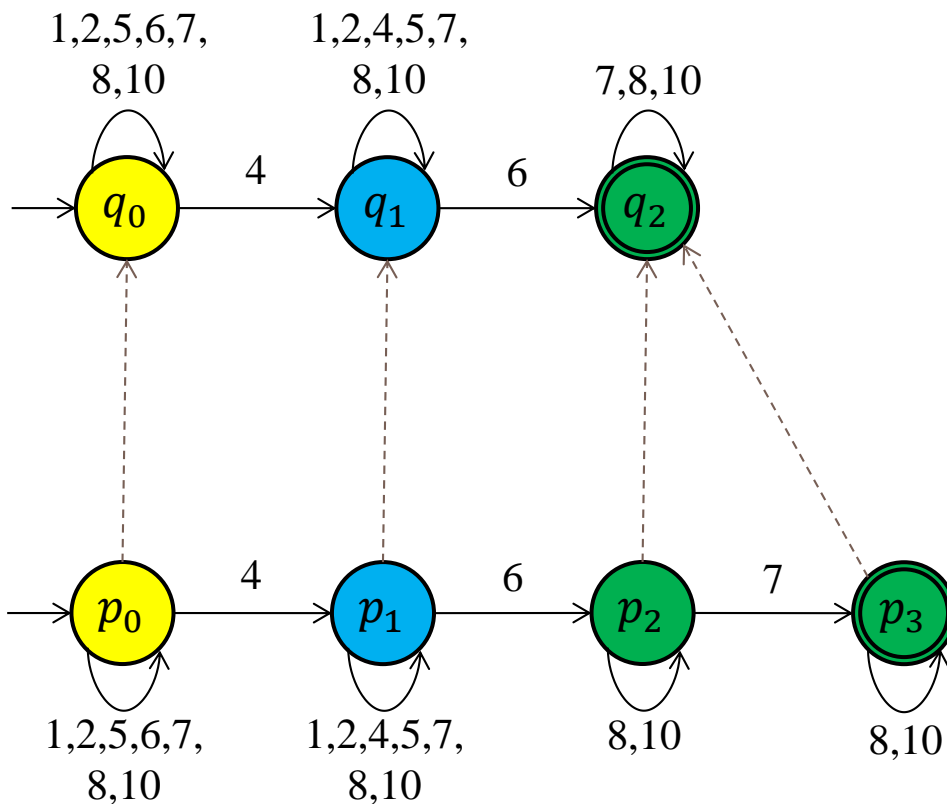
A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

For each transition

We do not distinguish final (initial) states from non-final (non-initial) states!

Shared Parts: Simulation Relation

Automaton A



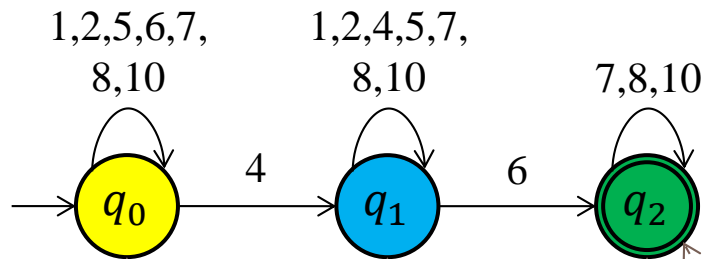
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

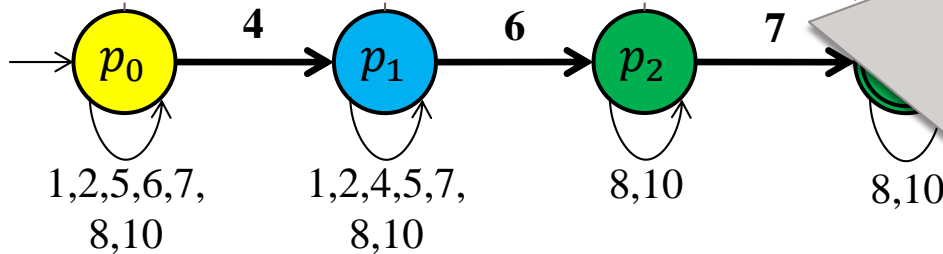
For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Shared Parts: Simulation Relation

Automaton A



H



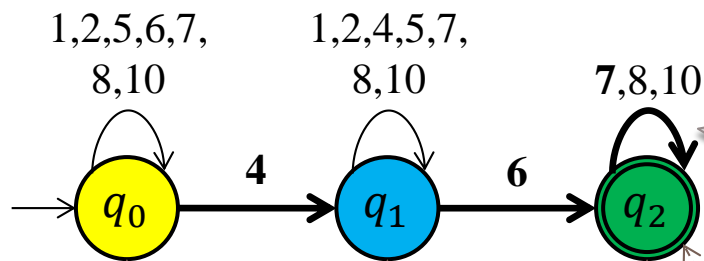
Automaton B

For $(p, q) \in H$:

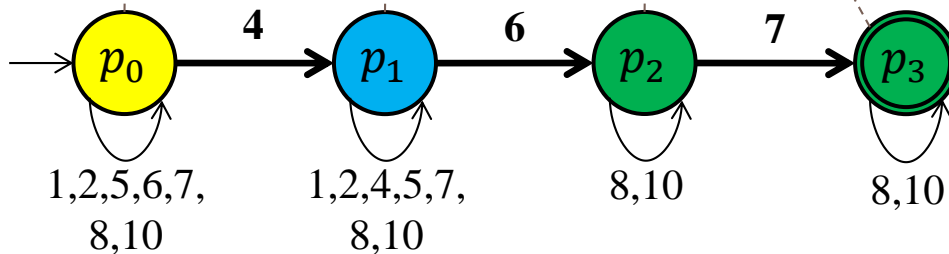
For each
transition sequence
starting from p

Shared Parts: Simulation Relation

Automaton A



H



Automaton B

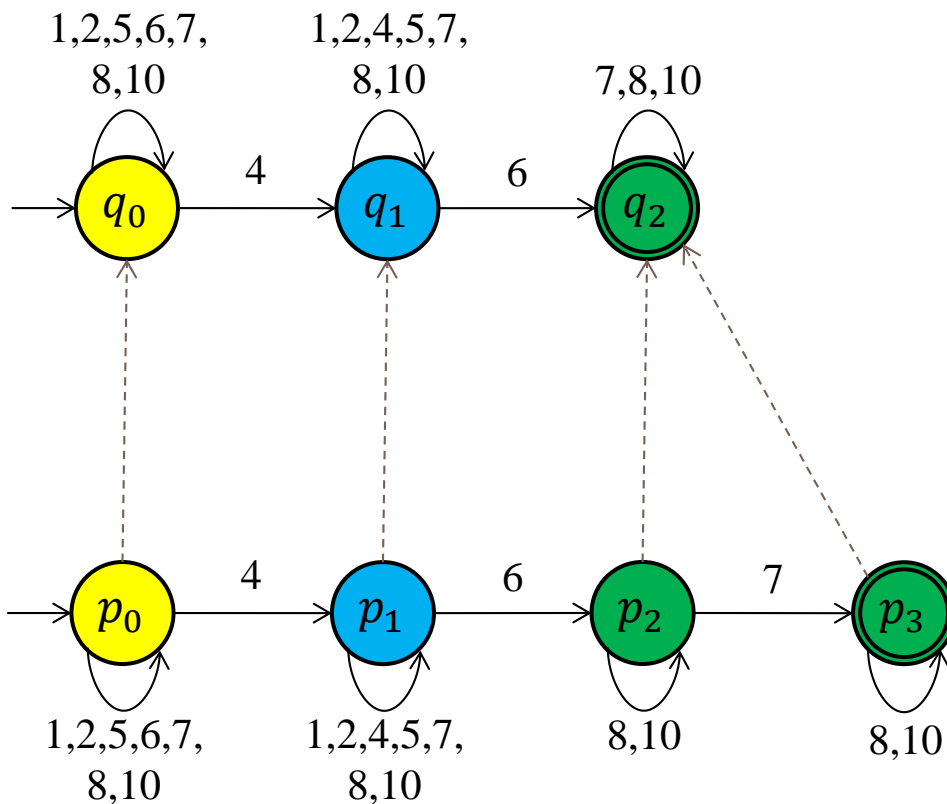
For $(p, q) \in H$:

For each
transition sequence
starting from p

there is a corresponding
transition sequence
starting in q

Shared Parts: Simulation Relation

Automaton A



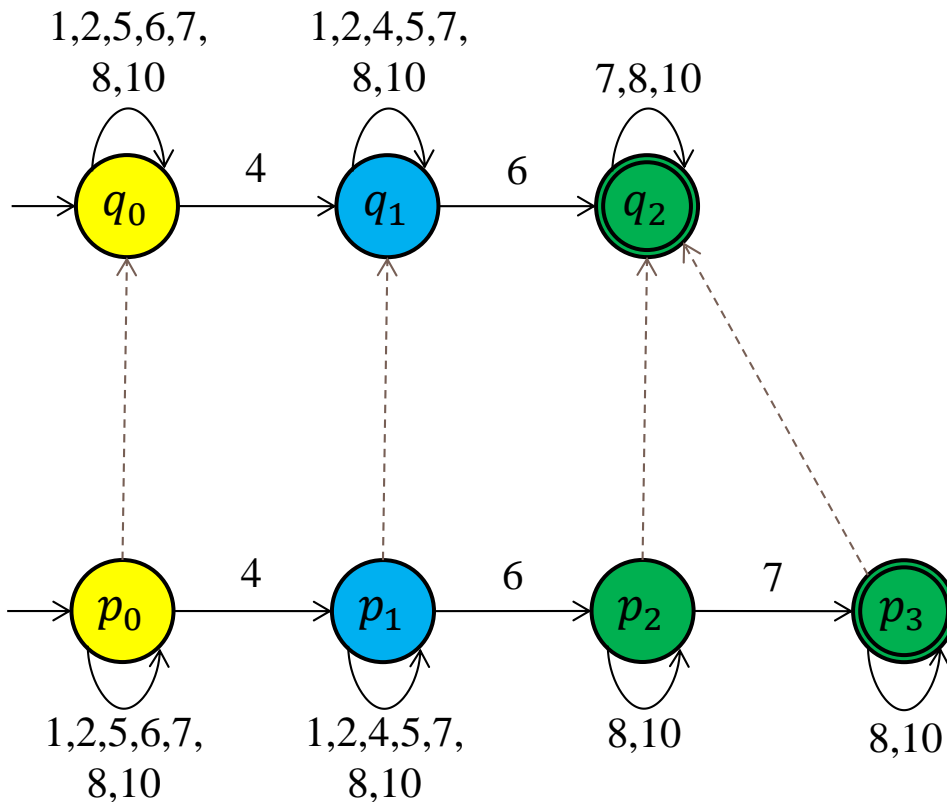
Automaton B

A simulation relation H associates states of B with states of A s.t. for $(p, q) \in H$ holds:

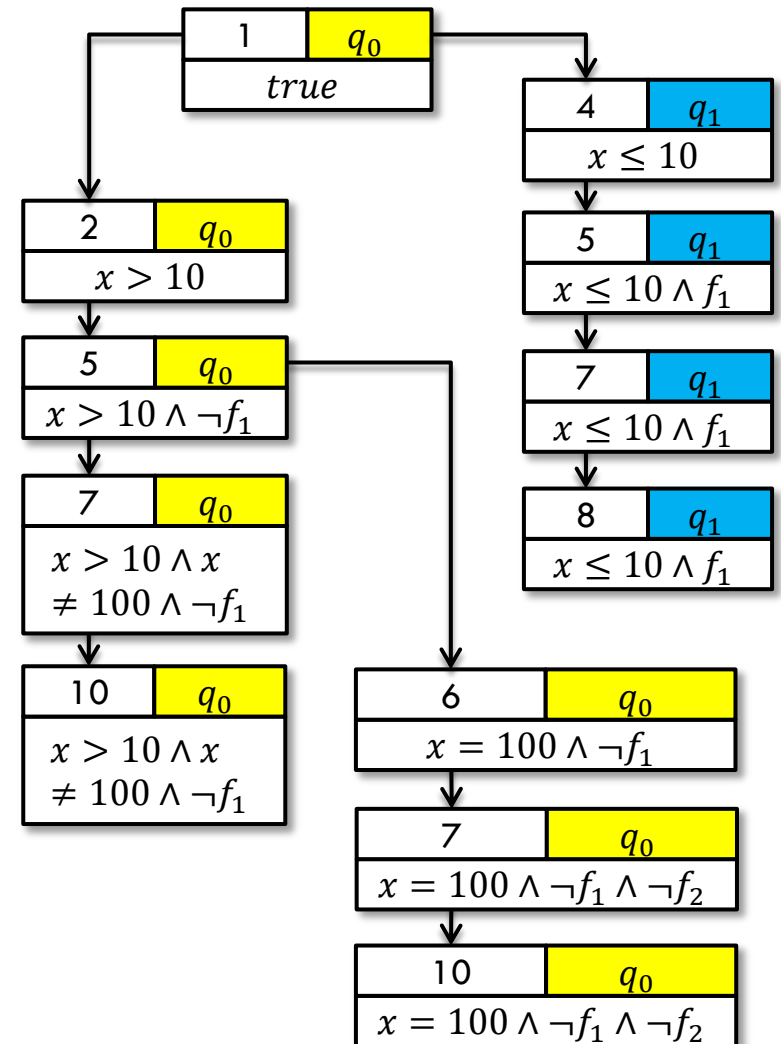
For each transition (p, a, p') in B there is a transition (q, a, q') in A such that $(p', q') \in H$

