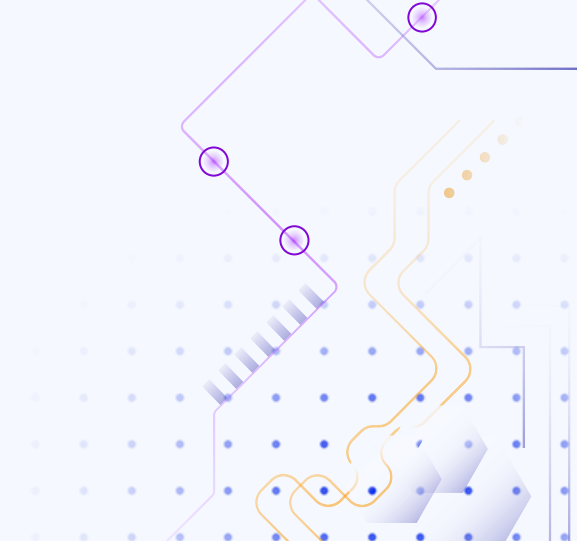





Improving the Encoding of Arrays in Btor2-to-C Translation

Bachelor-Thesis Defense Talk by Salih Ates
Date: August 30th , 2023





0

Intro Talk Recap

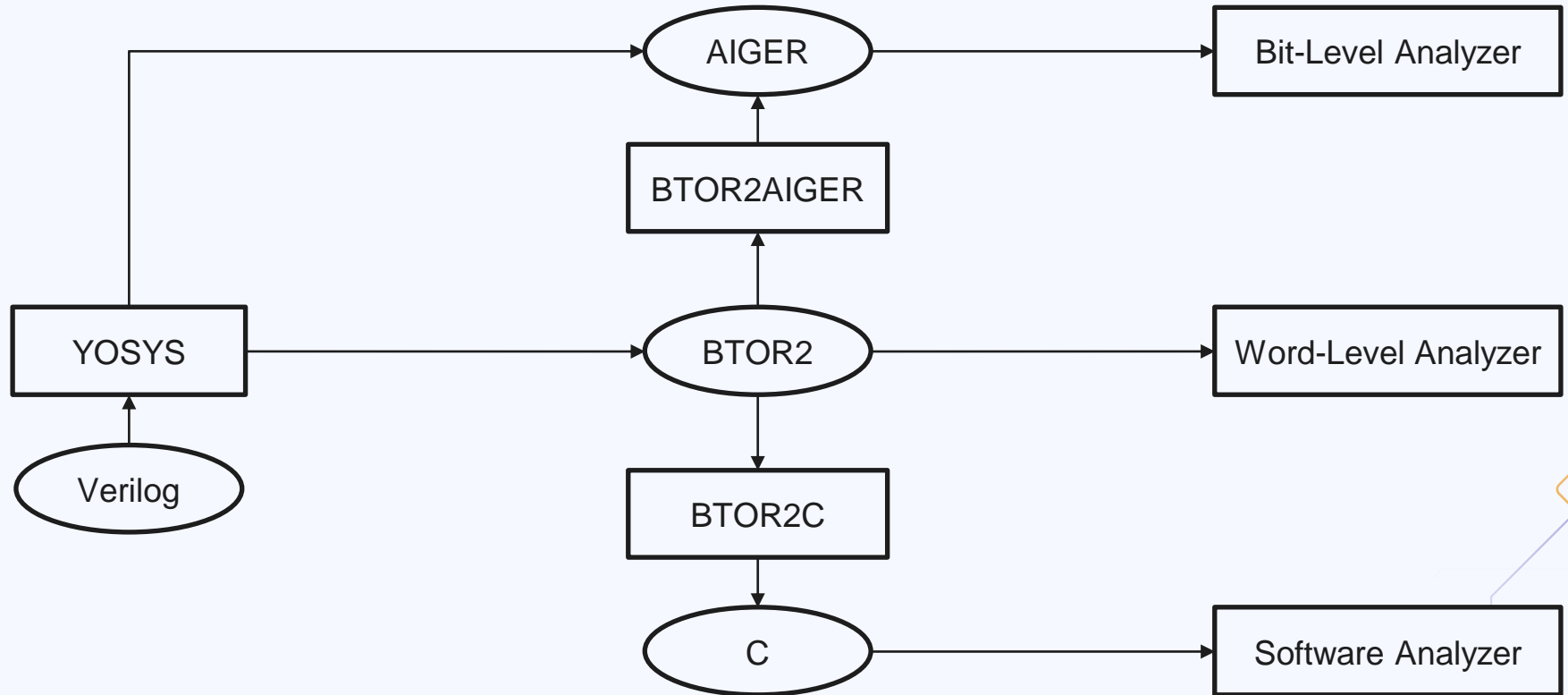
Motivation

Tool		ABC	AVR	CPACHECKER		ESBMC		VERIABS	
Algorithm		PDR	PDR	Pred.	Abs.	k -Induction		Loop	Abs.
Input	Tasks	AIGER	BTOR2	C-e	C-l	C-e	C-l	C-e	C-l
Correct results	1498	862	736	274	280	401	410	392	393
BV proofs	868	524	458	188	189	88	93	53	49
BV alarms	473	338	233	86	91	311	315	337	342
Array proofs	140	—	45	0	0	0	0	0	0
Array alarms	17	—	0	0	0	2	2	2	2
Wrong proofs		0	0	0	0	0	0	2	2
Wrong alarms		0	0	0	0	0	0	1	1
Timeouts		479	559	924	922	554	551	1049	1042
Out of memory		0	3	9	7	543	537	3	4
Other inconclusive		0	200	291	289	0	0	51	56

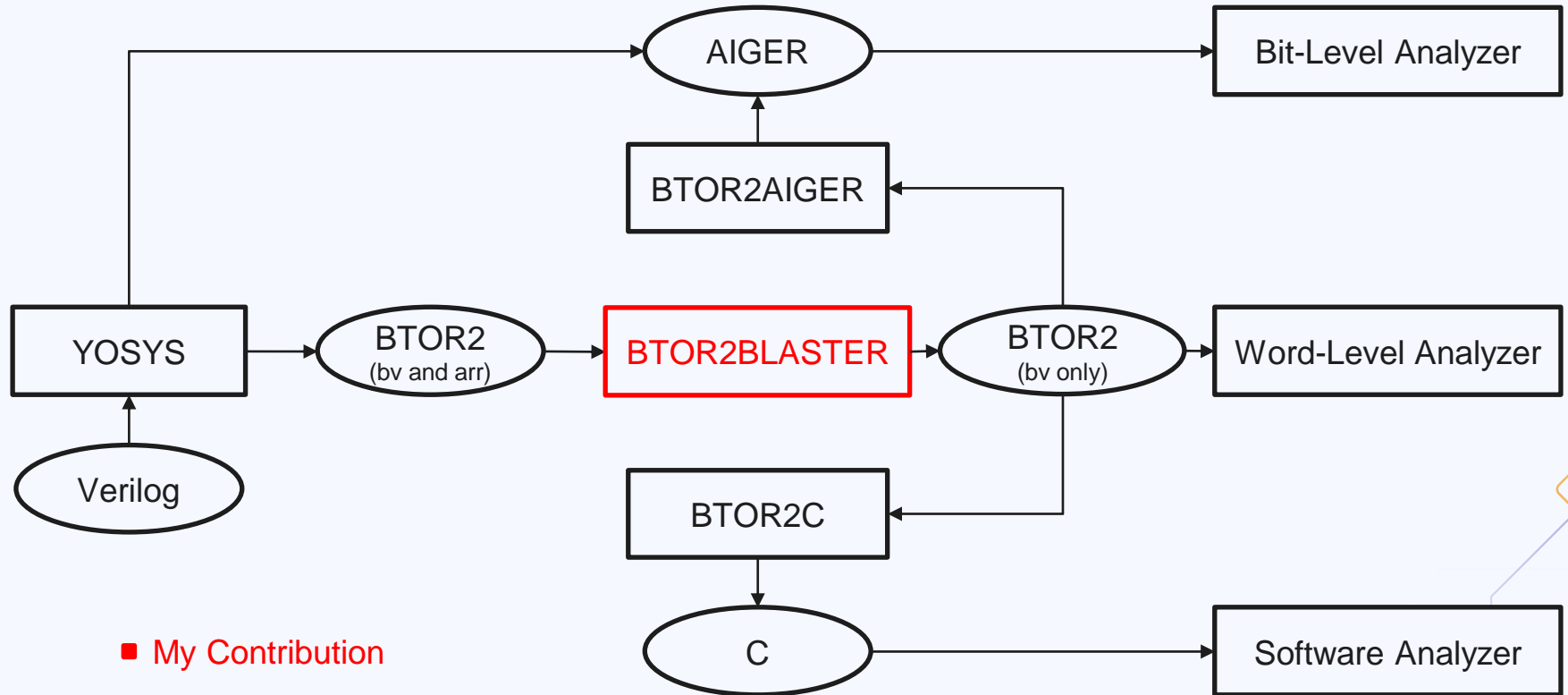
Source: Bridging Hardware and Software Analysis with Btor2C: A Word-Level-Circuit-to-C Translator, https://doi.org/10.1007/978-3-031-30820-8_12 (Table 1)



(1) Array blasting



(1) Array blasting



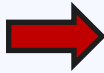
(2) ALAP-Scheduling of write-ops

(as-late-as-possible)

Objective:

Minimize number of duplications for write operations.

1 sort bitvec 3
2 sort array 1 1
3 state 2
4 input 1
5 constd 1 0
6 constd 1 1
7 constd 1 2
8 write 2 3 4 5
9 write 2 8 6 7
10 write 2 9 4 6
11 read 1 10 4
12 sort bitvec 1
13 eq 12 11 5
14 bad 13



```
SORT_2 write_8;  
for(i = 0; i < len(old_arr); ++i){  
    write_8[i] = old_arr[i];  
}  
write_8[arg_1] = value;
```

(2) ALAP-Scheduling of write-ops

(as-late-as-possible)

Objective:

Minimize number of duplications for write operations.

