

# Software Verification

Historical Landmarks and Current Developments

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# Some Historical Landmarks

- ▶ **70 years ago: Assertions and Proof Decomposition,**  
Alan Turing, 1949 [29]  
“In order that the man who checks may not have too difficult a task the programmer should make a number of definite assertions which can be checked individually, and from which the correctness of the whole program easily follows.”

# Landmarks, Alan Turing, 1949 [29]

Friday, 24th June.

Checking a large routine, by Dr. A. Turing.

How can one check a routine in the sense of making sure that it is right?

In order that the man who checks may not have too difficult a task the programmer should make a number of definite assertions which can be checked individually, and from which the correctness of the whole programme easily follows.

Consider the analogy of checking an addition. If it is given as:

$$\begin{array}{r} 1374 \\ 5906 \\ 6719 \\ 4337 \\ 7768 \\ \hline \end{array}$$

$$26104$$

one must check the whole at one sitting, because of the carries.

But if the totals for the various columns are given, as below:

$$\begin{array}{r} 1374 \\ 5906 \\ 6719 \\ 4337 \\ 7768 \\ \hline \end{array}$$

$$\begin{array}{r} 3974 \\ 2213 \\ \hline \end{array}$$

$$26104$$

the checker's work is much easier being split up into the checking of the various assertions  $3 + 9 + 7 + 3 + 7 = 29$  etc, and the small addition

$$\begin{array}{r} 3794 \\ 2213 \\ \hline 26104 \end{array}$$

# Some Historical Landmarks

- ▶ 70 years ago: Assertions and Proof Decomposition
- ▶ **60 years ago: Logic Interpolation,**  
William Craig, J. Symb. Log. 1957 [22]  
“Linear reasoning. A new form of the Herbrand-Gentzen theorem.”  
Defines an interpolation for logic formulas  
Made popular by Ken McMillan [28]

# Some Historical Landmarks

- ▶ 70 years ago: Assertions and Proof Decomposition
- ▶ 60 years ago: Logic Interpolation
- ▶ **50 years ago: Data-Flow Analysis and Abstract States,**

Gary Kildall, POPL 1973 [27]

“A Unified Approach to Global Program Optimization”

Defines algorithm, meet operation, lattice, etc.

Extended and made popular for program analysis by

F. Nielson, H. R. Nielson, C. Hankin, P. Cousot, R. Cousot

# Landmarks, Gary Kildall, POPL 1973 [27]

## A UNIFIED APPROACH TO GLOBAL PROGRAM OPTIMIZATION

Gary A. Kildall

Computer Science Group  
Naval Postgraduate School  
Monterey, California

### Abstract

A technique is presented for global analysis of program structure in order to perform compile time optimization of object code generated for expressions. The global expression optimization presented includes constant propagation, common subexpression elimination, elimination of redundant register load operations, and live expression analysis. A general purpose program flow analysis algorithm is developed which depends upon the existence of an "optimizing function." The algorithm is defined formally using a directed graph model of program flow structure, and is shown to be correct. Several optimizing functions are defined which, when used in conjunction with the flow analysis algorithm, provide the various forms of code optimization. The flow analysis algorithm is sufficiently general that additional functions can easily be defined for other forms of global code optimization.

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- ▶ 70 years ago: Assertions and Proof Decomposition
- ▶ 60 years ago: Logic Interpolation
- ▶ 50 years ago: Data-Flow Analysis and Abstract States
- ▶ **40 years ago: LTL and Model Checking,**  
Pnueli, Clarke, Emerson, Sifakis, 1981  
Specification languages, modeling languages, algorithms,  
theory, tools  
LTL, CTL, automata, Kripke structures, model checking,  
→ software model checking

“Handbook of Model Checking”, Springer, 2018 [19]

# Some Historical Landmarks

- ▶ 70 years ago: Assertions and Proof Decomposition
- ▶ 60 years ago: Logic Interpolation
- ▶ 50 years ago: Data-Flow Analysis and Abstract States
- ▶ 40 years ago: LTL and Model Checking
- ▶ **25 years ago: Predicate Abstraction,**  
Graf, Saïdi, 1997 [23]  
Enabling idea to project software to  
a (smaller) finite state space

# Some Historical Landmarks

- ▶ 70 years ago: Assertions and Proof Decomposition
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- ▶ 25 years ago: Predicate Abstraction
- ▶ **20 years ago: Tools for Software Model Checking**

“1st generation” of tools:

- ▶ Summer 2000: SLAM [2, 1]
- ▶ Fall 2000: BLAST [24, 10]
- ▶ 2004: SATABS [20]

SLAM paper received Test-of-Time Award from PLDI,  
first to apply predicate abstraction + CEGAR to software.  
BLAST received gold medals in competitions.