Reuse Information for Shared Parts

Automaton A

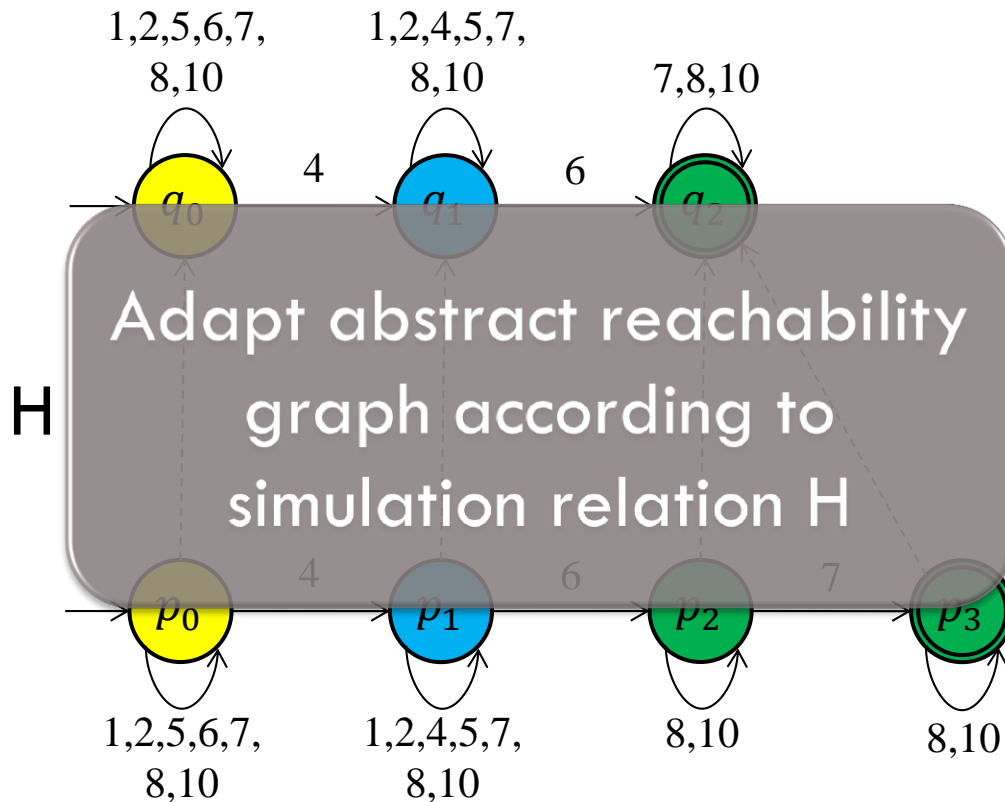


Automaton B

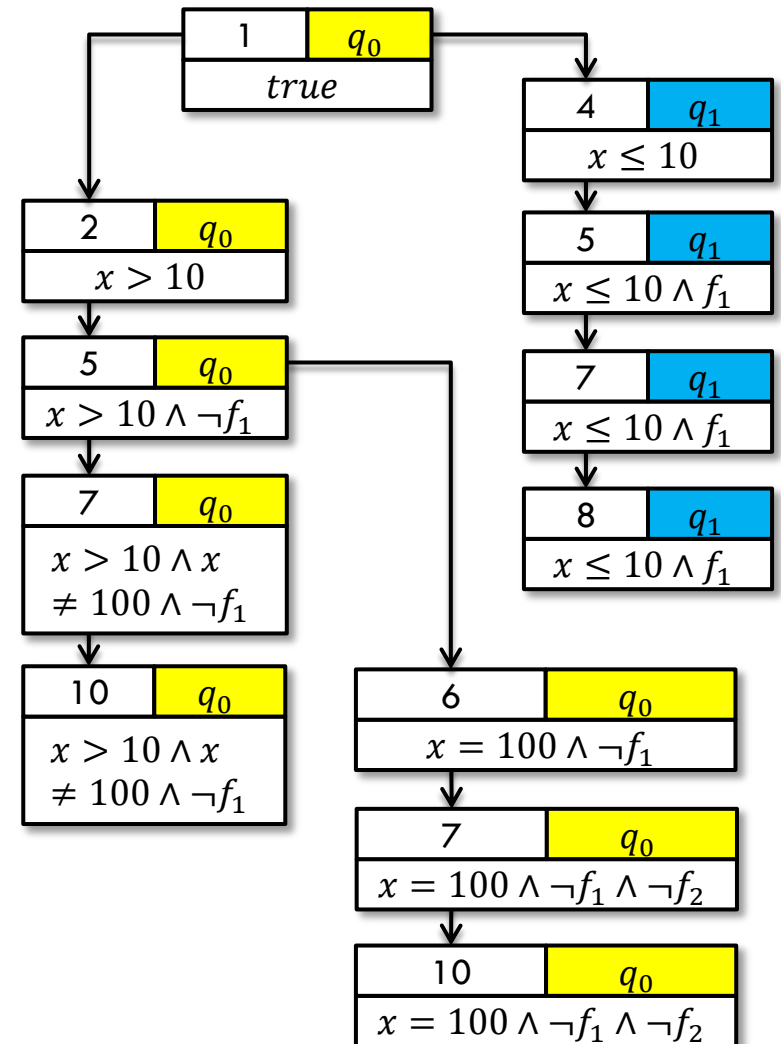


Reuse Information for Shared Parts

Automaton A

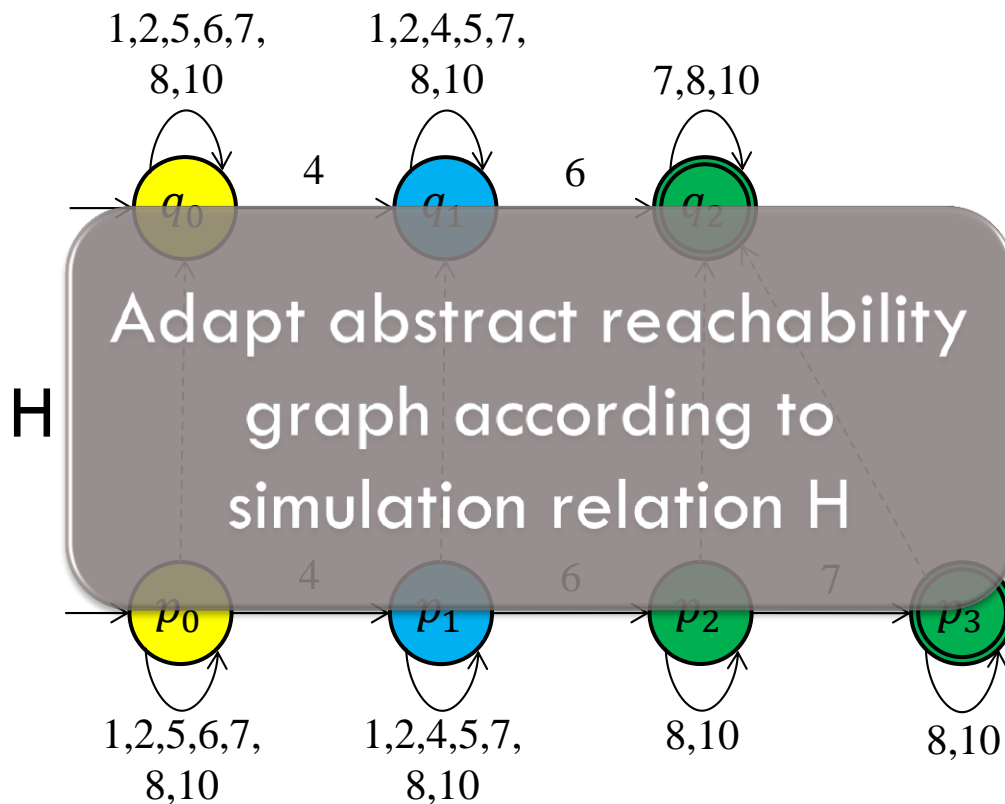


Automaton B

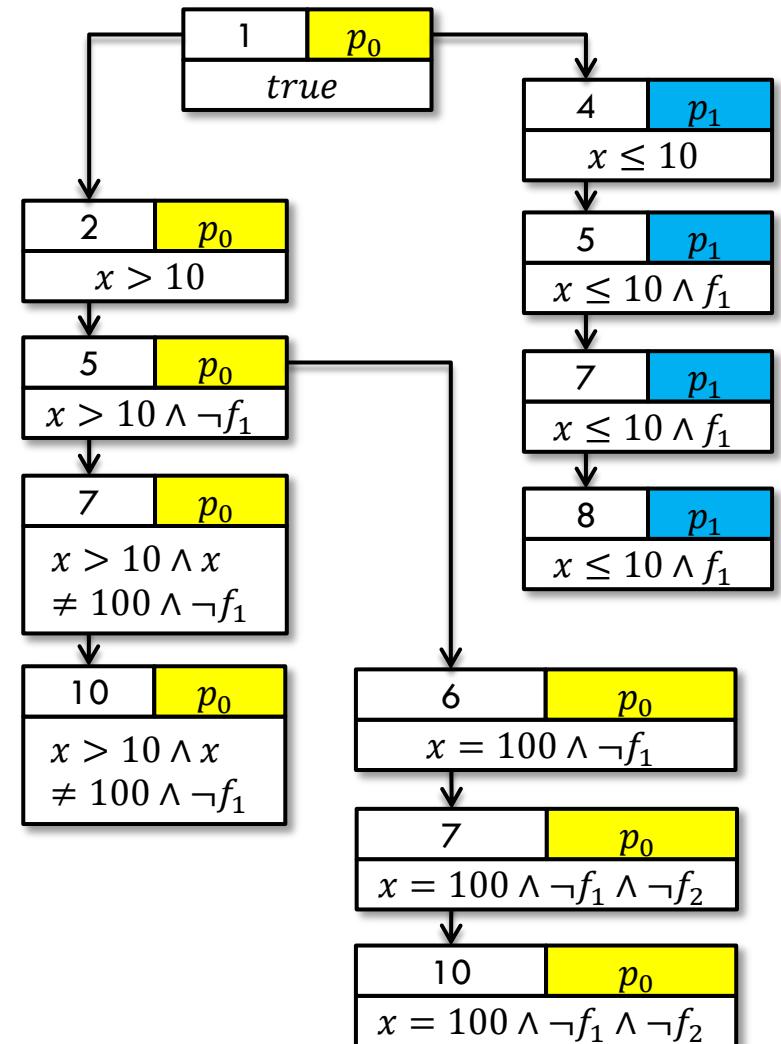


Reuse Information for Shared Parts

Automaton A

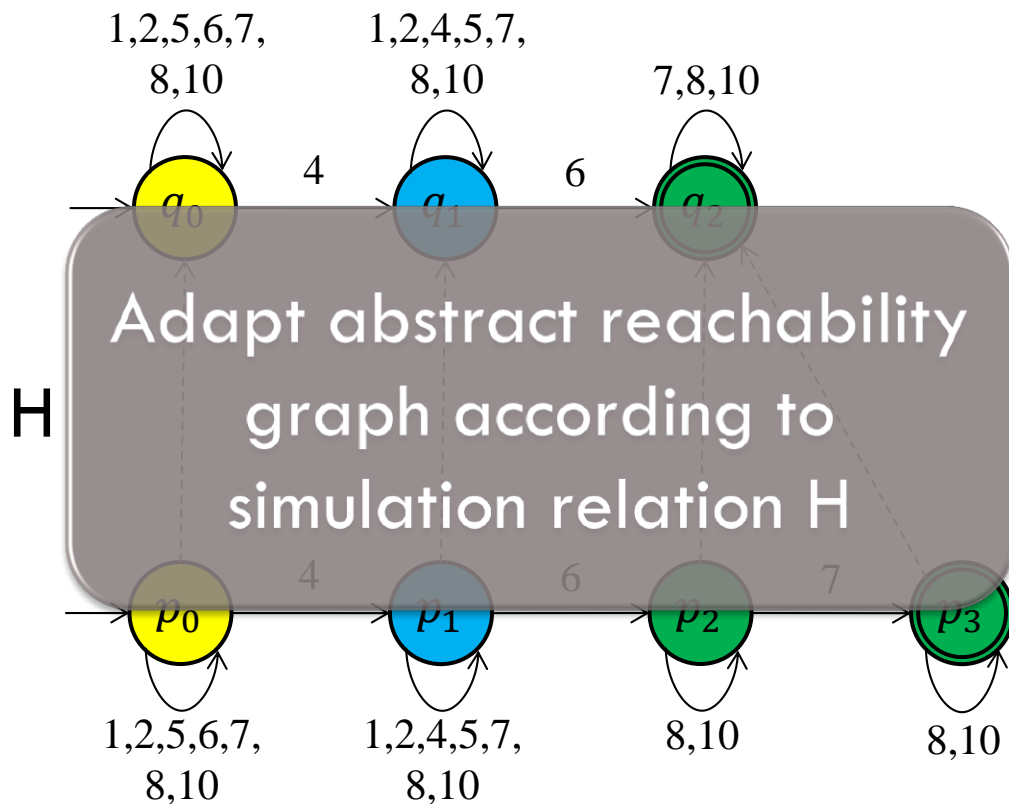


Automaton B

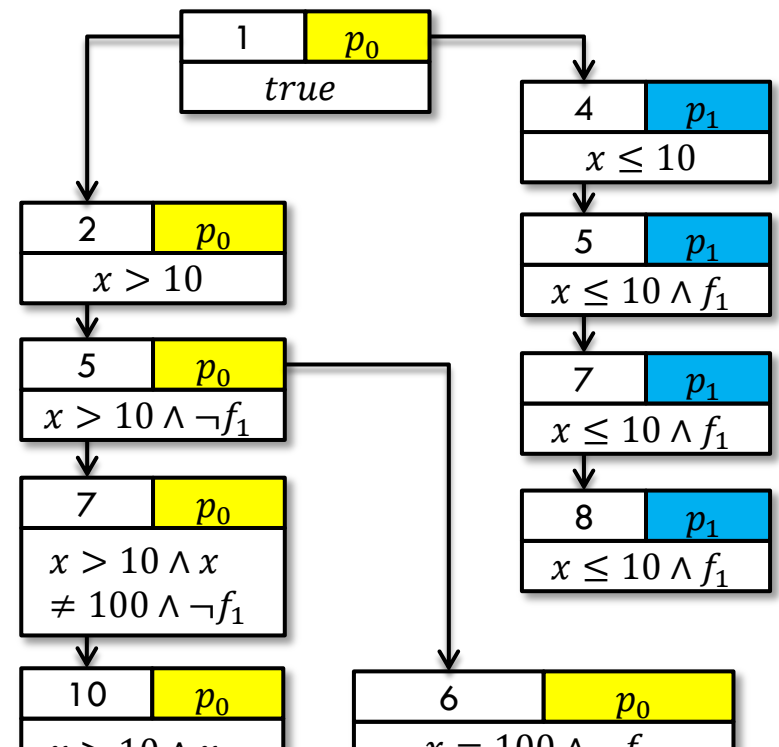