1 sort bitvec 3

2 sort array 1 1

3 state 2

4 input 1

5 constd 1 0

6 constd 1 1

7 constd 1 2

8 write 2 3 4 5

9 write 2 8 6 7

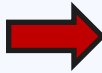
10 write 2 9 4 6

11 read 1 10 4

12 sort bitvec 1

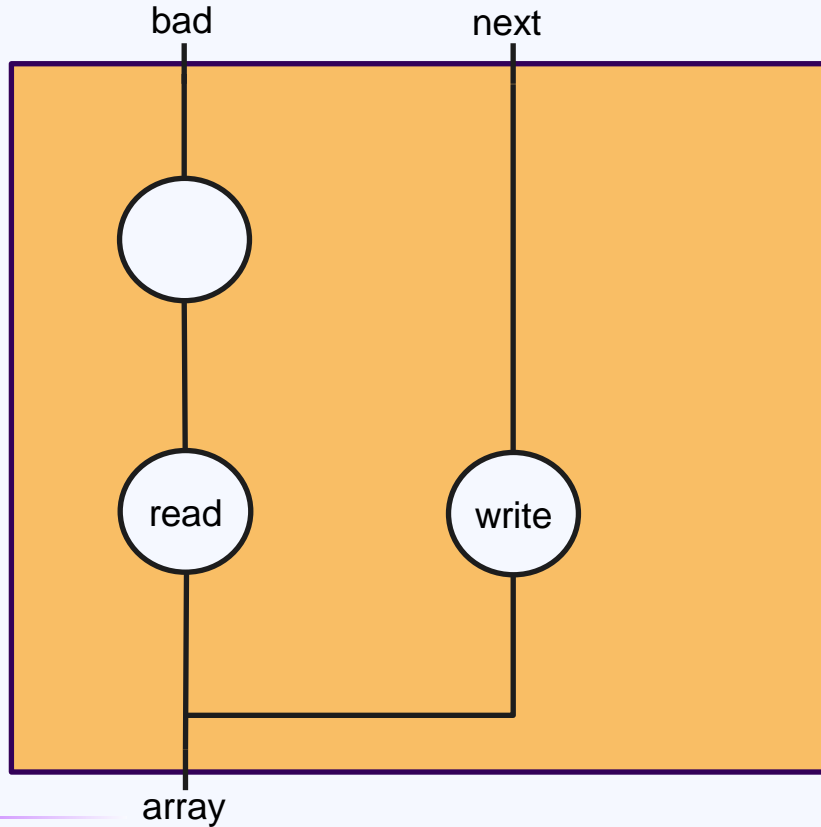
13 eq 12 11 5

14 bad 13



```
SORT_2* write_8 = old_arr;  
write_8[arg_1] = value;
```

(2) ALAP-Scheduling of write-ops



schedule = [array, write, read]

→ Duplication needed

schedule = [array, read, write]

→ Duplication can be avoided



1

Array blasting

(1) Array blasting

1 sort bitvec 1
2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2
5 state 4
6 input 3
7 constd 2 1
8 write 4 5 6 7
9 read 2 5 6
10 eq 1 5 8
11 neq 1 5 8
12 ite 3 10 5 8
13 init 3 5 8
14 next 3 5 8

All array operations:

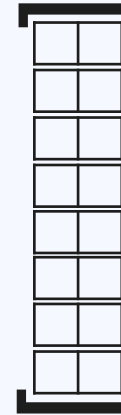
- state
- write
- read
- eq
- neq
- ite
- init
- next

(1) Array blasting - state

2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2
5 state 4



2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2



5 state 2
6 state 2
7 state 2
8 state 2
9 state 2
10 state 2
11 state 2
12 state 2

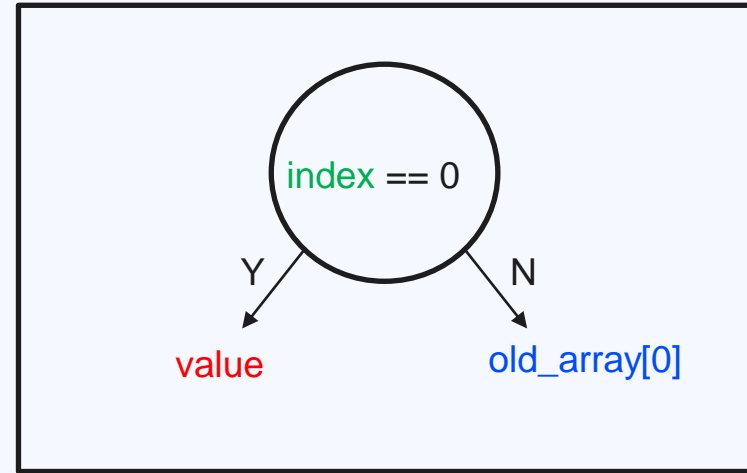
(1) Array blasting - write

```
2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2
5 state 4
6 input 3
7 constd 2 1
8 write 4 5 6 7
```

5 state 2
6 state 2
7 state 2
8 state 2
9 state 2
10 state 2
11 state 2
12 state 2

write_array[0] =

id write sort_n **old_array** **index** **value**



id ite sort_n (**index** == 0) **value** **old_array[0]**

(1) Array blasting - write

2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2
5 state 4
6 input 3
7 constd 2 1
8 write 4 5 6 7

5 state 2
6 state 2
7 state 2
8 state 2
9 state 2
10 state 2
11 state 2
12 state 2

id write sort_n old_array index value

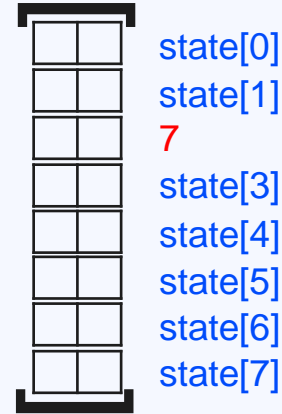
		8 ite 2 (input == 0) 7 state[0]
		9 ite 2 (input == 1) 7 state[1]
		10 ite 2 (input == 2) 7 state[2]
		11 ite 2 (input == 3) 7 state[3]
		12 ite 2 (input == 4) 7 state[4]
		13 ite 2 (input == 5) 7 state[5]
		14 ite 2 (input == 6) 7 state[6]
		15 ite 2 (input == 7) 7 state[7]

(1) Array blasting - write

```
2 sort bitvec 2
3 sort bitvec 3
4 sort array 3 2
5 state 4
6 constd 2 2
7 constd 2 1
8 write 4 5 6 7
```

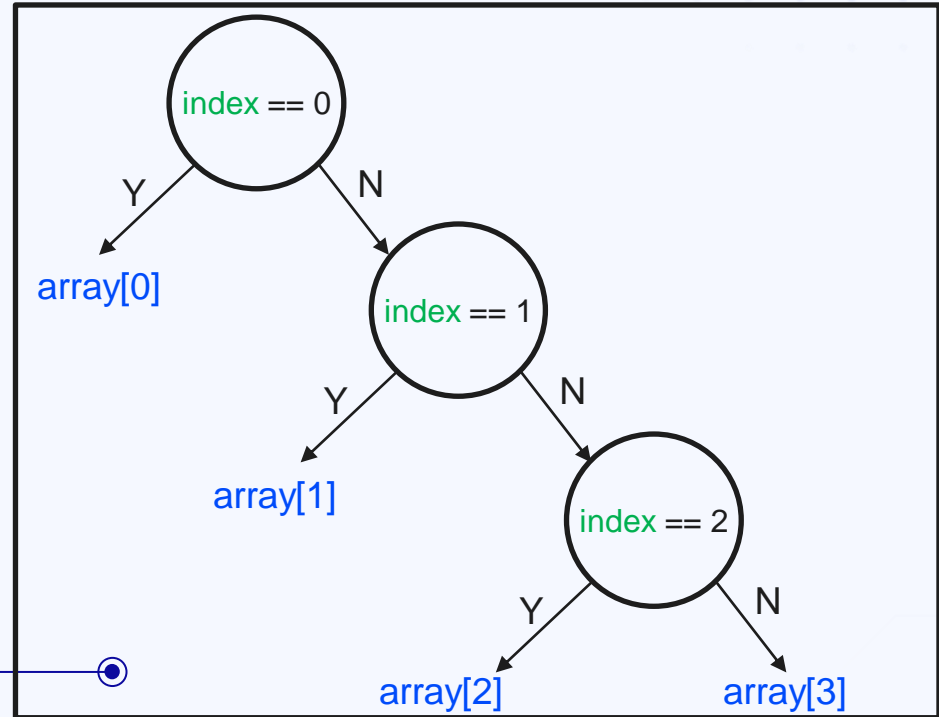
5 state 2
6 state 2
7 state 2
8 state 2
9 state 2
10 state 2
11 state 2
12 state 2

id write sort_n old_array constd value



(1) Array blasting – read (skewed)

id read sort_n array index



(1) Array blasting - read (skewed)