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- ▶ 20 years ago: Tools for Software Model Checking
- ▶ **15 years ago: Satisfiability Modulo Theory**
  - Standard formula format SMTLIB [3]
  - Enormous breakthrough, many tools, ... [21]

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- ▶ 15 years ago: Satisfiability Modulo Theory
- ▶ **10 years ago: Competition on Software Verification**  
2012 [4]  
Competitions create awareness of tools,  
provide comparative evaluations, establish standards  
(input, exchange, comparability, reproducibility)

# Some Historical Landmarks

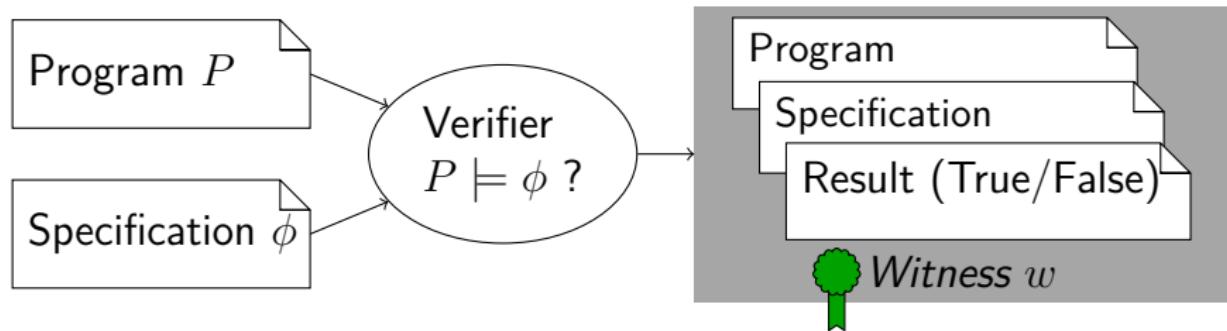
- ▶ 70 years ago: Assertions and Proof Decomposition
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- ▶ 20 years ago: Tools for Software Model Checking
- ▶ 15 years ago: Satisfiability Modulo Theory
- ▶ 10 years ago: Competition on Software Verification
- ▶ **today:** From **lack** of tools to **abundance** of tools  
Problem: missing standard interfaces, missing cooperation

# Competitions in Software Verification and Testing

- ▶ RERS: off-site, tools, free-style [25]
- ▶ SV-COMP: off-site, automatic tools, controlled [4]
- ▶ Test-Comp: off-site, automatic tools, controlled [6]
- ▶ VerifyThis: on-site, interactive, teams [26]

(alphabetic order)

# Automatic Software Verification



Theorem for  $P$  and  $S$ :  $P \models S$

If true, a proof of correctness was constructed.

If false, a proof by counterexample was constructed.

# Automatic Software Verification

Theorem for P and S:  $P \models S$

If true, a proof of correctness was constructed.

If false, a proof by counterexample was constructed.

Software often contains bugs. Thus, we appreciate tools that can answer with either outcome.

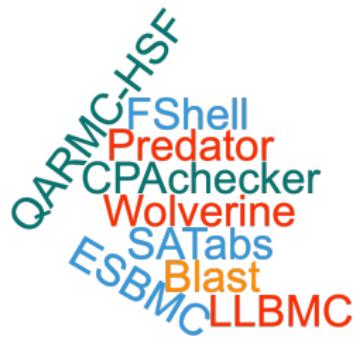
Note on **testing** and **BMC**:

⇒ verifiers for finding proofs by counterexample

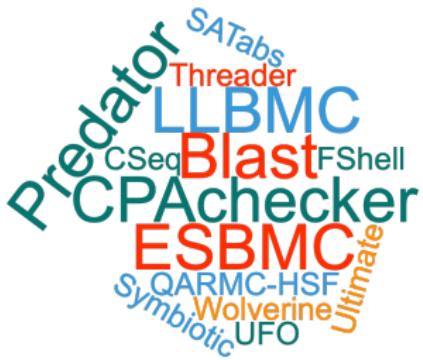
Note on **explicit-state model checking**:

⇒ verifiers that ‘produce’ huge invariants

# SV-COMP (Automatic Tools 2012)



# SV-COMP (Automatic Tools 2013, cumulative)



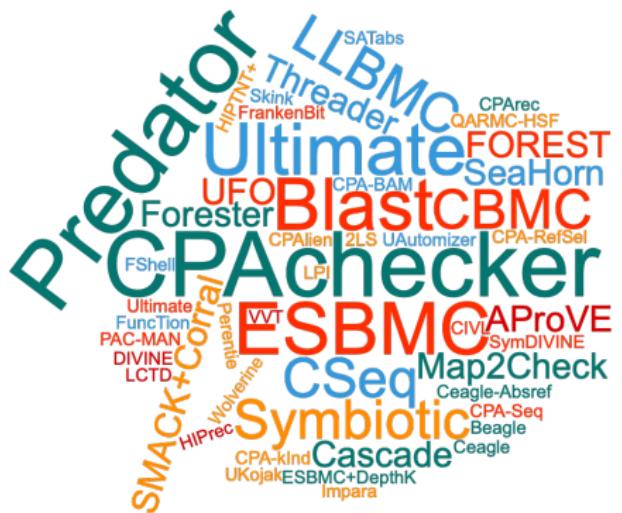
# SV-COMP (Automatic Tools 2014, cumulative)



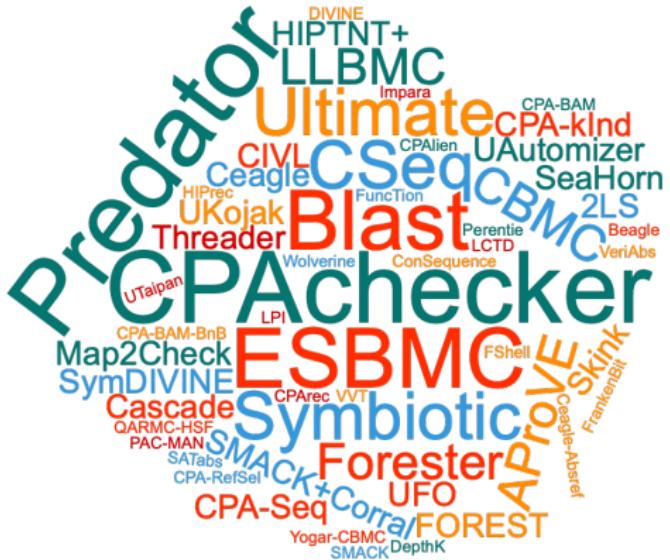
# SV-COMP (Automatic Tools 2015, cumulative)



SV-COMP (Automatic Tools 2016, cumulative)



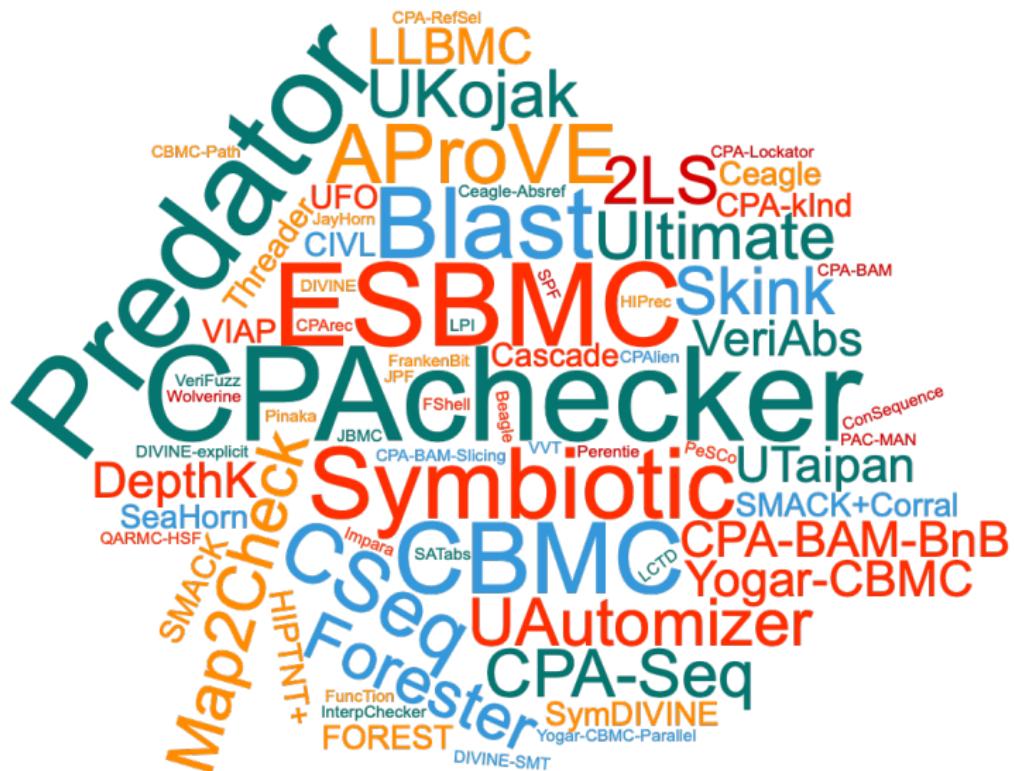
SV-COMP (Automatic Tools 2017, cumulative)