Reuse Information for Shared Parts

Automaton A



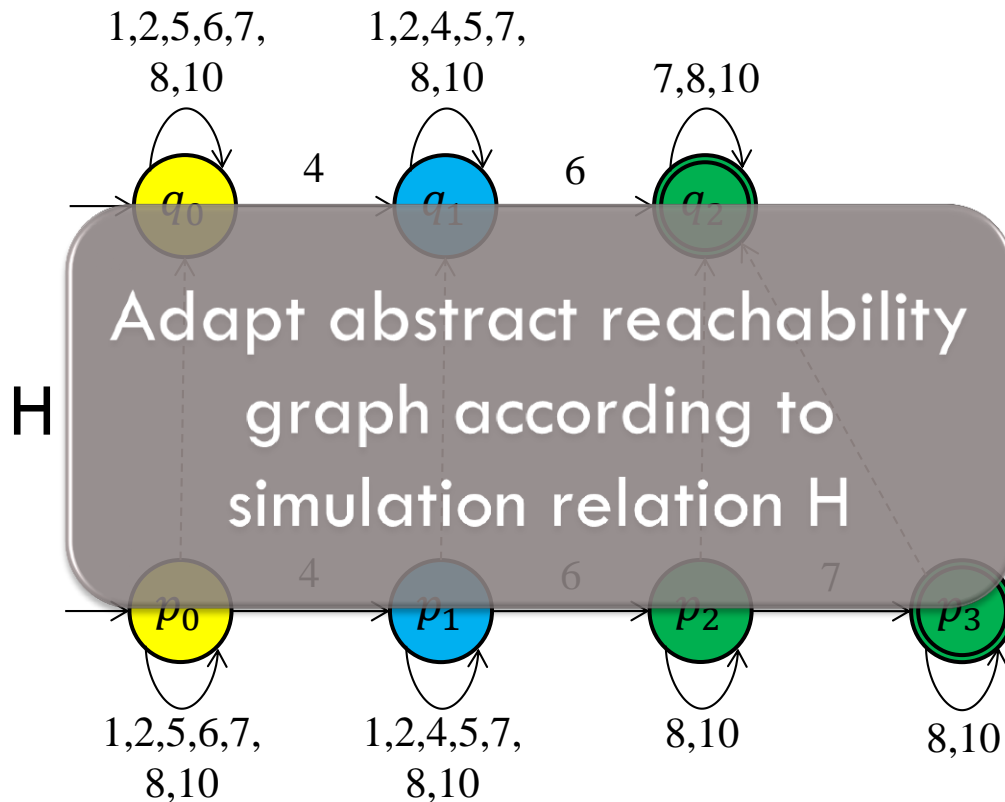
Automaton B



There is no abstract state labeled with p_3 !

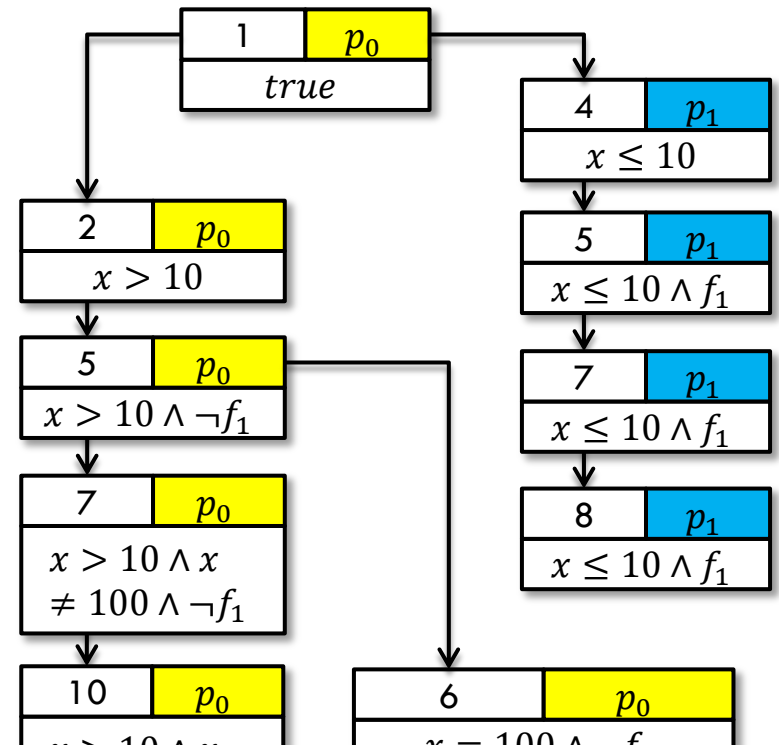
Reuse Information for Shared Parts

Automaton A



Automaton B

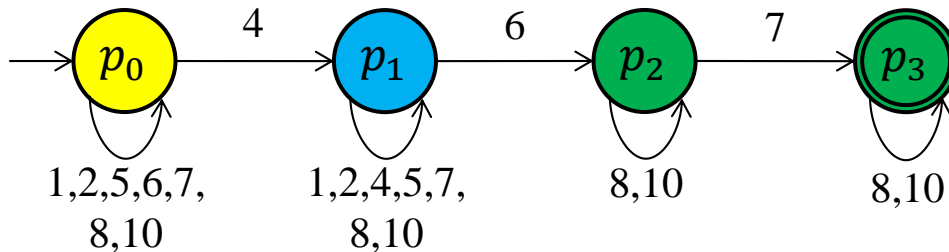
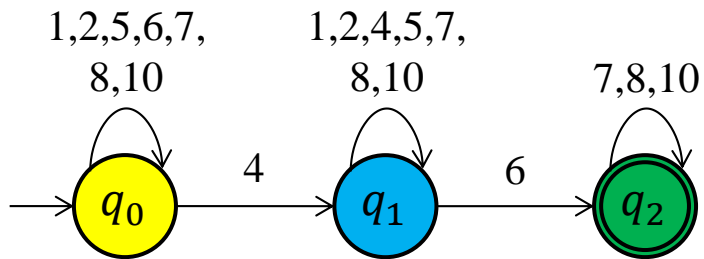
Unsatisfiable!



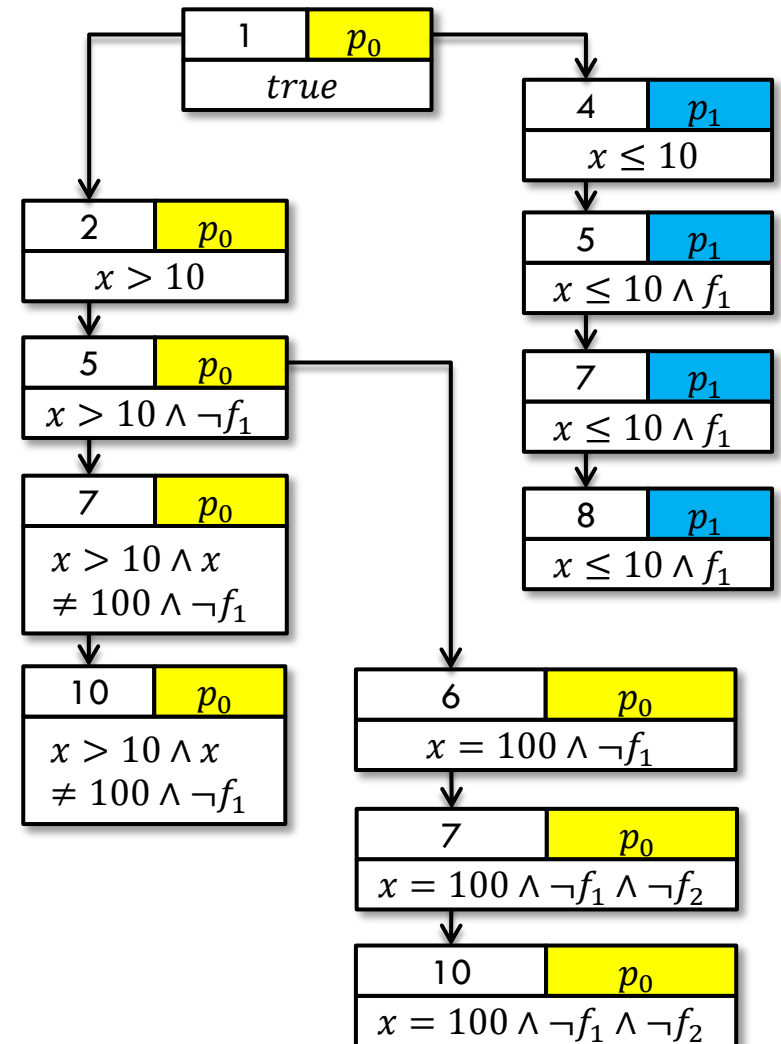
There is no abstract state labeled with p_3 !