id read sort_n array index

2 input 1

3 state 1

4 state 1

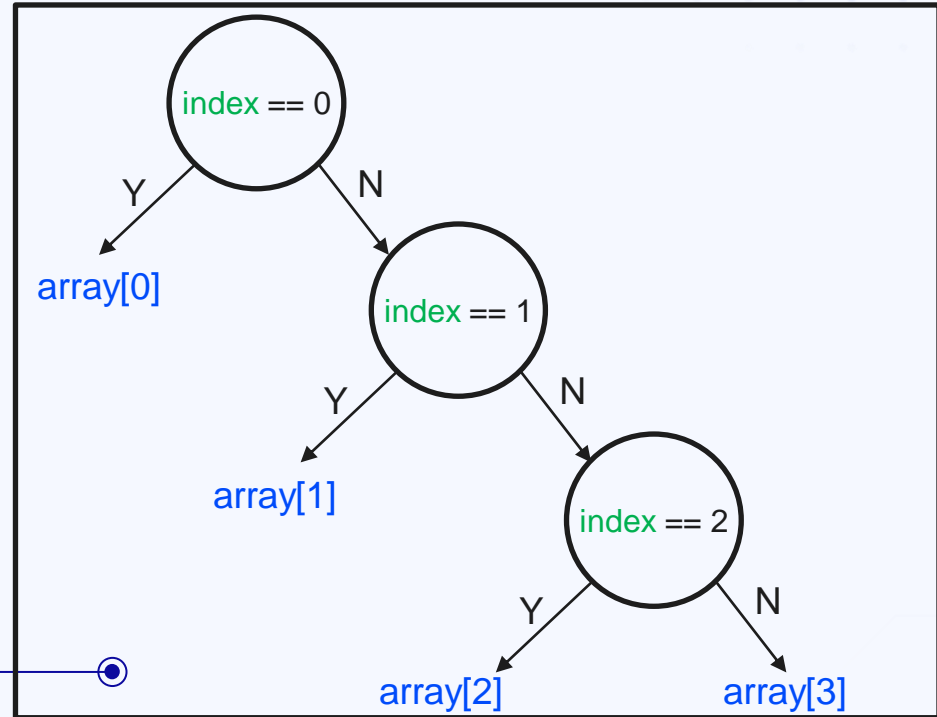
5 state 1

6 state 1

7 ite 1 (index == 2) 5 6

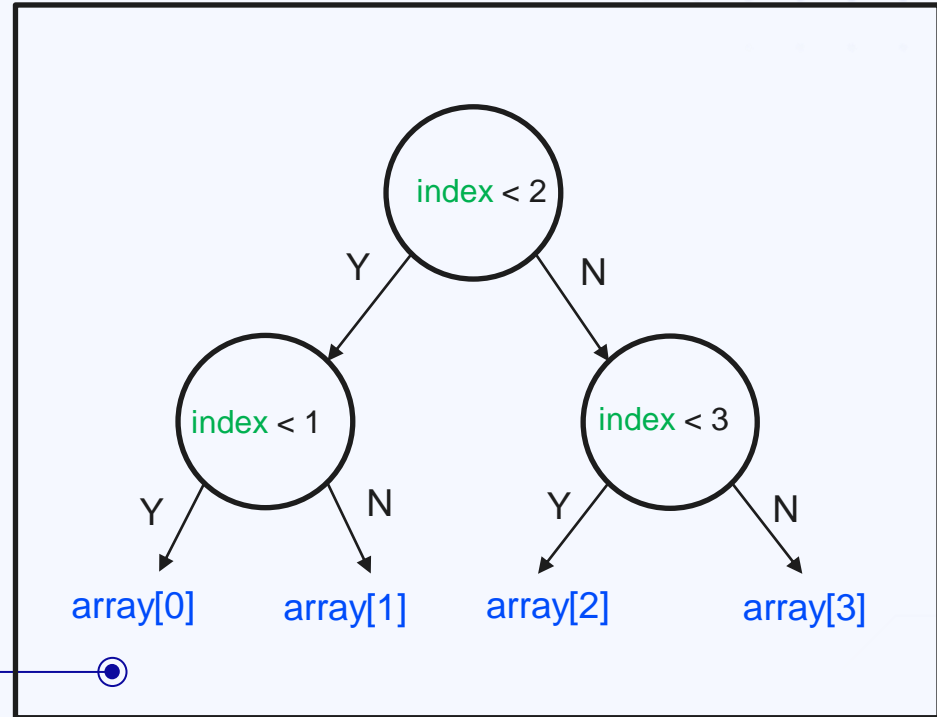
8 ite 1 (index == 1) 4 7

9 ite 1 (index == 0) 3 8



(1) Array blasting – read (balanced)

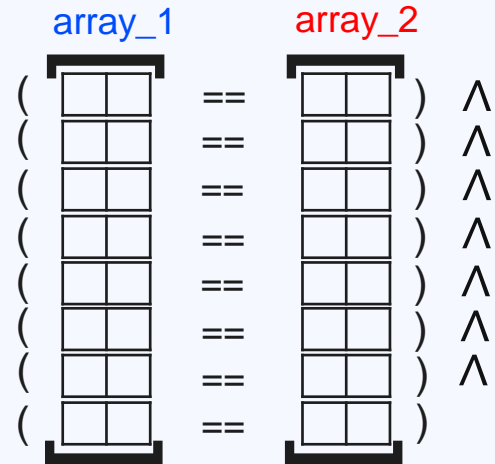
id read sort_n array index



(1) Array blasting – eq/neq

id eq sort_n array_1 array_2
id neq sort_n array_1 array_2

5 state 2		15 state 2
6 state 2		16 state 2
7 state 2		17 state 2
8 state 2	==	18 state 2
9 state 2		19 state 2
10 state 2		20 state 2
11 state 2		21 state 2
12 state 2		22 state 2



(1) Array blasting - ite

id ite sort_n cond array_1 array_2

35	ite 2	cond	5	state 2	15	state 2
36	ite 2	cond	6	state 2	16	state 2
37	ite 2	cond	7	state 2	17	state 2
38	ite 2	cond	8	state 2	18	state 2
39	ite 2	cond	9	state 2	19	state 2
40	ite 2	cond	10	state 2	20	state 2
41	ite 2	cond	11	state 2	21	state 2
42	ite 2	cond	12	state 2	22	state 2

(1) Array blasting - init

id init sort_n array_1 array_2

35	init	2	5	state	2	15	state	2
36	init	2	6	state	2	16	state	2
37	init	2	7	state	2	17	state	2
38	init	2	8	state	2	18	state	2
39	init	2	9	state	2	19	state	2
40	init	2	10	state	2	20	state	2
41	init	2	11	state	2	21	state	2
42	init	2	12	state	2	22	state	2

(1) Array blasting – next

id next sort_n array_1 array_2

35	next	2	5	state	2	15	state	2
36	next	2	6	state	2	16	state	2
37	next	2	7	state	2	17	state	2
38	next	2	8	state	2	18	state	2
39	next	2	9	state	2	19	state	2
40	next	2	10	state	2	20	state	2
41	next	2	11	state	2	21	state	2
42	next	2	12	state	2	22	state	2

(1) Array blasting

All array operations:

- ✓ state
- ✓ write
- ✓ read
- ✓ eq
- ✓ neq
- ✓ ite
- ✓ init
- ✓ next

2

ALAP-Scheduling of write-ops

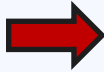
(2) ALAP-Scheduling of write-ops

(as-late-as-possible)

Objective:

Minimize number of duplications for write operations.

1 sort bitvec 3
2 sort array 1 1
3 state 2
4 input 1
5 constd 1 0
6 constd 1 1
7 constd 1 2
8 write 2 3 4 5
9 write 2 8 6 7
10 write 2 9 4 6
11 read 1 10 4
12 sort bitvec 1
13 eq 12 11 5
14 bad 13



```
SORT_2 write_8;  
for(i = 0; i < len(old_arr); ++i){  
    write_8[i] = old_arr[i];  
}  
write_8[arg_1] = value;
```

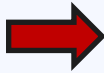

(2) ALAP-Scheduling of write-ops

(as-late-as-possible)

Objective:

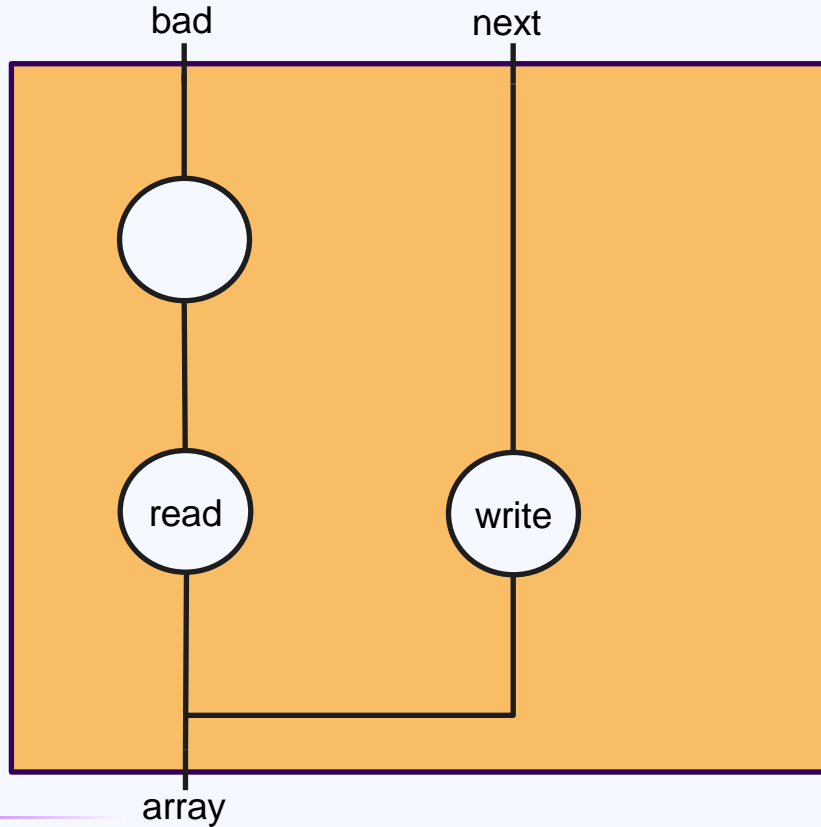
Minimize number of duplications for write operations.

1 sort bitvec 3
2 sort array 1 1
3 state 2
4 input 1
5 constd 1 0
6 constd 1 1
7 constd 1 2
8 write 2 3 4 5
9 write 2 8 6 7
10 write 2 9 4 6
11 read 1 10 4
12 sort bitvec 1
13 eq 12 11 5
14 bad 13



```
SORT_2* write_8 = old_arr;  
write_8[arg_1] = value;
```

(2) ALAP-Scheduling of write-ops



→ write → read →

!