SV-COMP (Automatic Tools 2018, cumulative)



# SV-COMP (Automatic Tools 2019, cumulative)



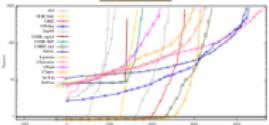
# What is the best verifier?

- ▶ Many different kinds of programs seem to require many different good tools with different strengths

# SV-COMP (Automatic Tools)

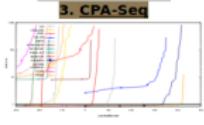
## ReachSafety

1. VeriAbs
2. CPA-Seq
3. PeSCo



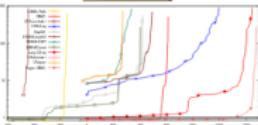
## MemSafety

1. Symbiotic
2. PredatorHP
3. CPA-Seq



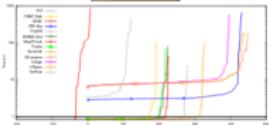
## ConcurrencySafety

1. Yogar-CBMC
2. Lazy-CSeg
3. CPA-Seq



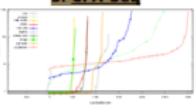
## NoOverflows

1. UAutomizer
2. UTaipan
3. CPA-Seq



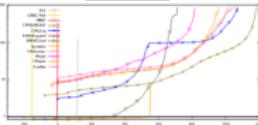
## Termination

1. UAutomizer
2. AProVE
3. CPA-Seq



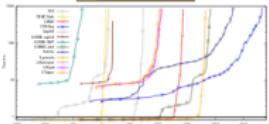
## SoftwareSystems

1. CPA-BAM-BnB
2. CPA-Seq
3. VeriAbs



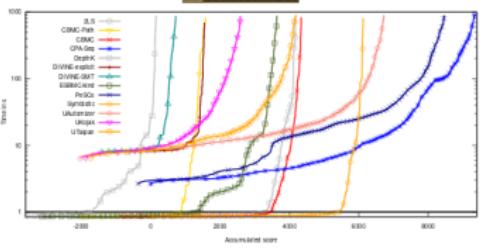
## FalsificationOverall

1. CPA-Seq
2. PeSCo
3. FSBMC-kind



## Overall

1. CPA-Seq
2. PeSCo
3. UAutomizer



<https://sv-comp.sosy-lab.org/2019/results>

# Which techniques are used?

| Participant     | CEGAR | Predicate Abstraction | Symbolic Execution | Bounded Model Checking | k-Induction | Property-Directed Reach. | Explicit-Value Analysis | Numeric. Interval Analysis | Shape Analysis | Separation Logic | Bit-Precise Analysis | ARG-Based Analysis | Lazy Abstraction | Interpolation | Automata-Based Analysis | Concurrency Support | Ranking Functions | Evolutionary Algorithms |
|-----------------|-------|-----------------------|--------------------|------------------------|-------------|--------------------------|-------------------------|----------------------------|----------------|------------------|----------------------|--------------------|------------------|---------------|-------------------------|---------------------|-------------------|-------------------------|
| 2LS             |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| AProVE          |       |                       | ✓                  |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| CBMC            |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| CBMC-PATH       |       |                       |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| CPA-BAM-BnB     | ✓     | ✓                     |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| CPA-LOCKATOR    | ✓     | ✓                     |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| CPA-SEQ         | ✓     | ✓                     |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| DEPTHK          |       |                       |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| DIVINE-EXPLICIT |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| DIVINE-SMT      |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| ESBMC-KIND      |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| JAYHORN         | ✓     | ✓                     |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| JBMC            |       |                       |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| JPF             |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| LAZY-CSEQ       |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| MAP2CHECK       |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| PeSCo           | ✓     | ✓                     |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| PINAKA          |       |                       | ✓                  | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| PREDATORHP      |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| SKBNK           | ✓     |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| SMACK           | ✓     |                       |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| SPF             |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| SYMBIOTIC       |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| UAUTOMIZER      | ✓     | ✓                     |                    | ✓                      | ✓           |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| UKOJA           | ✓     | ✓                     |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |
| UTP             |       |                       |                    |                        |             |                          |                         |                            |                |                  |                      |                    |                  |               |                         |                     |                   |                         |