Reuse Information for Shared Parts

Automaton A

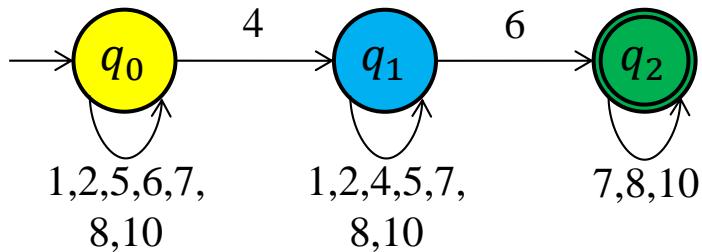
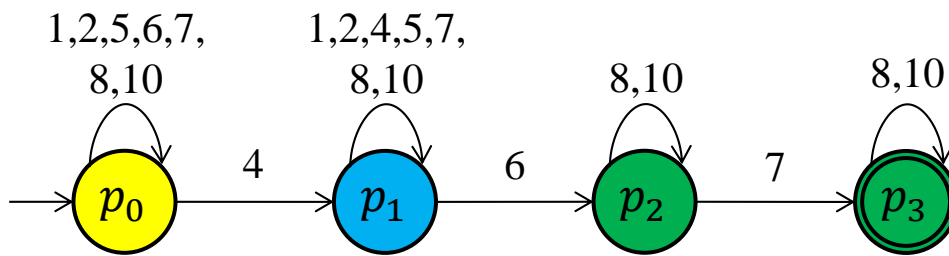


Automaton B

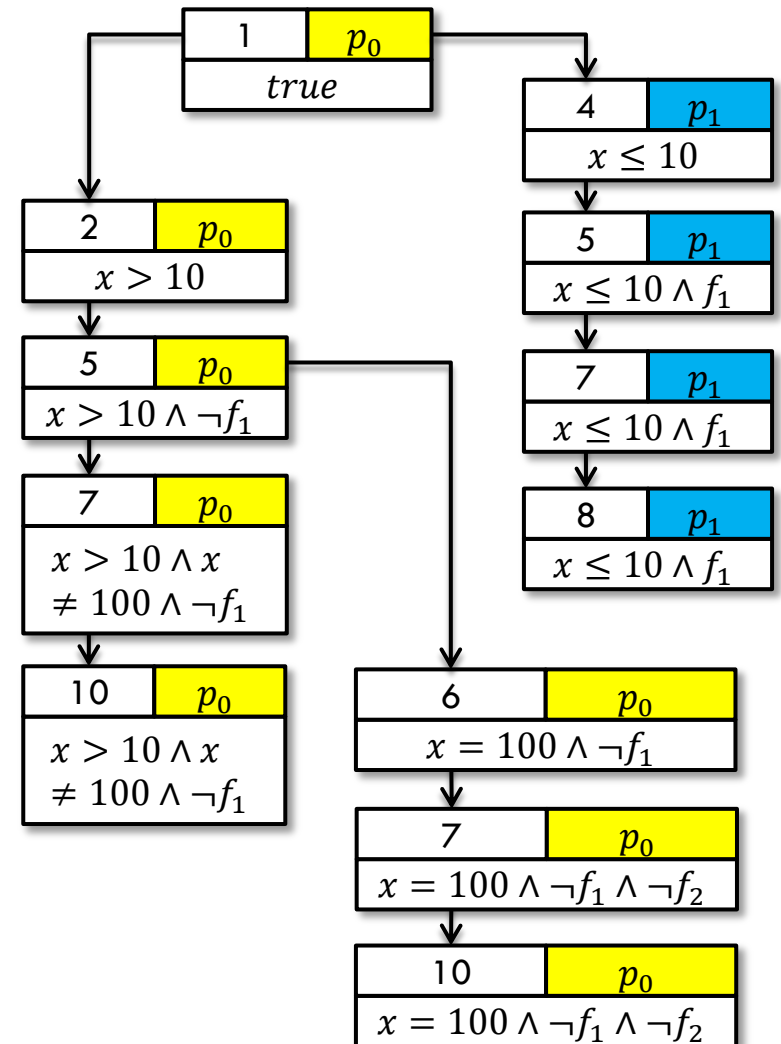


Reuse Information for Shared Parts

Automaton B

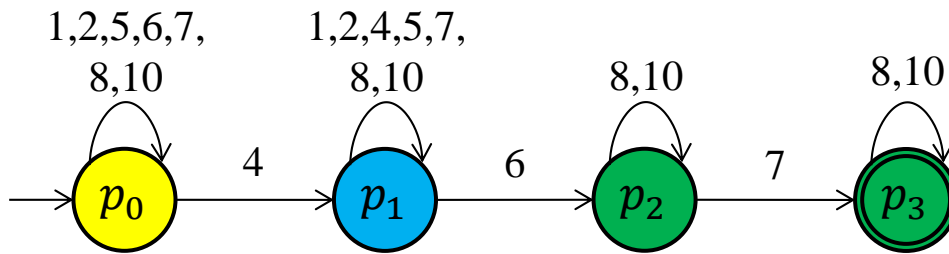


Automaton A

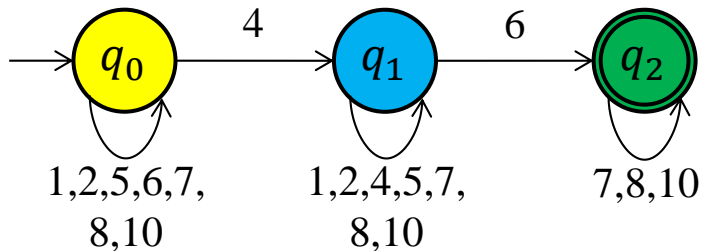


Reuse Information for Shared Parts

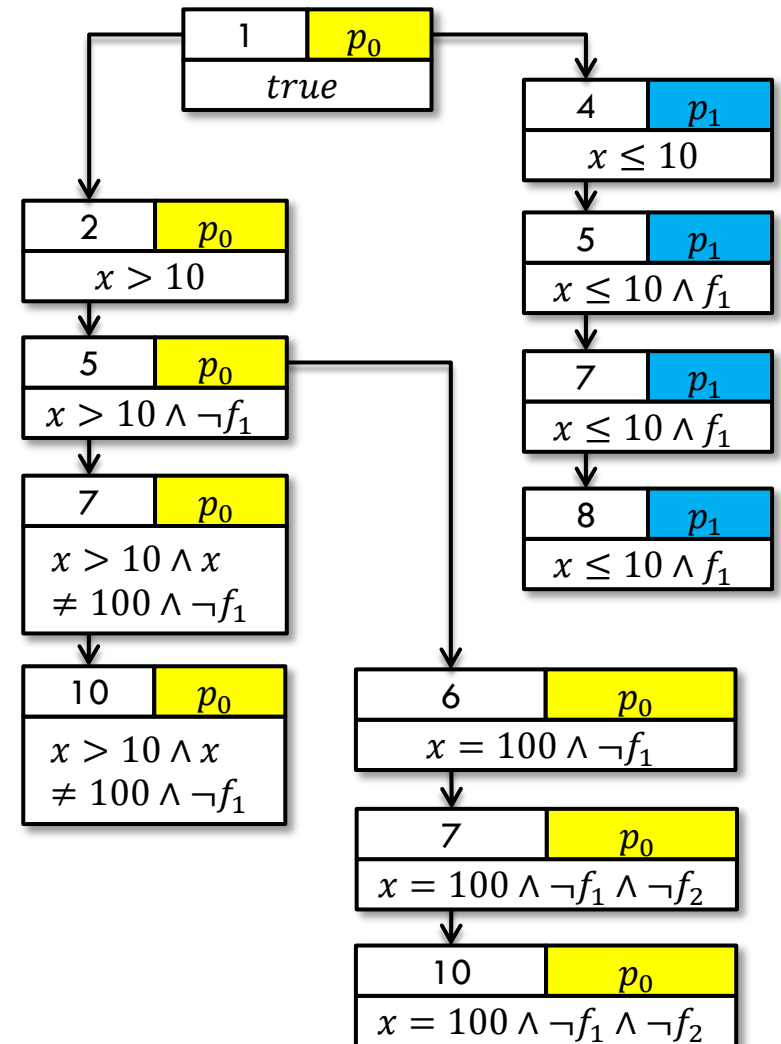
Automaton B



$$H = \emptyset$$

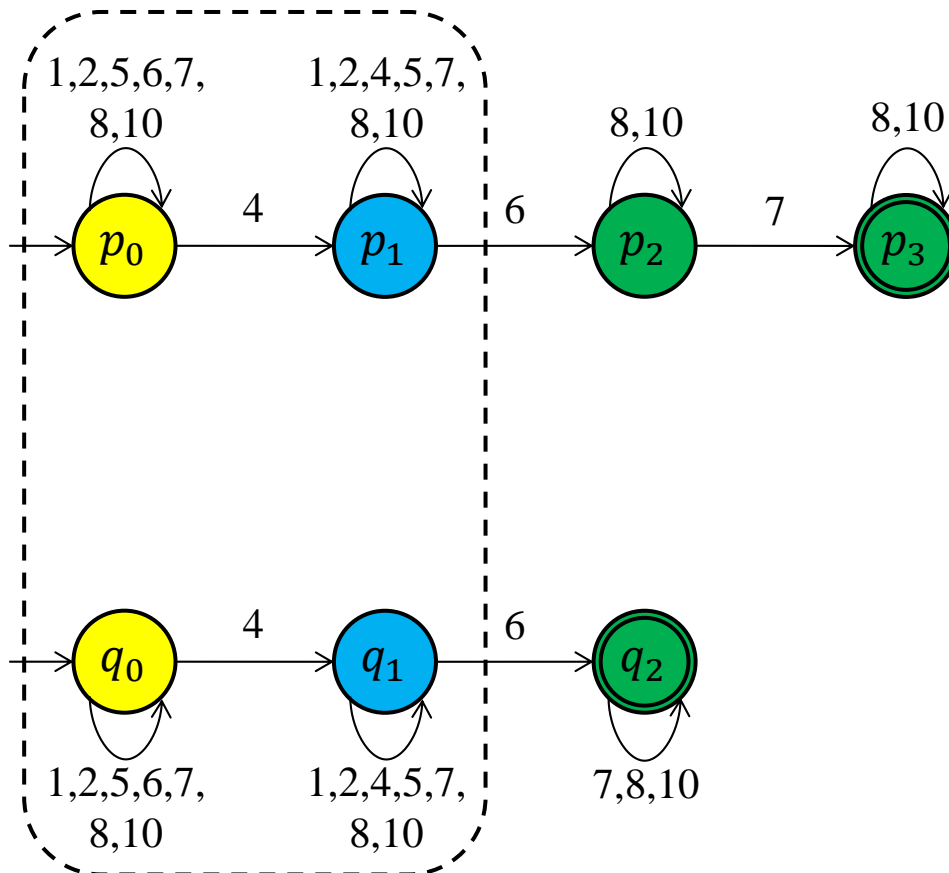


Automaton A

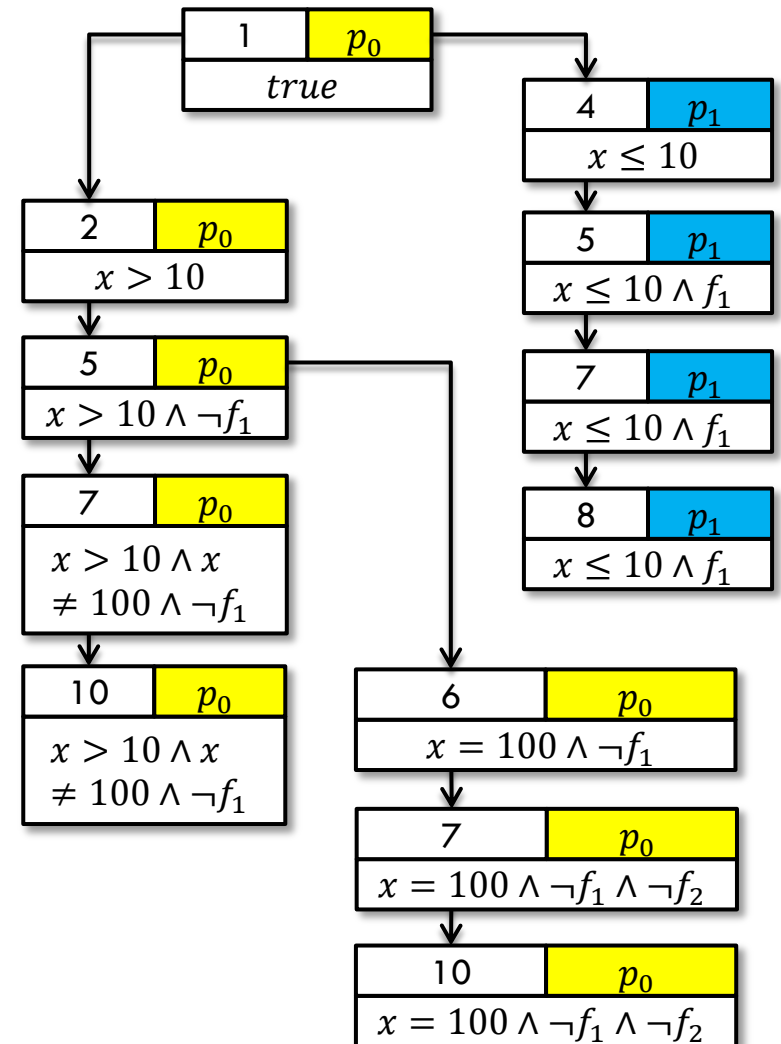


Reuse Information for Shared Parts

Automaton B

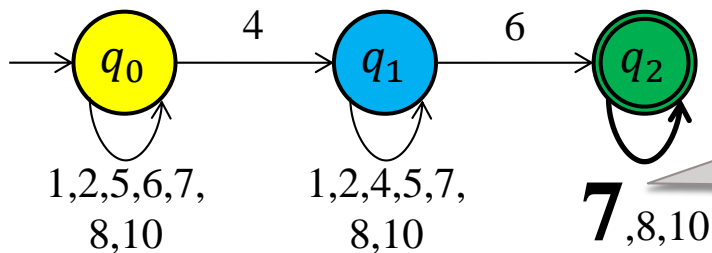
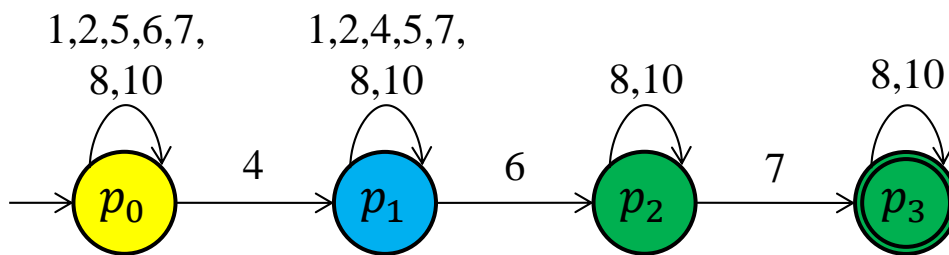