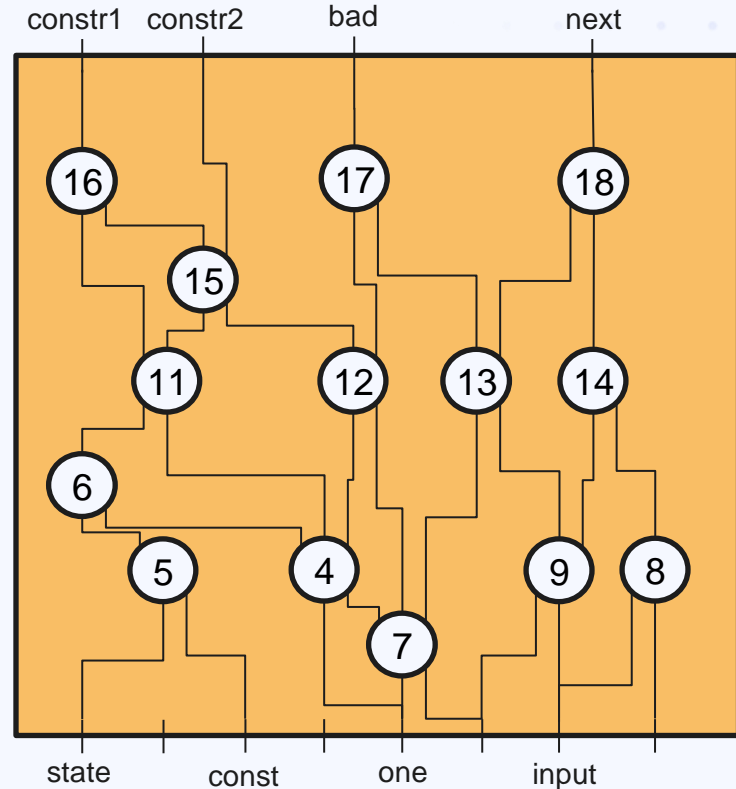
→ read → write →

✓

(2) ALAP-Scheduling of write-ops

```
for(;;) {
```

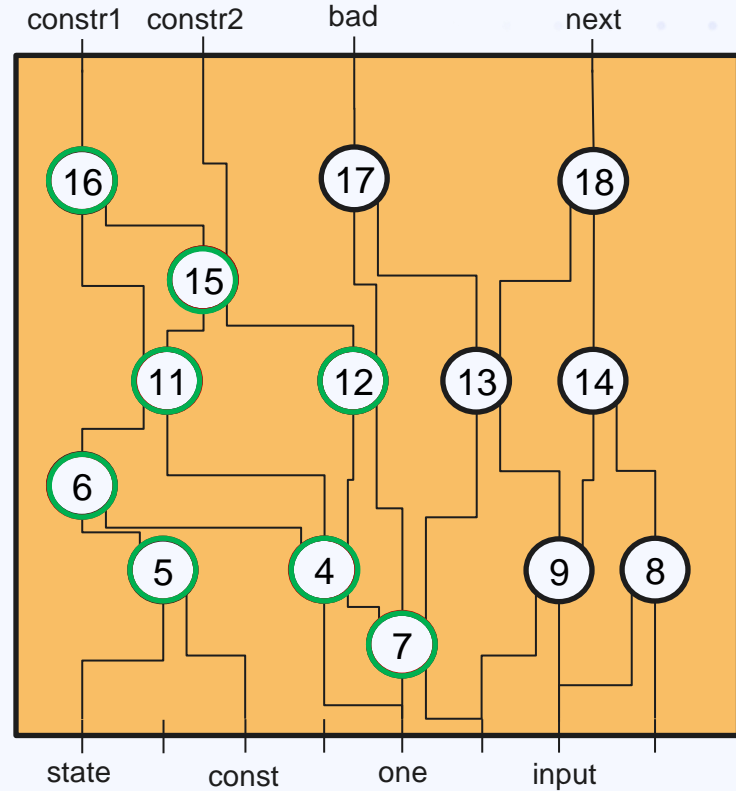
```
}
```



(2) ALAP-Scheduling of write-ops

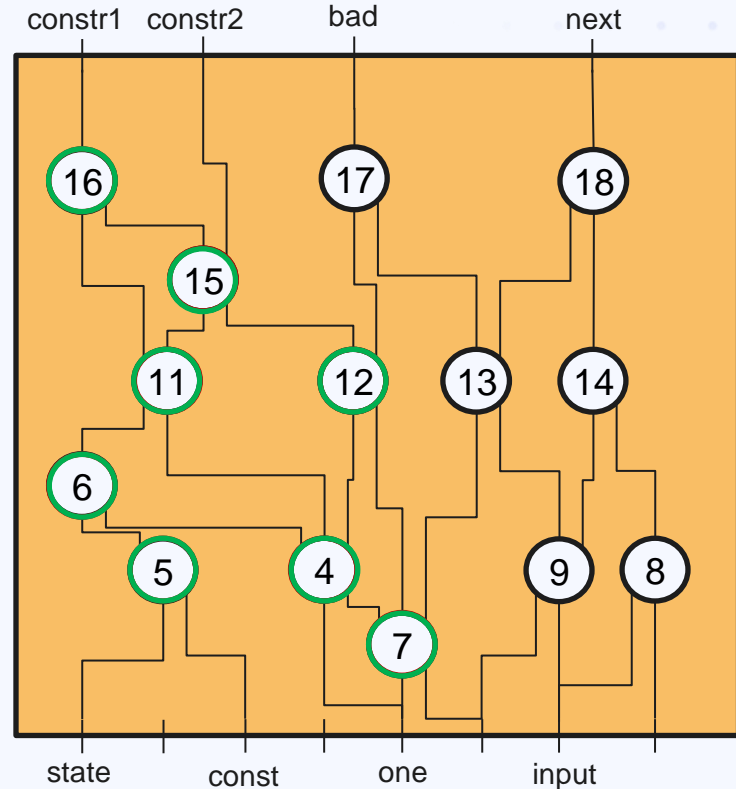
```
for(;;) {
```

```
}
```



(2) ALAP-Scheduling of write-ops

```
for(;;) {  
    var_5 = ...  
    ...  
    var_16 = ...  
    assume(constr1);  
    ...  
    assume(constr2);  
    ...  
    assert(bad);  
    ...  
    state_5 = next_arg_1;  
}
```



(2) ALAP-Scheduling of write-ops

```
for(;;) {
```

W1

W2

```
  assume(constr1);
```

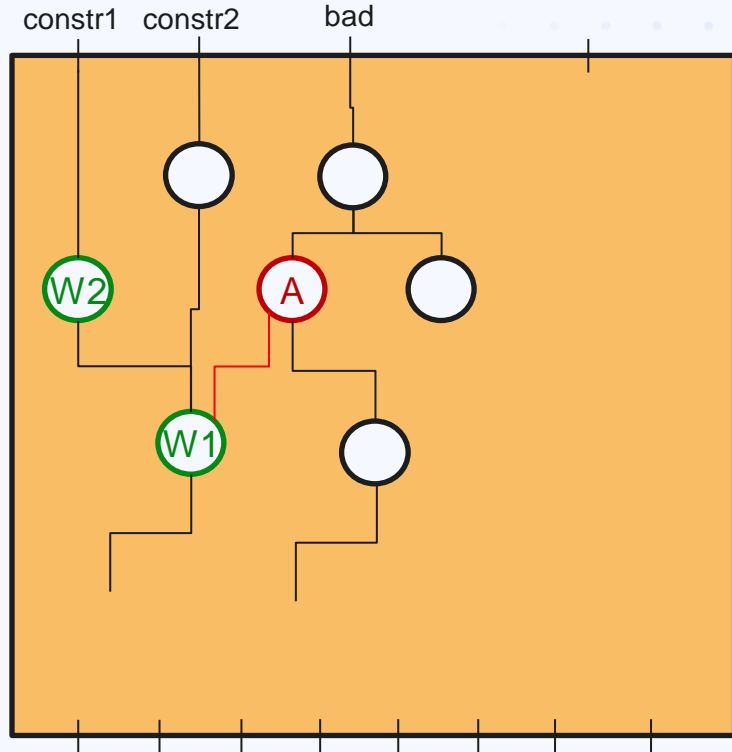
```
  ...
```

```
  assume(constr2);
```

A

```
  verifier(bad);
```

```
}
```



(2) ALAP-Scheduling of write-ops

```
for(;;) {
```

W1

A

W2

```
  assume(constr1);
```

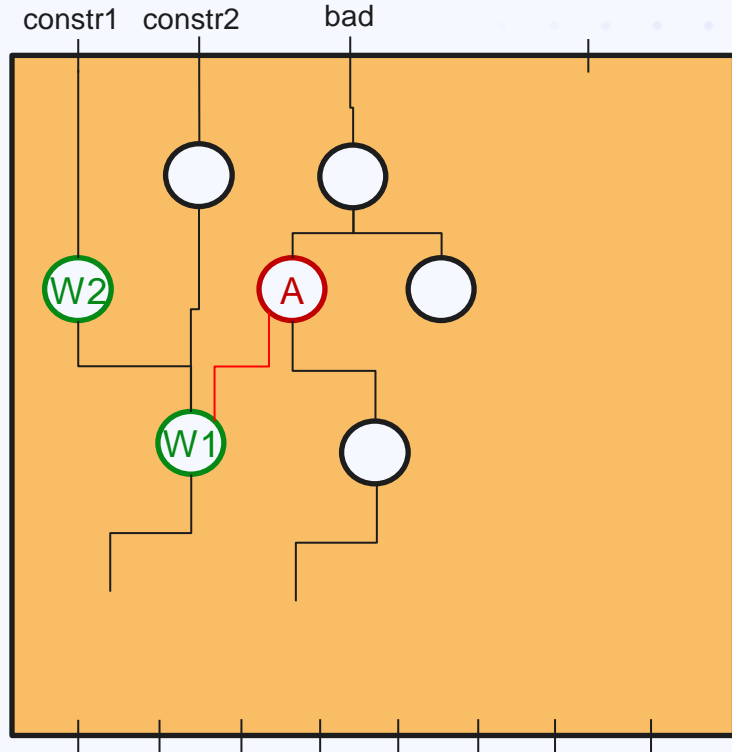
```
  ...
```

```
  assume (constr2);
```