Competition Report [5]

[https://doi.org/10.1007/978-3-030-17502-3\\_9](https://doi.org/10.1007/978-3-030-17502-3_9)

# Algorithms

- 17 Bounded Model Checking
- 13 CEGAR
- 8 Predicate Abstraction
- 5 k-Induction
- 4 Symbolic Execution
- 3 Automata-Based Analysis
- 2 Property-Directed Reachability (IC3)

# Abstract Domains

- 24 Bit-Precise Analysis
- 10 Explicit-Value Analysis
- 9 Numerical Interval Analysis
- 4 Shape Analysis
- 1 Separation Logic

# Testing

- ▶ Fuzzing (VeriFuzz [18], based on AFL)
- ▶ Symbolic execution (KLEE [17])
- ▶ Software model checking (CoVeriTest [13])

# SMT-based Software Model Checking

- ▶ Predicate Abstraction  
(BLAST, CPAchecker, SLAM, ...)
- ▶ IMPACT  
(CPAchecker, IMPACT, WOLVERINE, ...)
- ▶ Bounded Model Checking  
(CBMC, CPAchecker, ESBMC, ...)
- ▶  $k$ -Induction  
(CPAchecker, ESBMC, 2LS, ...)
- ▶ Property-Directed Reachability (PDR, also known as IC3)  
(CPAchecker, SEAHORN, VVT, ...)
- ▶ Trace Abstraction  
(ULTIMATE AUTOMIZER, CPAchecker in progress, ...)

# Unification Efforts

## A Unifying View on SMT-Based Software Verification

Dirk Beyer, Matthias Dangl, Philipp Wendler

Journal of Automated Reasoning, 2018 [8]

based on

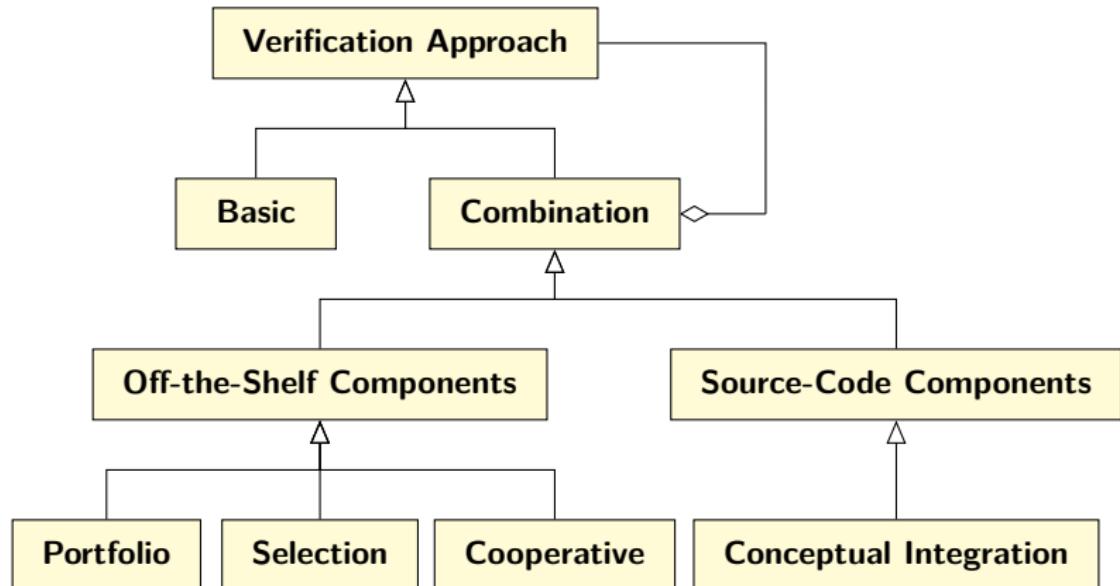
- ▶ Configurable Program Analysis [11, 12]
- ▶ Large-Block Encoding [7, 15]
- ▶ Satisfiability Modulo Theories [3]

## Combining Model Checking and Data-Flow Analysis

Dirk Beyer, Sumit Gulwani, David Schmidt

Handbook of Model Checking, 2018 [9]

# Combinations and Cooperation [16]



# Decompose Software Verification [14]

Step 1: Find invariants

Step 2: Try to prove that invariants hold

Step 3: Try to prove that invariants imply the specification

Repeat if no success

# Conclusion

- ▶ Software verification: successful past, bright future
- ▶ Competitions solve several problems
- ▶ Science as knowledge compression
- ▶ Cooperating combinations are the future

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