Automaton A

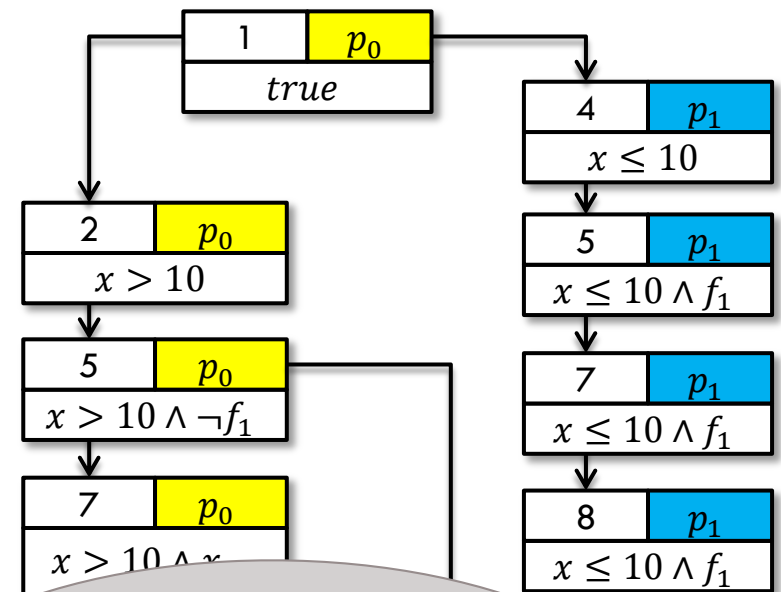


Reuse Information for Shared Parts

Automaton B



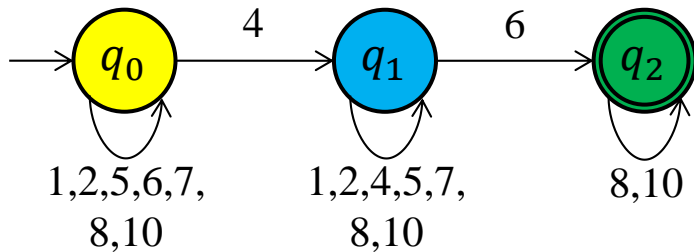
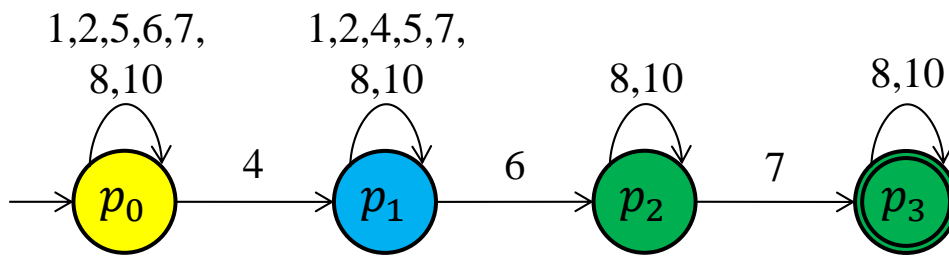
Automaton A



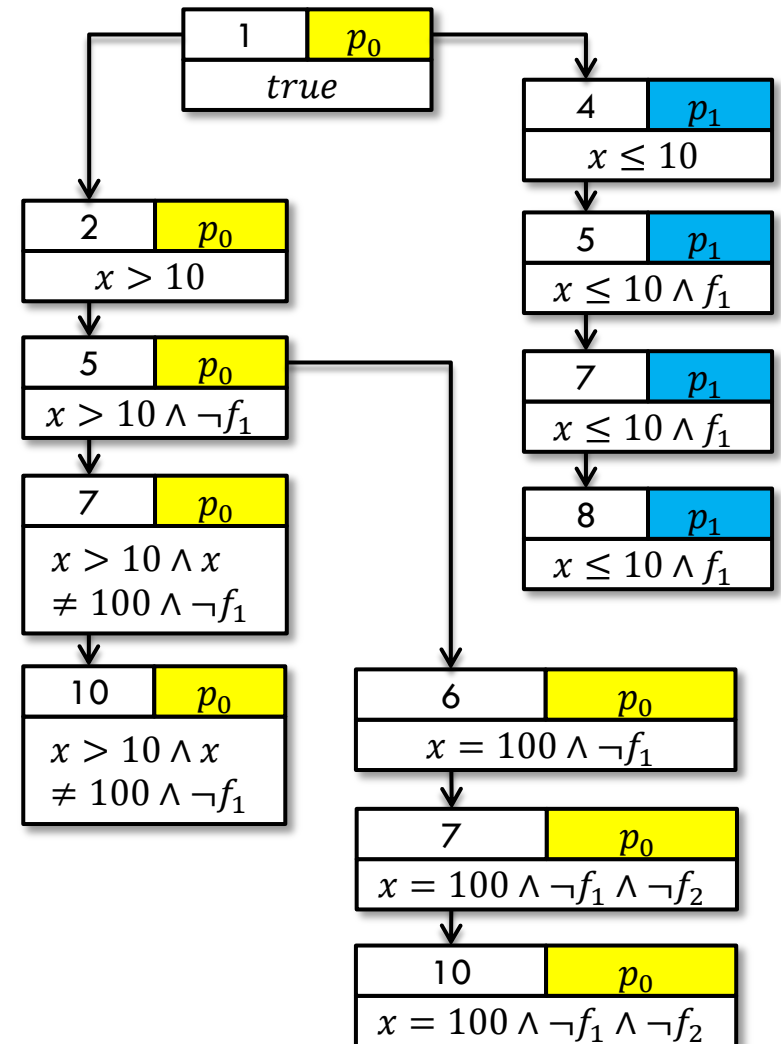
What if we
remove
 $(q_2, 7, q_2)$?

Simulation Modulo $(q_2, 7, q_2)$

Automaton B

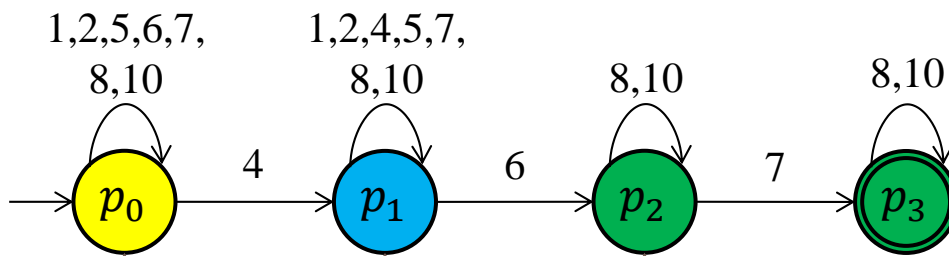


Automaton A'

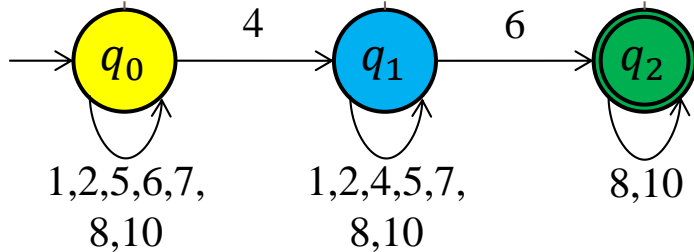


Simulation Modulo $(q_2, 7, q_2)$

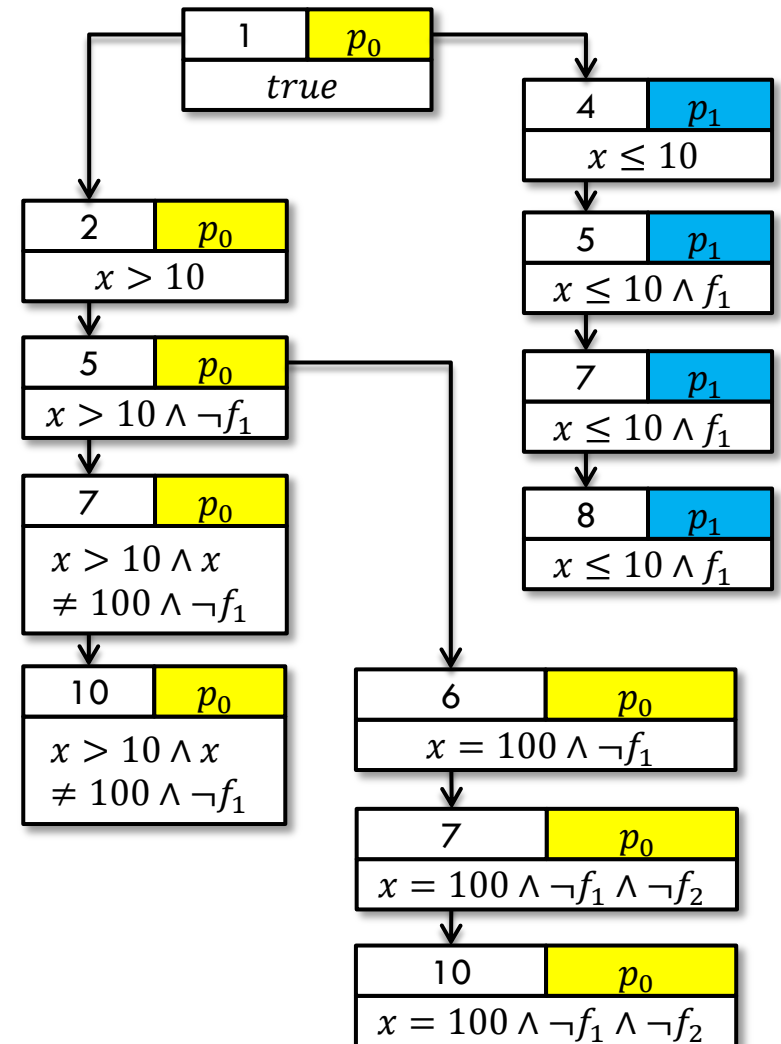
Automaton B



H

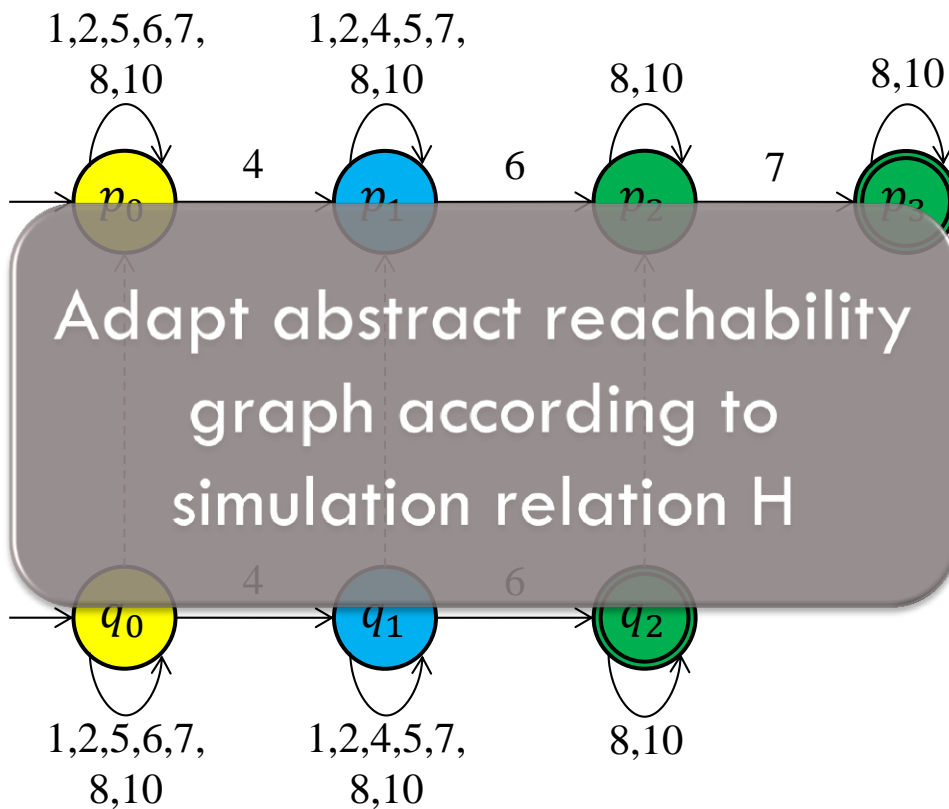


Automaton A'