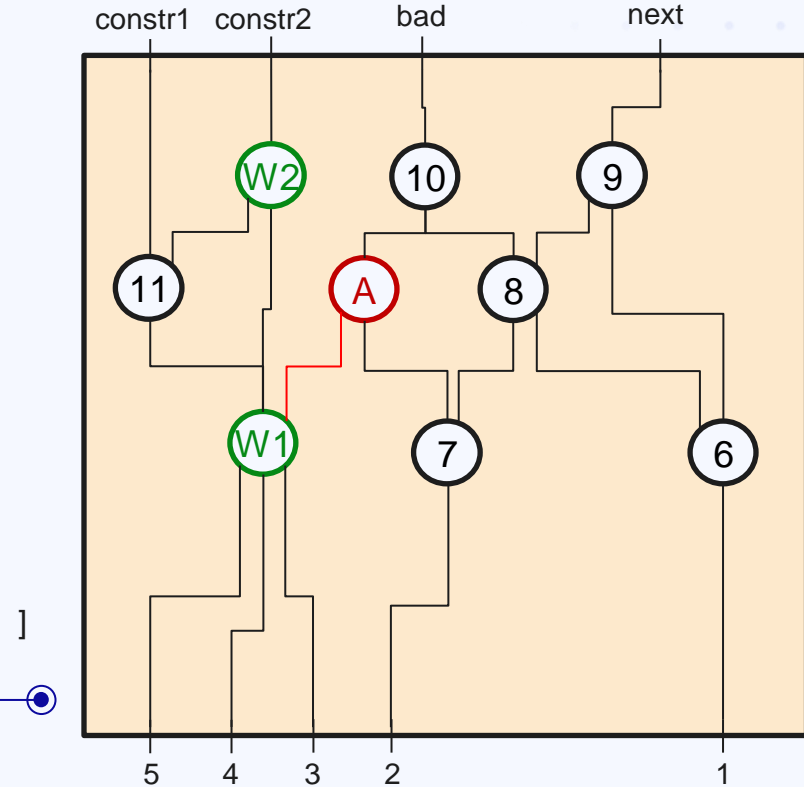
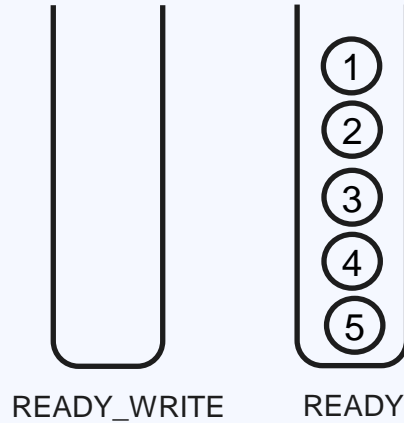
```
  ...
```

```
  assert(bad);
```

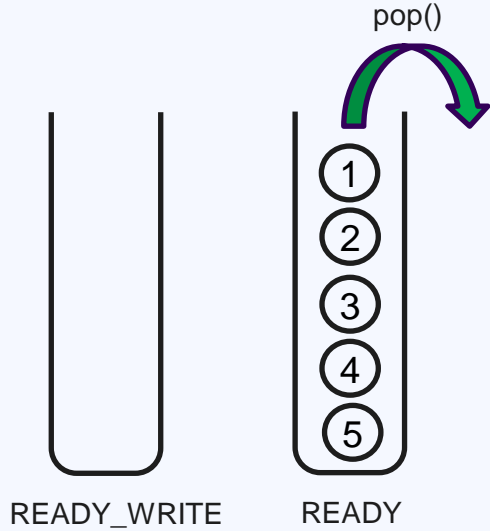
```
}
```



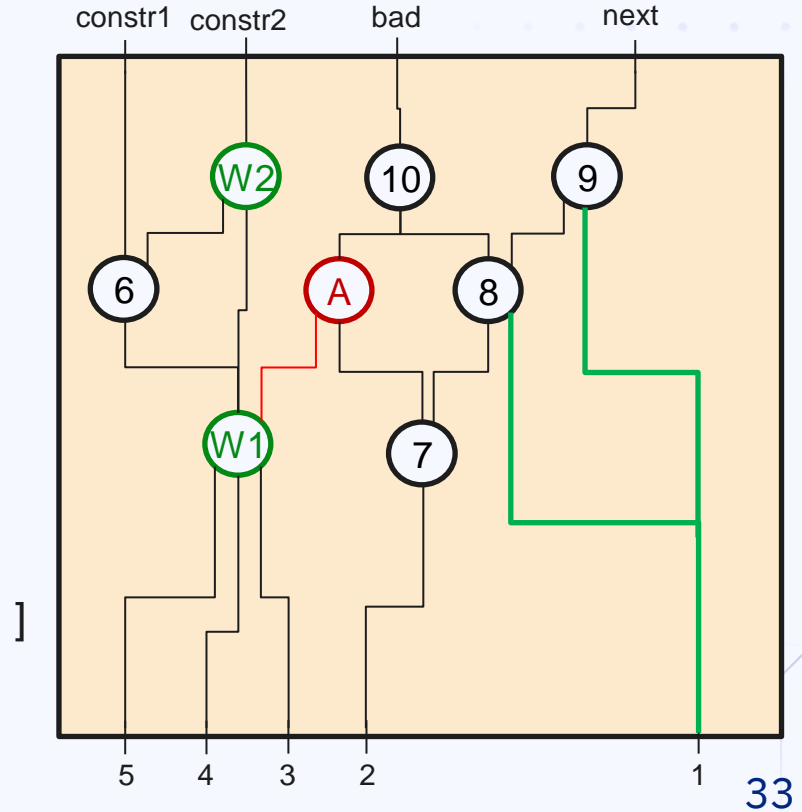
(2) ALAP-Scheduling of write-ops



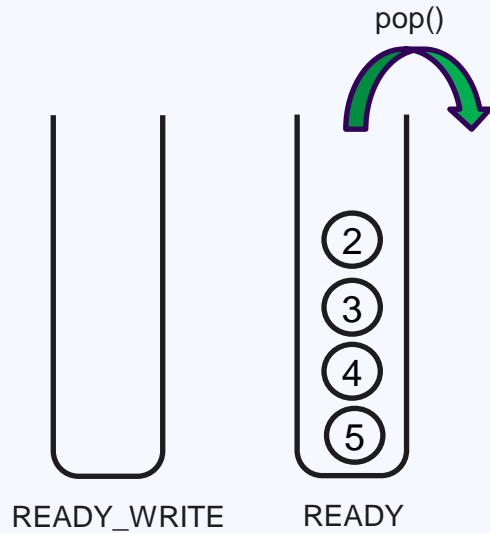
(2) ALAP-Scheduling of write-ops



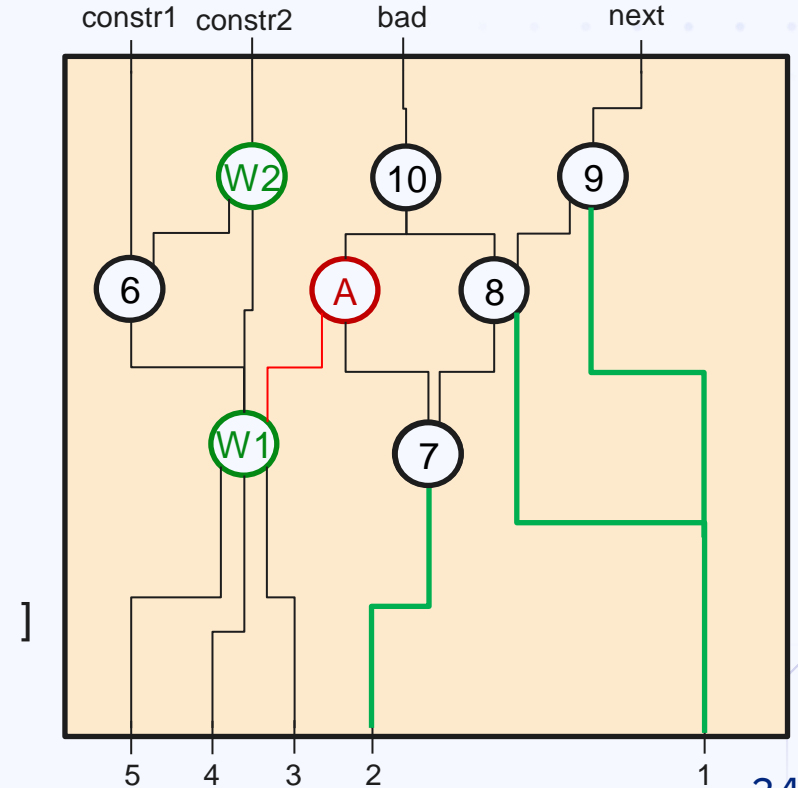
SCHEDULE = [①



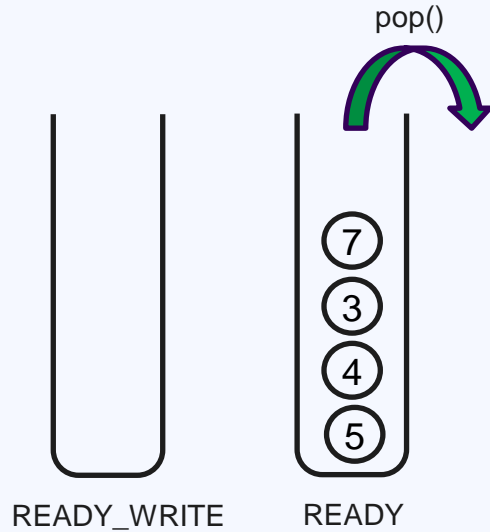
(2) ALAP-Scheduling of write-ops



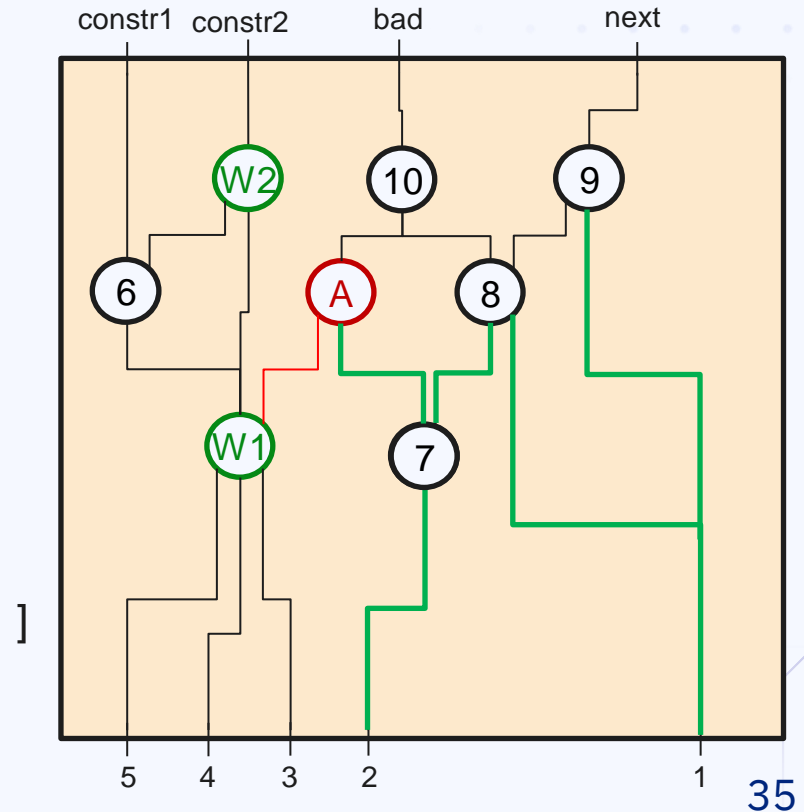
SCHEDULE = [①②]