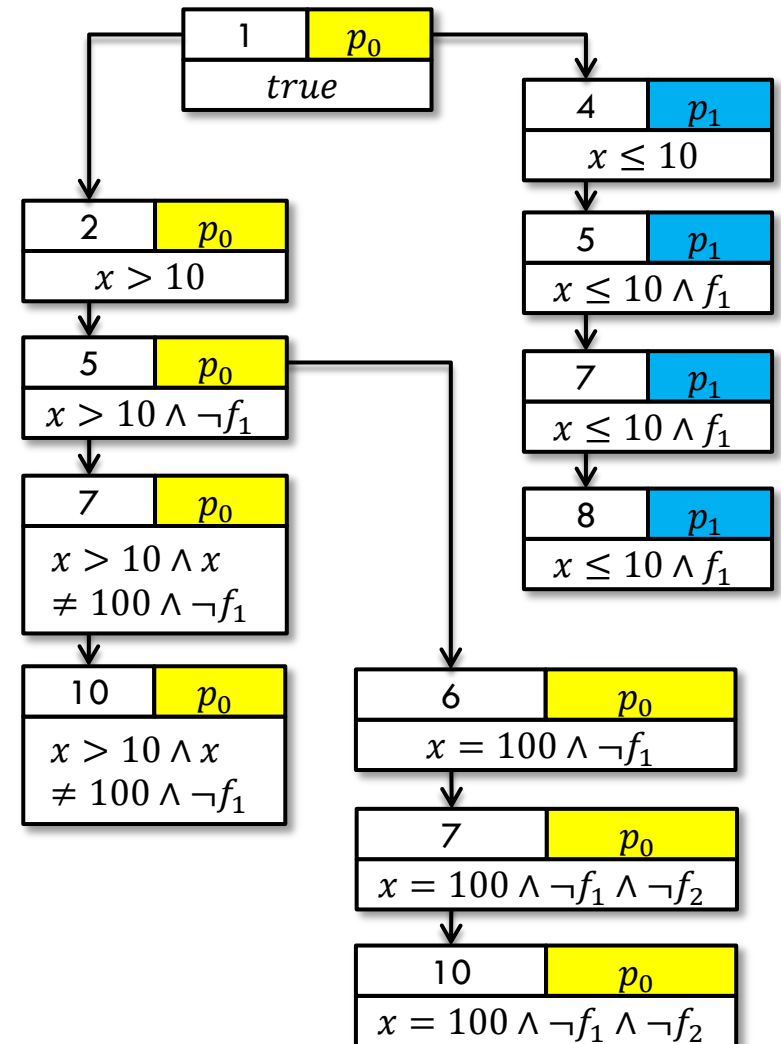


Simulation Modulo $(q_2, 7, q_2)$

Automaton B

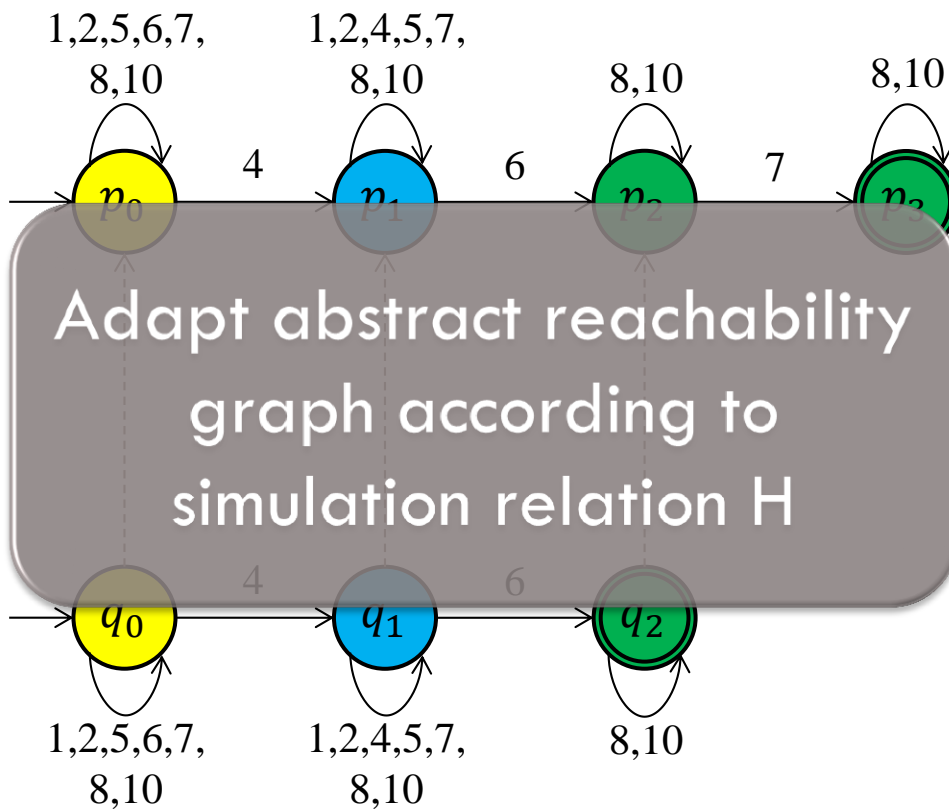


Automaton A'

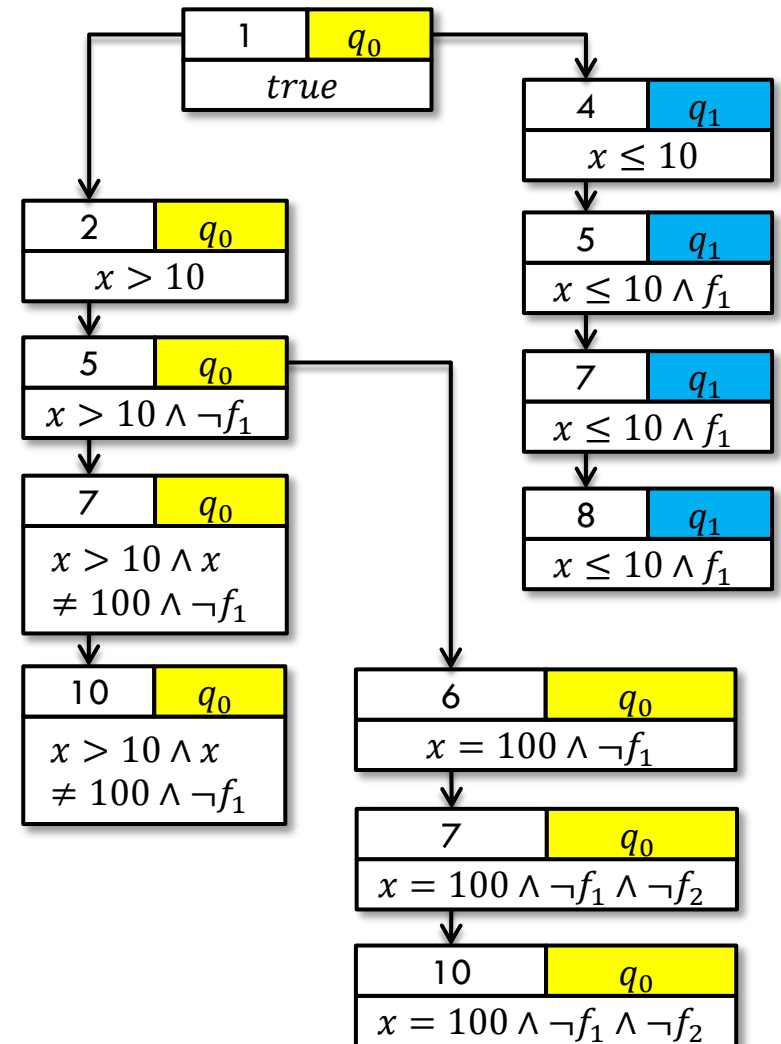


Simulation Modulo $(q_2, 7, q_2)$

Automaton B

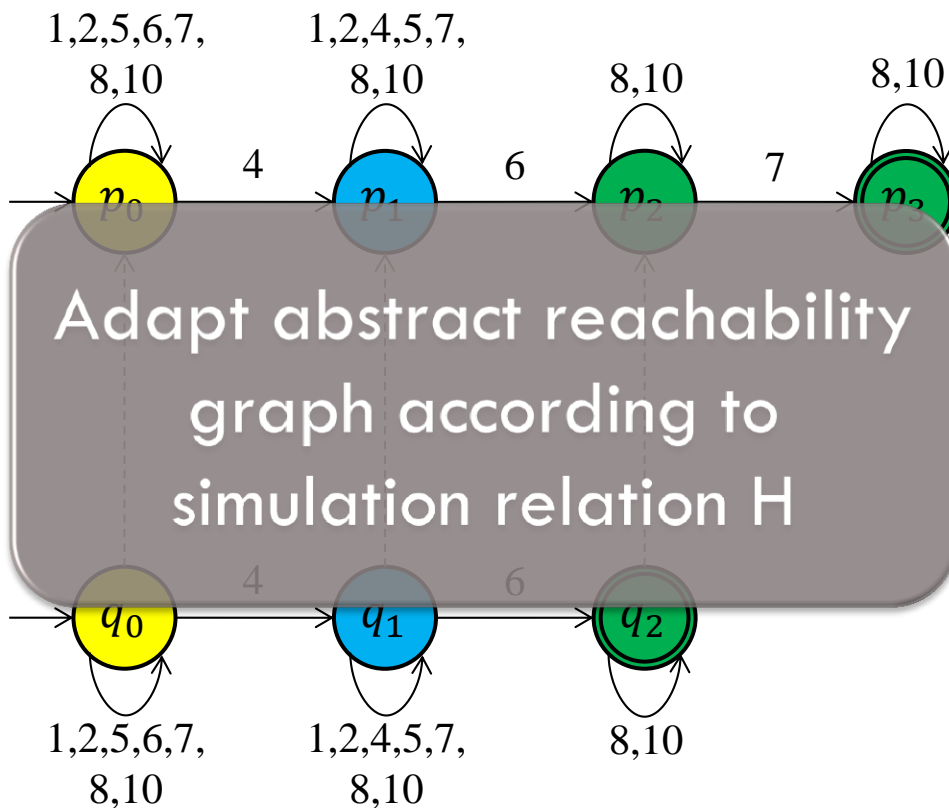


Automaton A'