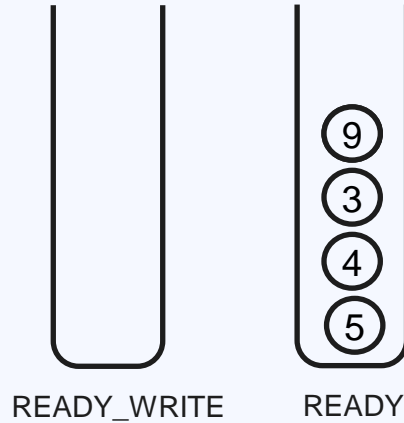
(2) ALAP-Scheduling of write-ops



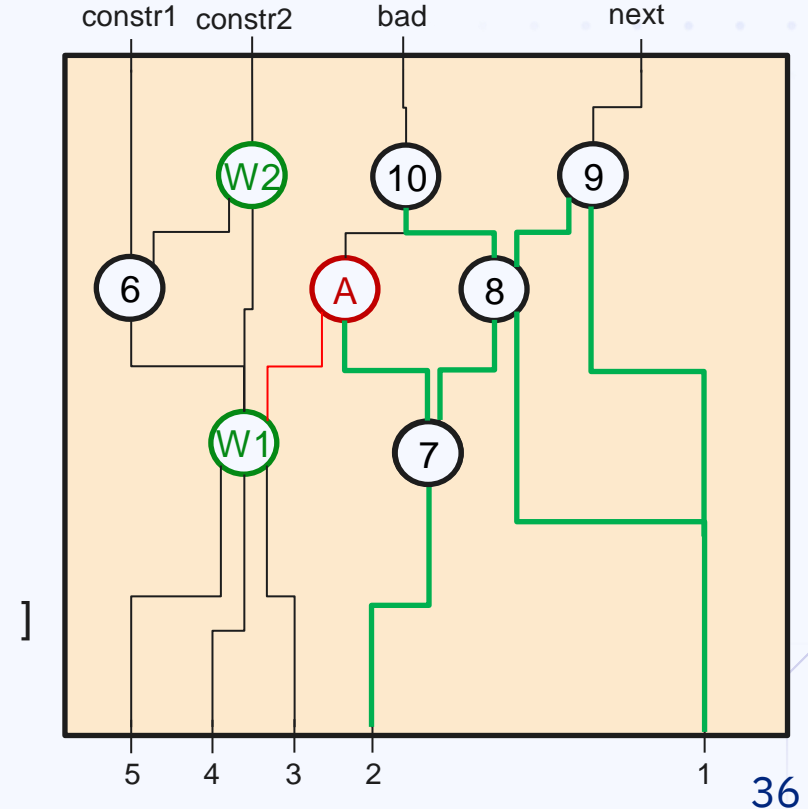
SCHEDULE = [①②⑦]



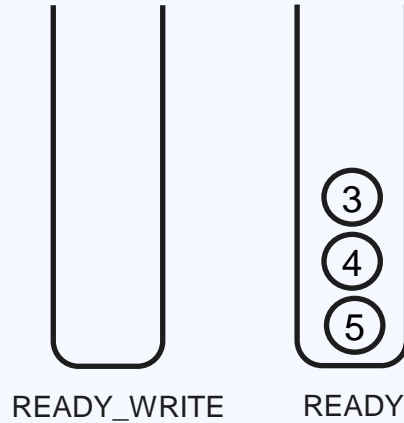
(2) ALAP-Scheduling of write-ops



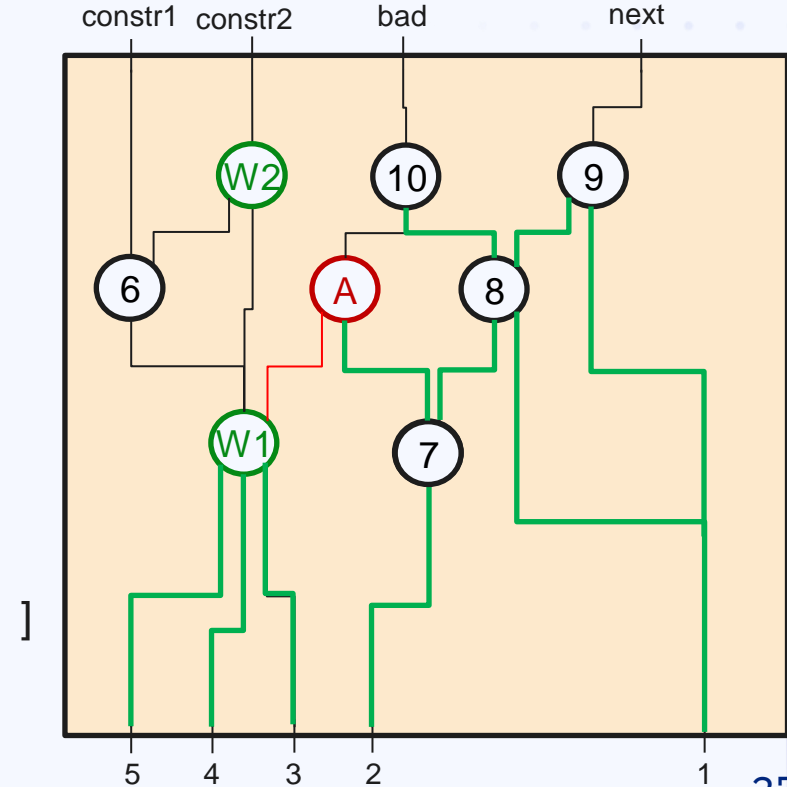
SCHEDULE = [1 2 7 8 9]



(2) ALAP-Scheduling of write-ops



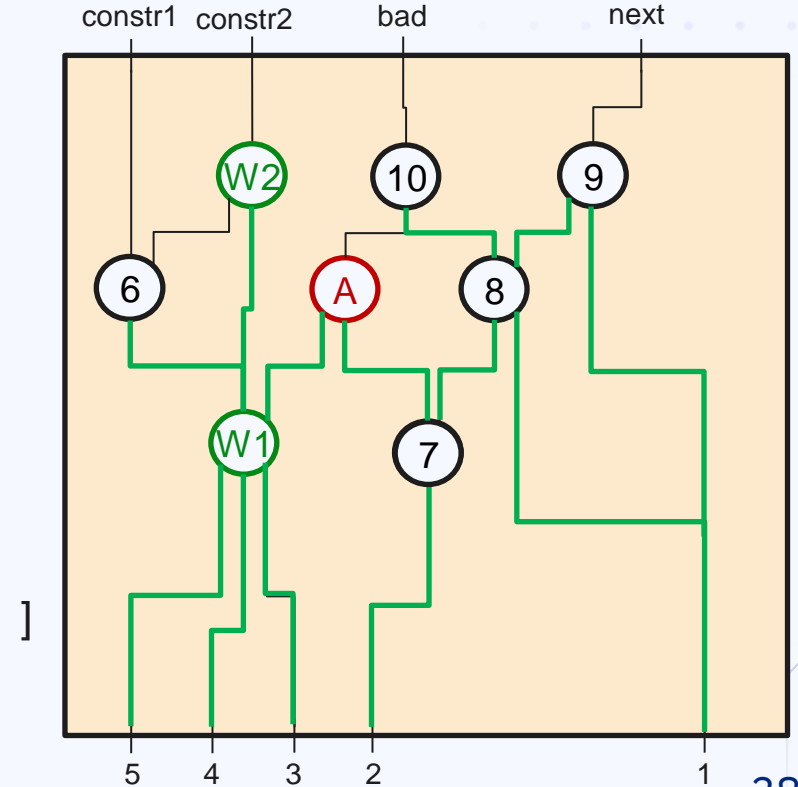
SCHEDULE = [1, 2, 7, 8, 9, 3, 4, 5]



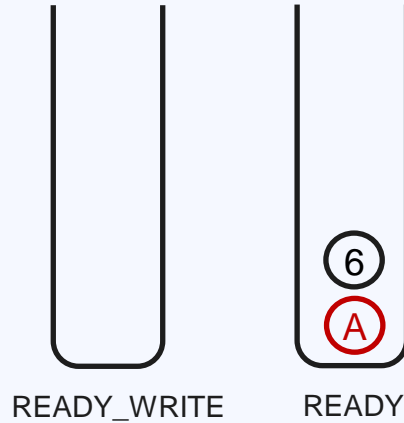
(2) ALAP-Scheduling of write-ops



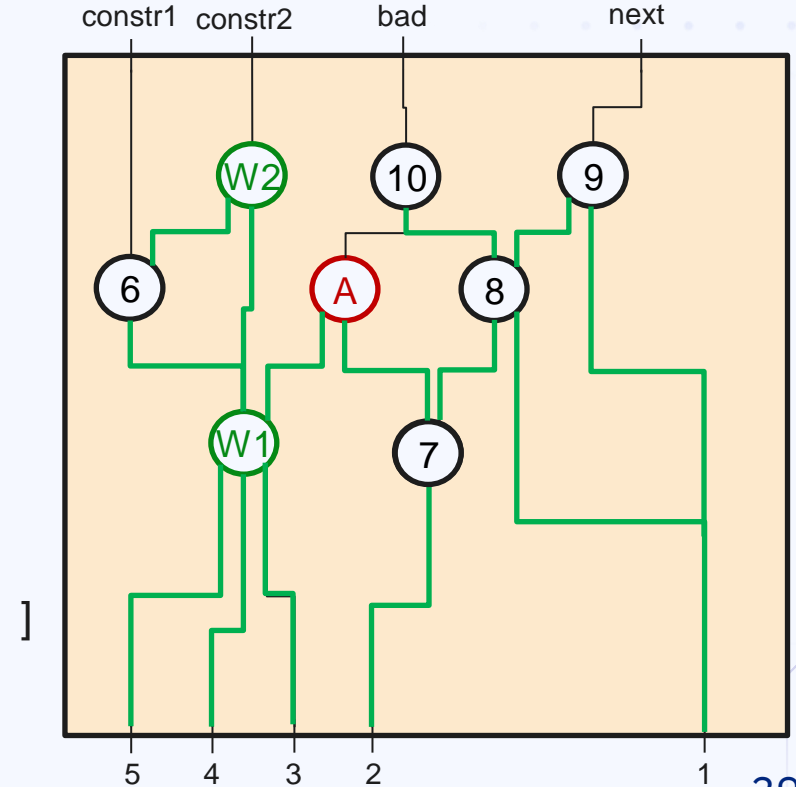
SCHEDULE = [1 2 7 8 9 3 4 5 W1]