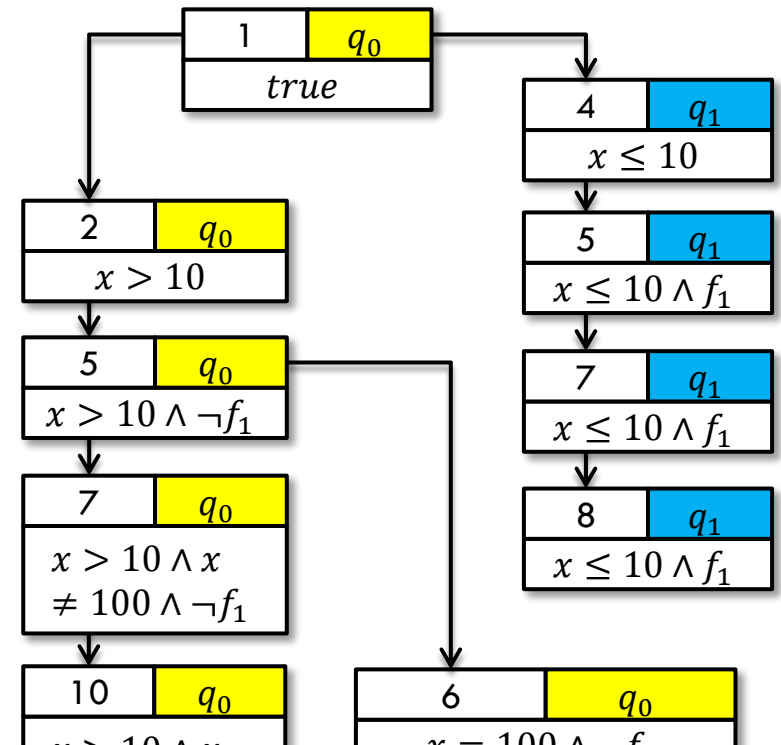


Simulation Modulo $(q_2, 7, q_2)$

Automaton B



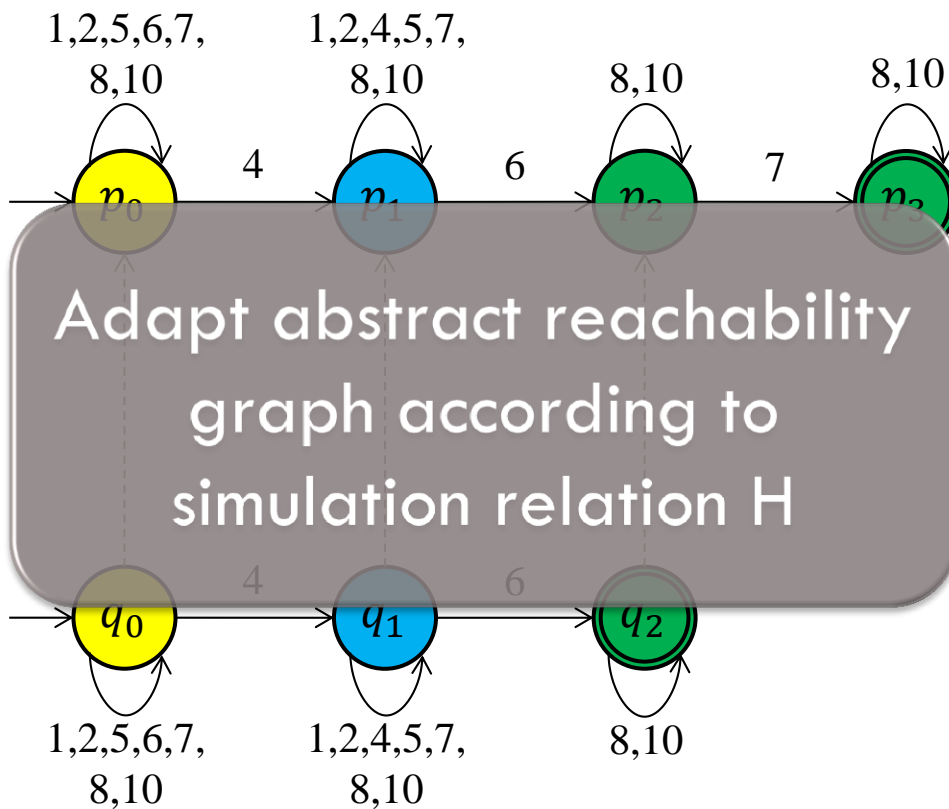
Automaton A'



There is no abstract state labeled with q_2 !

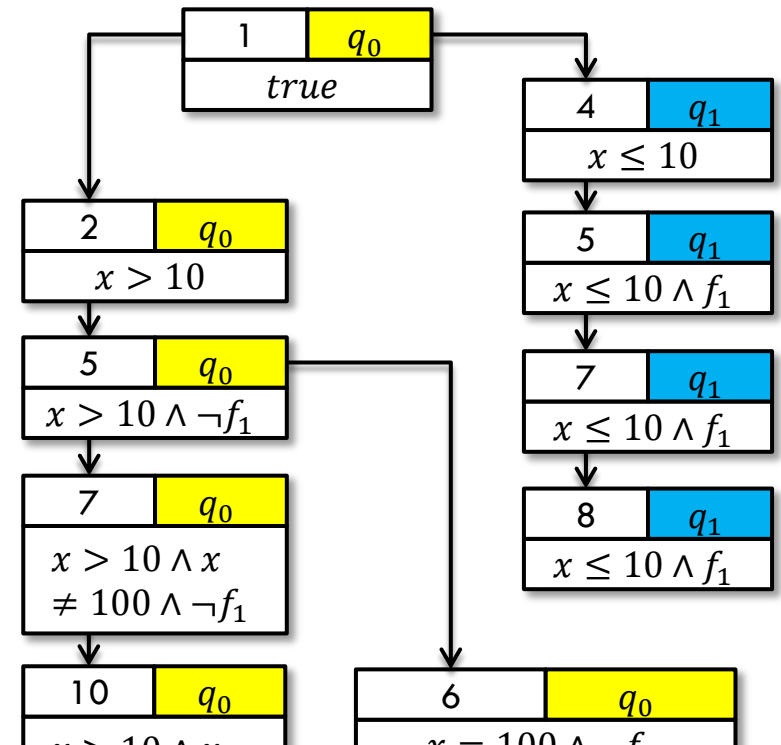
Simulation Modulo $(q_2, 7, q_2)$

Automaton B



Automaton A'

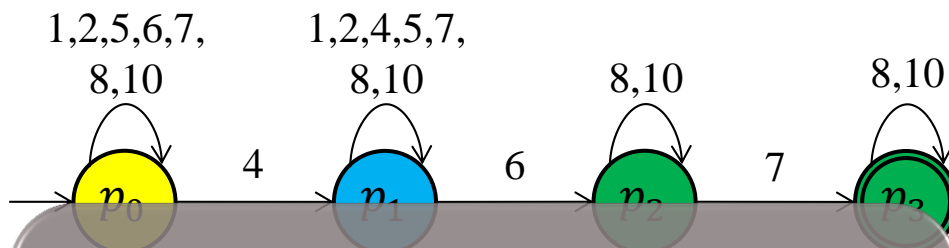
Unsatisfiable!



There is no abstract state labeled with q_2 !

Simulation Modulo $(q_2, 7, q_2)$

Automaton B

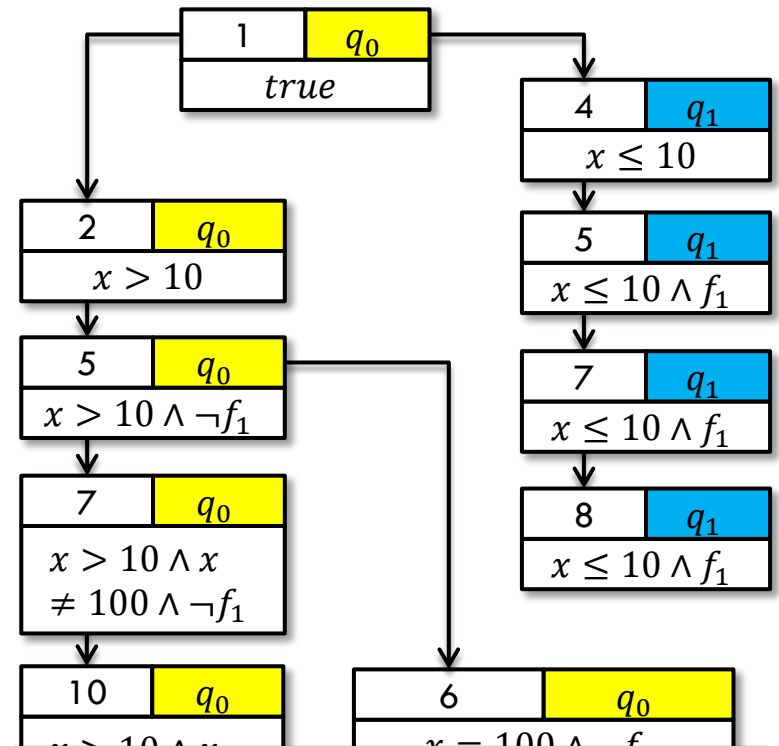


Adapt abstract reachability

Automaton A is
unsatisfiable as well!

Automaton A'

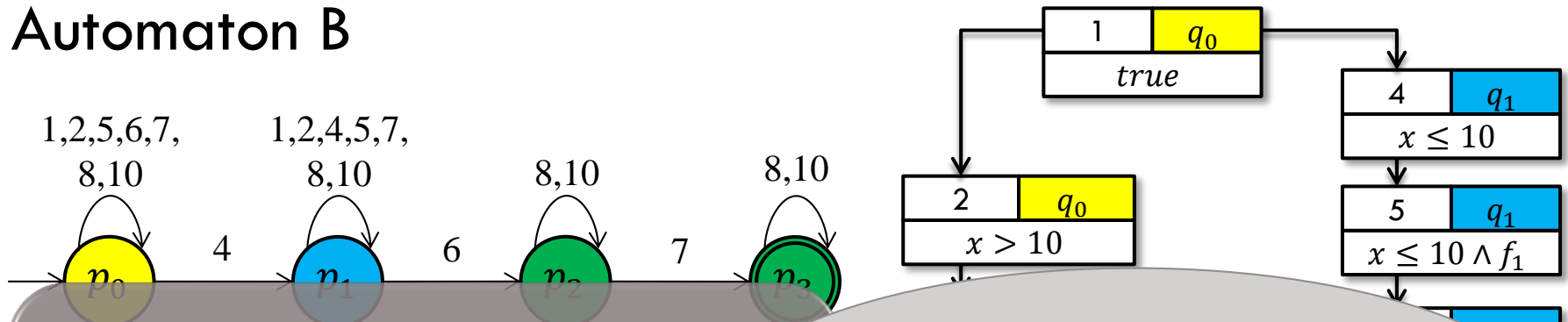
Unsatisfiable!



There is no abstract state
labeled with q_2 !

Simulation Modulo $(q_2, 7, q_2)$

Automaton B



Adapt abstract reachability

In general, we need a special handling for $(q_2, 7, q_2)$!

Automaton A is unsatisfiable as well!

There is no abstract state labeled with q_2 !

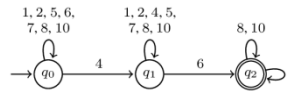
Automaton A' ← Unsatisfiable!

Simulation Modulo X

- Identify a set X of automaton transitions (of the new test goal automaton)
- Exclude X when computing a simulation relation between the old automaton and the new automaton
- Adapt abstract reachability graph
- Reinvoke the reachability analysis for automaton transitions in X
- **The choice of X is not unique!**

State Space Exploration

Automaton



Initial Abstract State



Information Reuse

Stored
ARGs

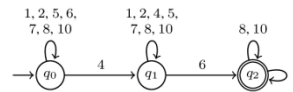
Reachability Analysis

State Space Exploration

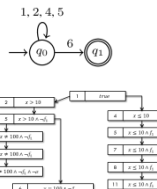
Initial Abstract State



Automaton



Information Reuse

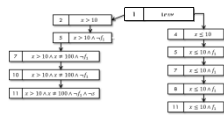


Stored ARGs

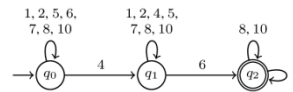
Reachability Analysis

State Space Exploration

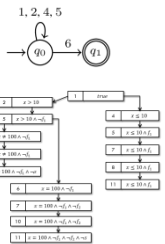
Initial Abstract State



Automaton



Information Reuse

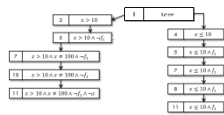


Stored ARGs

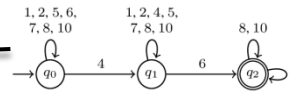
Reachability Analysis

State Space Exploration

Initial Abstract State



Automaton

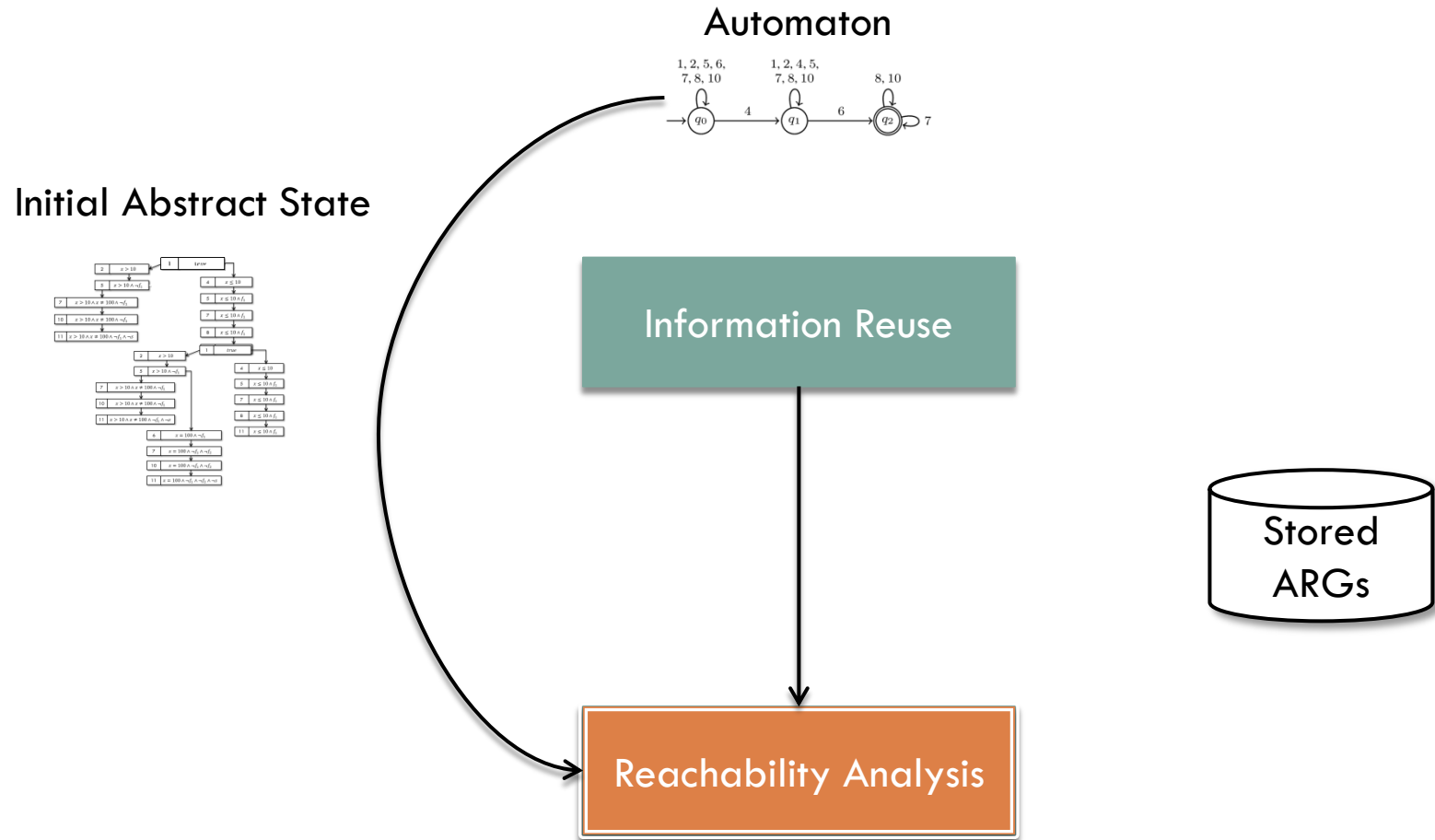


Information Reuse

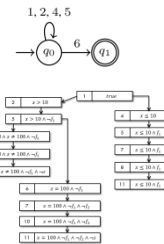
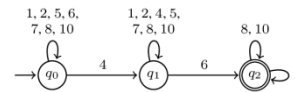
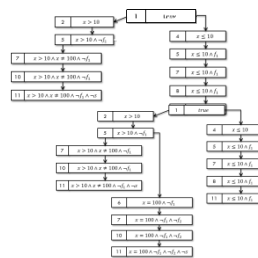
Reachability Analysis

Stored
ARGs

State Space Exploration



State Space Exploration

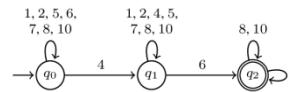


State Space Exploration

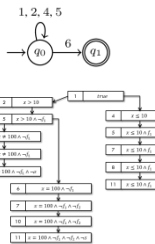
Initial Abstract State



Automaton



Information Reuse

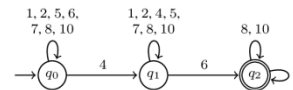


Stored ARGs

Reachability Analysis

State Space Exploration

Automaton



Initial Abstract State



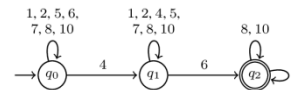
Information Reuse

Stored
ARGs

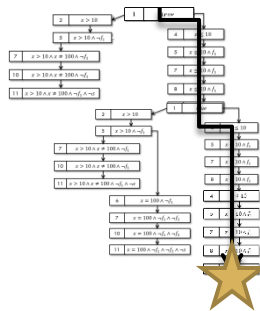
Reachability Analysis

State Space Exploration

Automaton



Initial Abstract State



Information Reuse

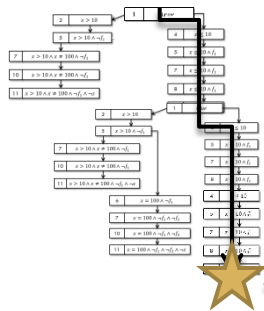
Witness of
Satisfiability

Stored
ARGs

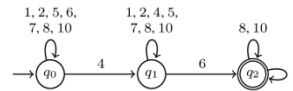
Reachability Analysis

State Space Exploration

Initial Abstract State



Automaton



Information Reuse

Witness of Satisfiability

Reachability Analysis

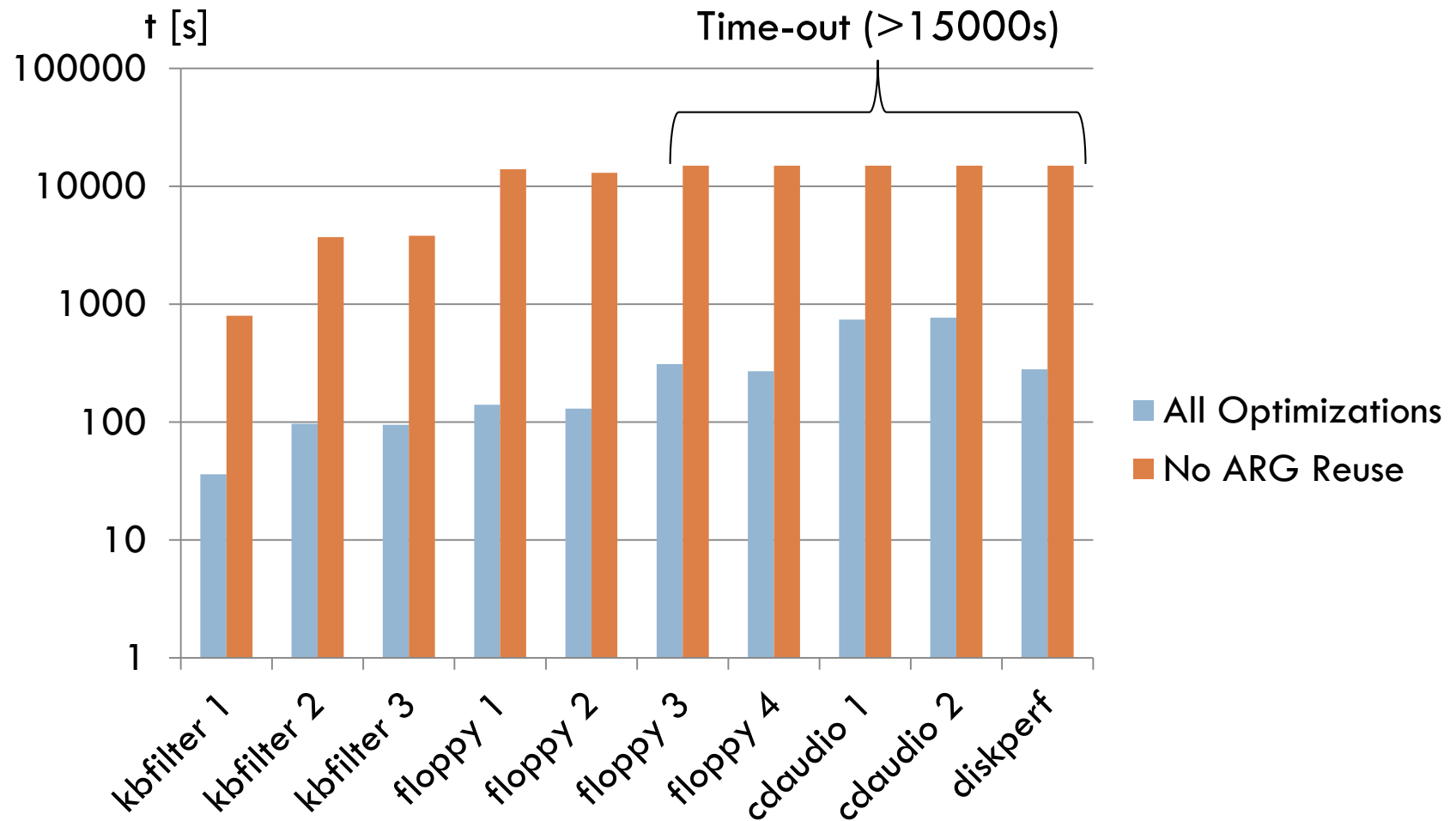
Derive Inputs

Stored ARGs

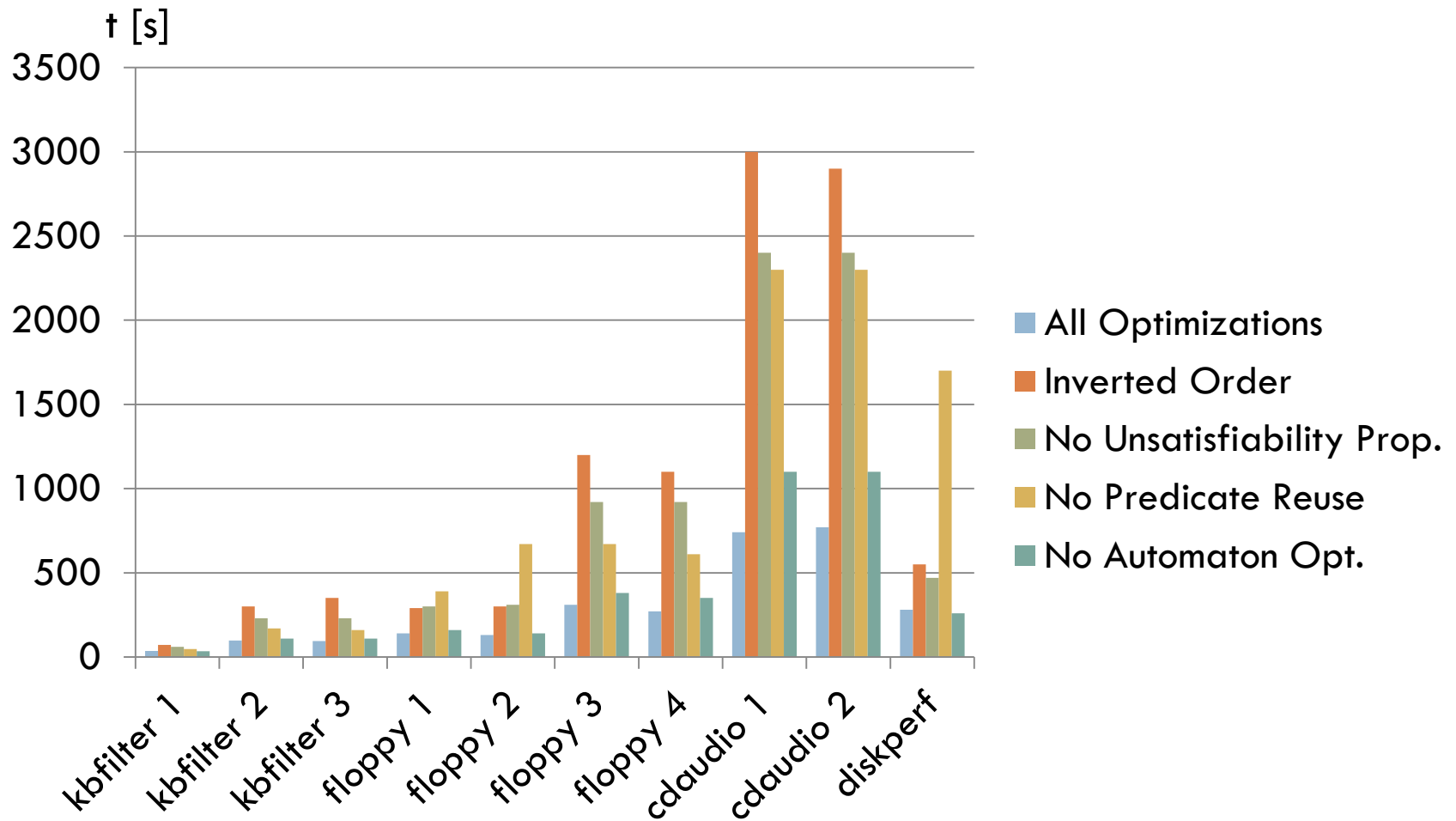
Experiments

- Variants of Basic Block Coverage:
 - ▣ BB : Cover each basic block
 - ▣ BB^2 : Cover each pair of basic blocks
 - ▣ BB^3 : Cover each triple of basic blocks
- Bounded-Path Coverage

Experiments (BB^2 Coverage)



Experiments (BB^2 Coverage)



Conclusion

- *Simulation Modulo X*: Reuse of reachability information based on relations between test-goal automata.
- *Multi-Goal Reachability Analysis*

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Thank you!