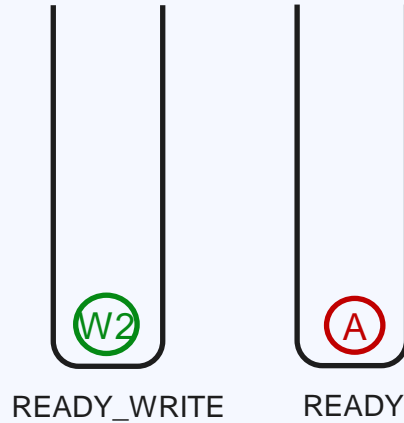
(2) ALAP-Scheduling of write-ops



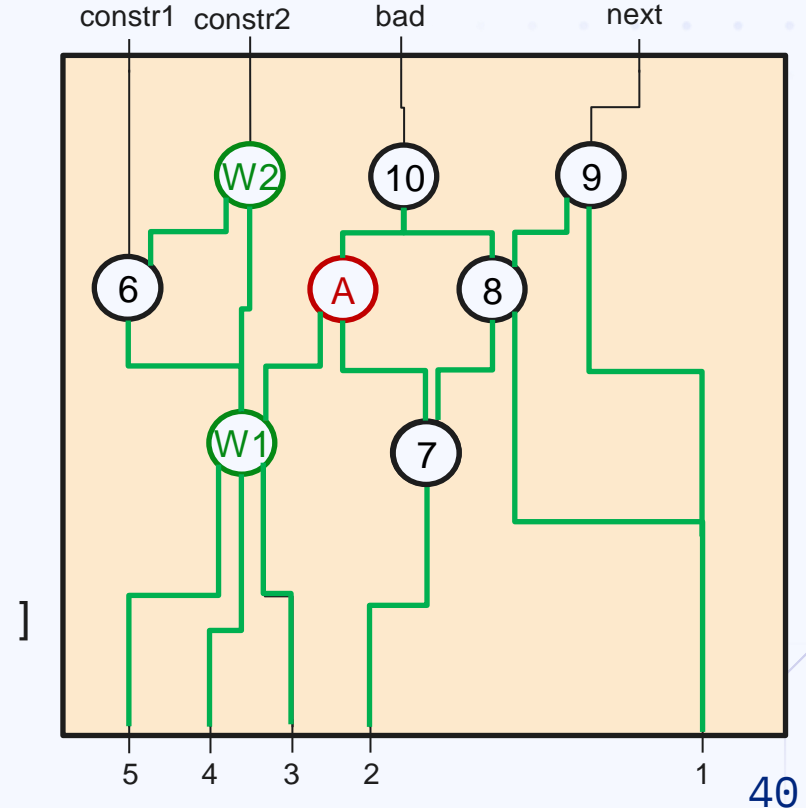
SCHEDULE = [1 2 7 8 9 3 4 5 W1 6]



(2) ALAP-Scheduling of write-ops



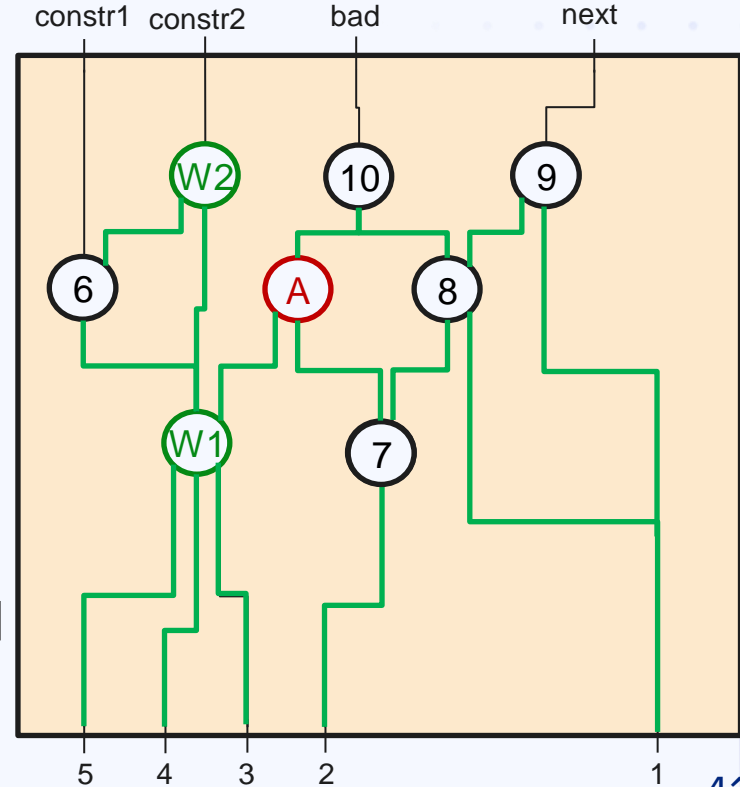
SCHEDULE = [1 2 7 8 9 3 4 5 W1 6 A]



(2) ALAP-Scheduling of write-ops



SCHEDULE = [1 2 7 8 9 3 4 5 W1 6 A 10 W2]





ing of write-ops

constr1 constr2 bad next

```
for(;;) {
```



```
assume(constr1);
```

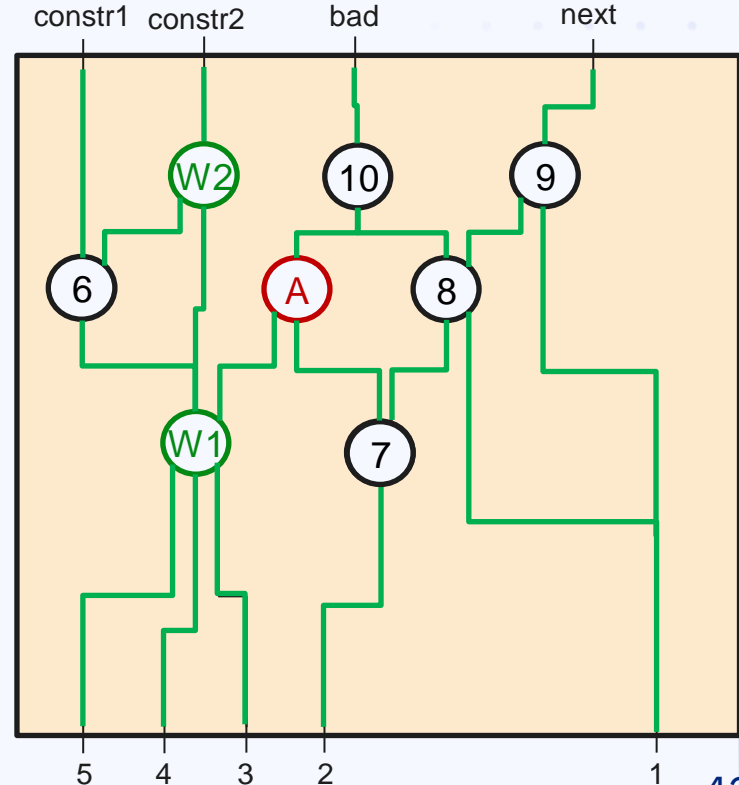
```
assume(constr2);
```

```
assert(bad);
```

```
state_x = next_arg
```

}

SCHEDULE = [1 2 7 8 9 3 4 5 W1 6 A 10 W2]



(2) ALAP-Scheduling of write-ops

```
for(;;) {
```

...

W1

A

W2

```
  assume(constr1);
```

```
  assume(constr2);
```

```
  assert(bad);
```

```
  state_x = next_arg
```

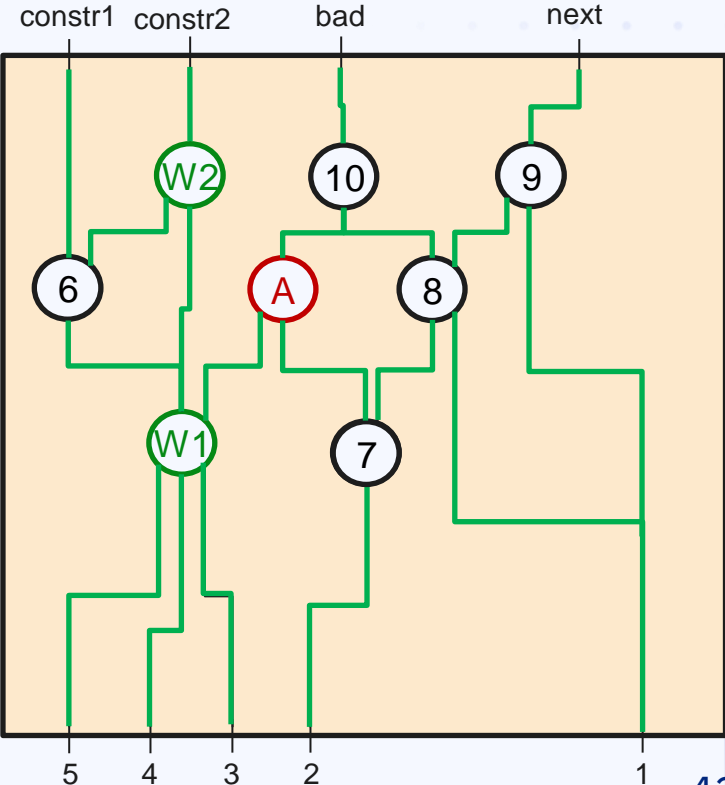
```
}
```

1. Create intermediate nodes

2. Check constraints

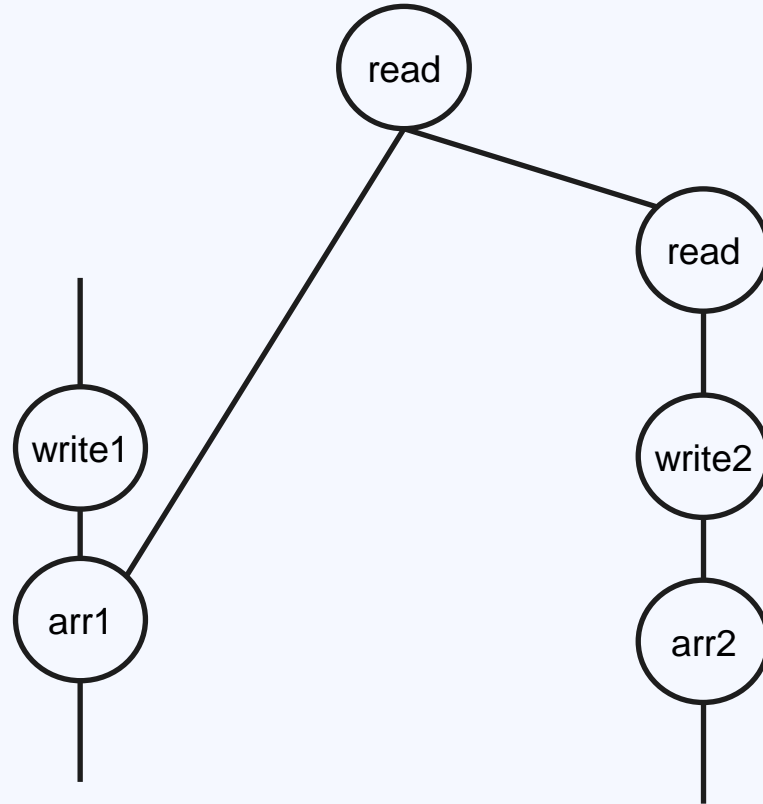
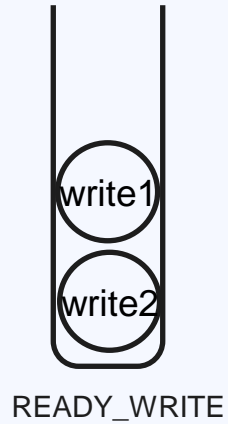
3. Check properties

4. Assign next values



SCHEDULE = [1 2 7 8 9 3 4 5 W1 6 A 10 W2]

(3) Experiments





3

Experiments

(3) Experiments

Setup:

- Ubuntu 22.04 (64 bit)
- Intel Xeon E3-1230 v5 (8 cores)
- 33 GB RAM

Limits for each task:

- 2 CPU cores
- 15 min of CPU time
- 15 GB RAM

Verifiers:

- ABC
- AVR
- CPAchecker
- ESBMC
- CBMC

Tasks:

- Collection of Btor2 tasks used in Btor2C paper
- 318 tasks for AVR
- 175 tasks for Software Verifiers
- 51 tasks for ABC
- 276 safe, 24 unsafe, 18 unknown
- Max array index bit-vector width: 12

(3) Experiments

Tool	ABC		AVR		
Algorithm	PDR		PDR		
# Tasks	51 (T: 27 F: 24)		318 (T: 294 F: 24)		
Input	AIGER		BTOR2		
Configuration	balanced	skewed	/	balanced	skewed
Proofs	11	11	129	137	136
Alarms	5	5	0	2	2
Wrong proofs	0	0	0	0	0
Wrong alarms	0	0	0	0	0
Timeouts	35	35	84	96	98
Out of memory	0	0	0	0	0
Other inconclusive	0	0	105	83	82

Total correct: 138

Total correct: 143

(3) Experiments

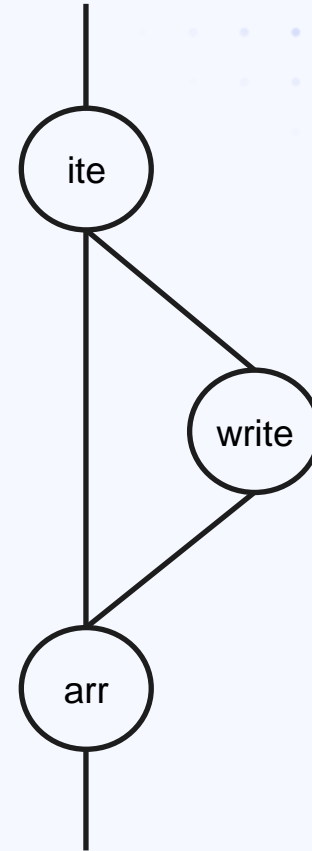
Tool	CPACHECKER				ESBMC				CBMC			
Algorithm	Pred. Abs.				k-Induction				BMC			
# Tasks	175 (T: 154 F: 21)				175 (T: 154 F: 21)				175 (T: 154 F: 21)			
Input	C				C				C			
Configuration	/	balanced	skewed	alap	/	balanced	skewed	alap	/	balanced	skewed	alap
Proofs	0	4	6	0	0	0	0	0	0	0	0	0
Alarms	0	0	0	0	2	2	2	2	19	15	15	20
Wrong proofs	0	0	0	0	0	0	0	0	0	0	0	0
Wrong alarms	0	0	0	0	0	0	0	0	0	0	0	0
Timeouts	173	167	165	173	68	48	48	69	0	0	0	0
Out of memory	0	1	1	0	104	125	125	104	91	84	87	93
Other inconclusive	2	3	3	2	1	0	0	0	65	76	73	62

Total correct: 7

(3) Experiments

1/175 Tasks avoid copies

SCHEDULE = [arr, write, ite]



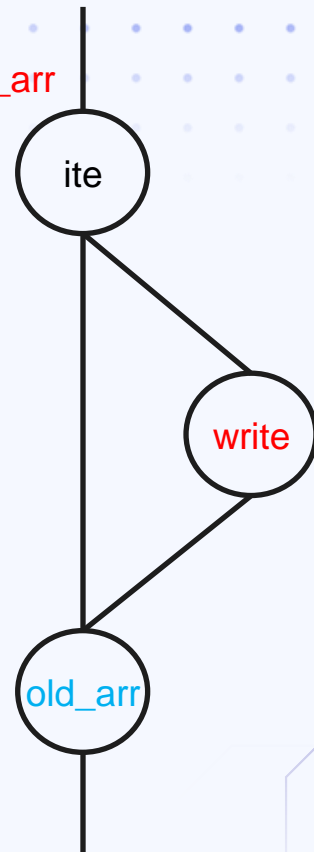
(4) Experiments

```
SORT_2 write_arr;  
for(i = 0; i < len(old_arr); ++i){  
    write_arr[i] = old_arr[i];  
}  
write_arr[arg_1] = value;
```



```
SORT_2* write_arr = old_arr;  
write_arr[arg_1] = (cond) ? old_arr[arg_1] : value;
```

ite sort_n cond old_arr write_arr



(3) Experiments

```
1 sort bitvec 1
2 sort bitvec (3-14)
3 sort bitvec 32
4 sort array 2 3
5 constd 1 0
6 constd 1 1
7 constd 2 0
8 constd 3 0
9 state 2 idx
10 state 4 mem
11 state 2 i
12 constd 2 0
13 constd 2 1
14 add 2 11 13
15 constd 2 7
16 ult 1 11 15 i_lt_const
17 ite 2 16 14 11 i_ite_res
18 next 2 11 17
19 write 4 10 11 8
20 init 2 11 7
21 ult 1 9 11
22 read 3 10 9
23 neq 1 22 8
24 and 1 21 23
25 next 4 10 19
26 bad 24
```

```
1 sort bitvec 8
2 sort bitvec (3-14)
3 sort array 2 1
4 constd 2 3
5 constd 1 8
6 state 3
7 write 3 6 4 5
8 read 1 7 4
9 constd 1 5
10 write 3 7 4 9
11 read 1 10 4
12 sort bitvec 1
13 eq 12 8 11
14 bad 13
```

```
1 sort bitvec (3-14)
2 sort array 1 1
3 state 2
4 input 1
5 constd 1 0
6 constd 1 1
7 constd 1 2
8 write 2 3 4 5
9 write 2 8 6 7
10 write 2 9 4 6
11 read 1 10 4
12 sort bitvec 1
13 eq 12 11 5
14 bad 13
```

(3) Experiments

Tool	ABC		AVR		
Algorithm	PDR		PDR		
# Tasks	36		36		
Input	AIGER		BTOR2		
Configuration	balanced	skewed	/	balanced	skewed
Proofs	33	33	24	32	29
Alarms	0	0	0	0	0
Wrong proofs	0	0	0	0	0
Wrong alarms	0	0	0	0	0
Timeouts	3	3	0	4	3
Out of memory	0	0	0	0	0
Other inconclusive	0	0	12	0	4
			Total correct:33		
			Total correct: 36		

(3) Experiments

Tool	CPACHECKER				ESBMC			
Algorithm	Pred. Abs.				k-Induction			
# Tasks	36				36			
Input	C				C			
Configuration	/	balanced	skewed	alap	/	balanced	skewed	alap
Proofs	4	14	16	25	25	18	18	25
Alarms	0	0	0	0	0	0	0	0
Wrong proofs	0	0	0	0	0	0	0	0
Wrong alarms	0	0	0	0	0	0	0	0
Timeouts	29	12	8	8	8	0	0	10
Out of memory	0	0	2	0	3	18	18	1
Other inconclusive	3	10	10	3	0	0	0	0

Total correct: 16

Total correct: 17

Total correct: 26

Total correct: 18

Total correct: 30

Total correct: 30

4

Conclusion

(4) Conclusion

- Btor2blaster increased number of proofs overall
- 51 out of 318 array containing Btor2 tasks can now be used with ABC
- Usage of both options (skewed and balanced) can increase total number of proofs and alarms
- ITE pattern occurs in all but one task of the collection which makes copies necessary (future work: identify pattern reliably and avoid copy)
- ALAP-Scheduling works as intended on manually created tasks but **doesn't guarantee optimum** (future work: integer linear programming for optimal scheduling)
- Array problem likely caused by SMT solver